

Realizing Richard Feynman's Dream of a Quantum Simulator

IB, KITP Public Lecture 28 September, 2016



www.quantum-munich.de

Overview

Motivation

Matter as a Wave

The Path to Ultracold Quantum Matter

Optical Crystal Formed by Laser Light

Applications

Outlook

- **Understand and Design Quantum Materials** - one of the biggest challenge of Quantum Physics in the 21st Century

- **Technological Relevance**

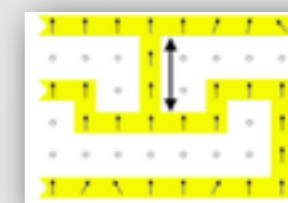
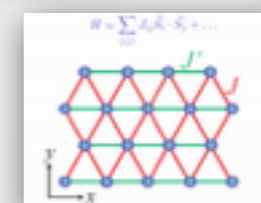
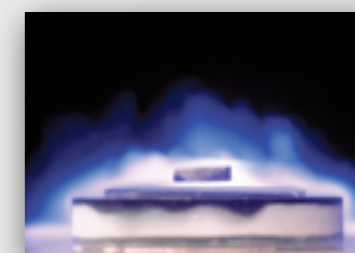
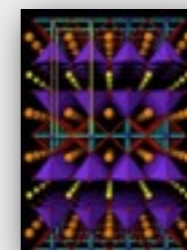
High-Tc Superconductivity (Power Delivery)

Magnetism (Storage, Spintronics...)

Novel Quantum Sensors (Precision Detectors)

Quantum Technologies

(Quantum Computing, Metrology, Quantum Sensors,...)



Many cases: lack of basic understanding of underlying processes

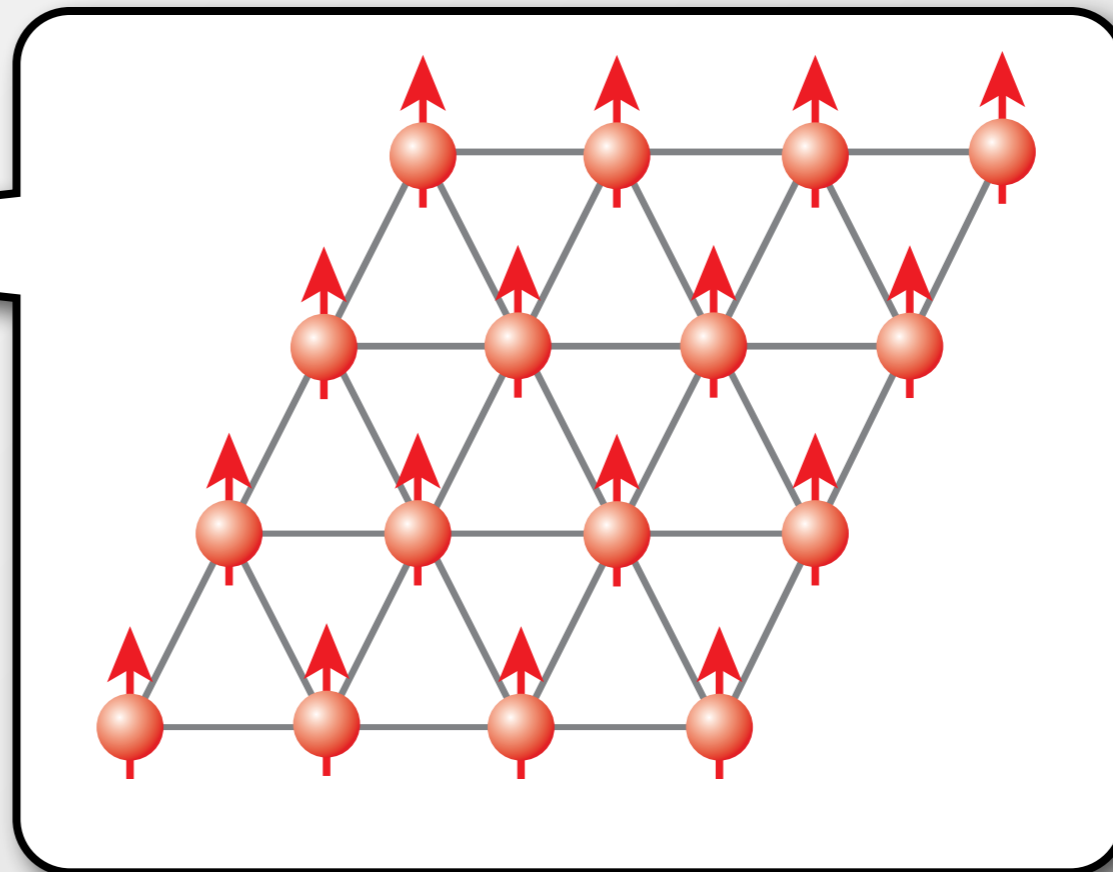
Difficulty to separate effects: probe impurities, complex interplay, masking of effects...

Many cases: even simple models “not solvable”

Need to synthesize new material to analyze effect of parameter change

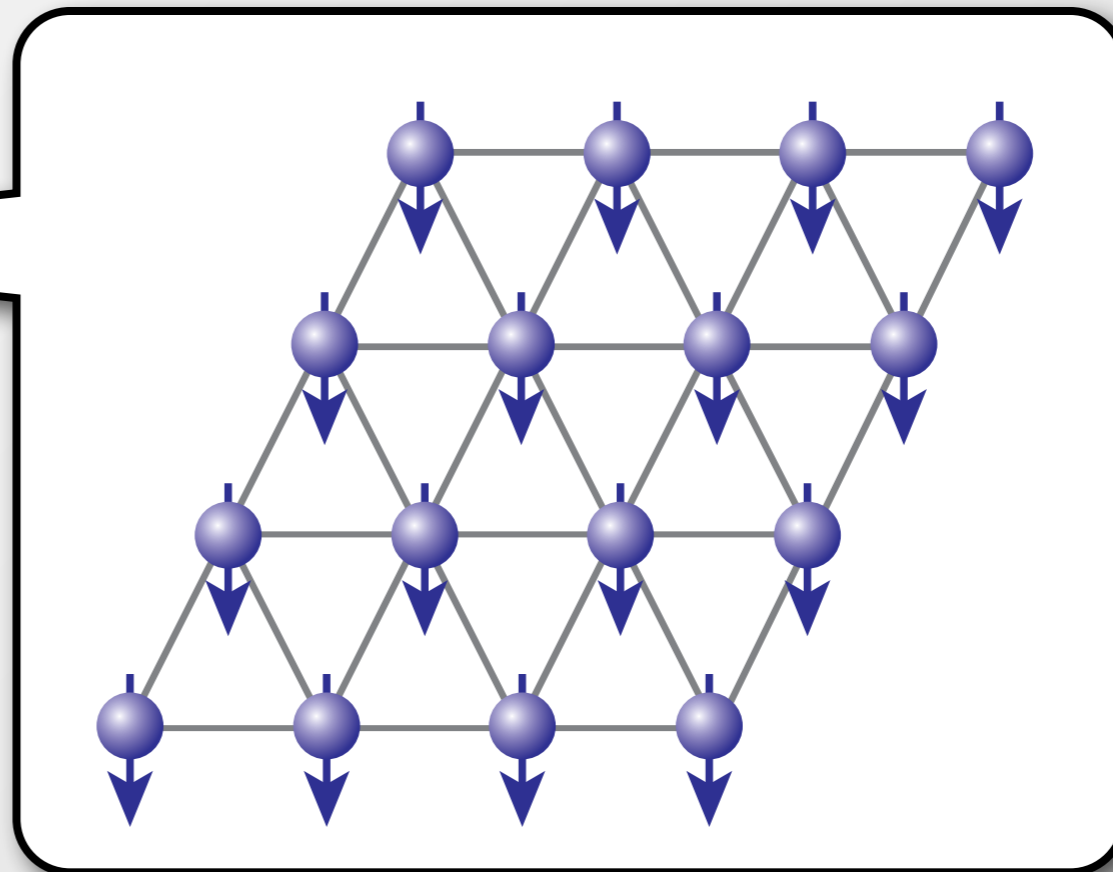


the 'ultimate' hard drive



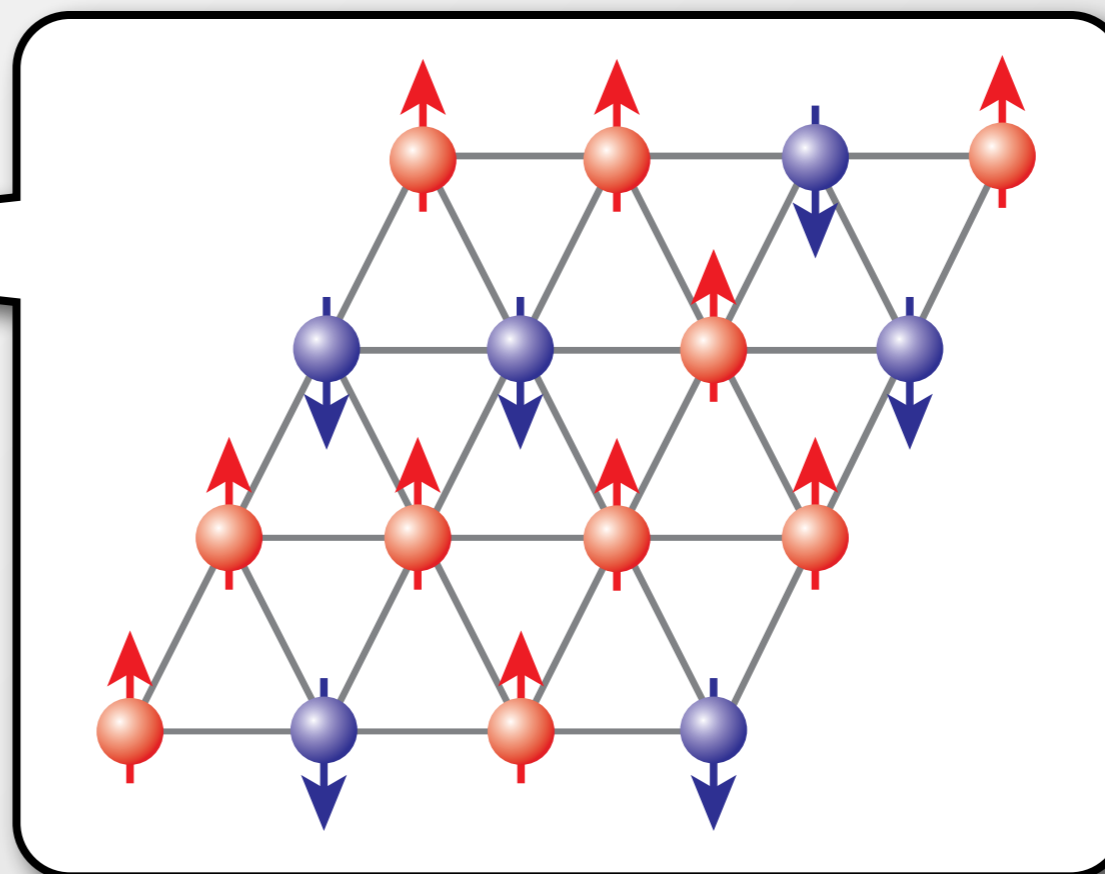
Crystal of spins

the 'ultimate' hard drive



Crystal of spins

the 'ultimate' hard drive



Crystal of spins

$$|\Psi\rangle = c_1 \left| \begin{array}{c} \uparrow \uparrow \uparrow \uparrow \\ \uparrow \uparrow \uparrow \\ \uparrow \uparrow \\ \uparrow \end{array} \right\rangle + c_2 \left| \begin{array}{c} \uparrow \uparrow \uparrow \uparrow \\ \uparrow \uparrow \downarrow \uparrow \\ \uparrow \uparrow \uparrow \\ \uparrow \uparrow \downarrow \uparrow \end{array} \right\rangle + \dots + c_{2^N} \left| \begin{array}{c} \downarrow \downarrow \downarrow \downarrow \\ \downarrow \downarrow \downarrow \\ \downarrow \downarrow \\ \downarrow \end{array} \right\rangle$$

AND AND AND

2^N Configurations simultaneously!

$$|\Psi\rangle = c_1 \left| \begin{array}{c} \uparrow \uparrow \uparrow \uparrow \\ \uparrow \uparrow \uparrow \\ \uparrow \uparrow \\ \uparrow \end{array} \right\rangle + c_2 \left| \begin{array}{c} \uparrow \uparrow \uparrow \uparrow \\ \uparrow \uparrow \downarrow \uparrow \\ \uparrow \uparrow \uparrow \\ \uparrow \uparrow \downarrow \uparrow \end{array} \right\rangle + \dots + c_{2^N} \left| \begin{array}{c} \downarrow \downarrow \downarrow \downarrow \\ \downarrow \downarrow \downarrow \\ \downarrow \downarrow \\ \downarrow \end{array} \right\rangle$$

AND AND AND

2^N Configurations simultaneously!

Roadrunner – Los Alamos



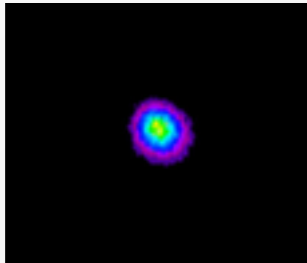
1.1 Petaflops/s
2000 t
3.9 MW

State of the art: < 40 spins ($2^{40} \times 2^{40}$) (what does it take to simulate 300 spins ?)

each doubling allows for one more spin 1/2 only

2^{300} estimated number of protons in the universe

Control of single and few particles



Single Atoms and Ions



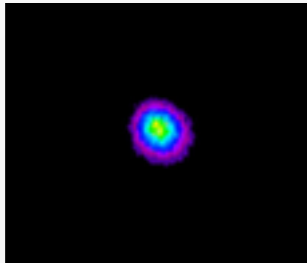
Photons



D. Wineland

S. Haroche

Control of single and few particles



Single Atoms and Ions



Photons



D. Wineland

S. Haroche

Challenge: ... towards ultimate control of many-body quantum systems

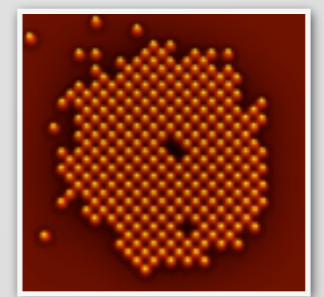


R. P. Feynman's Vision

A *Quantum Simulator* to study the dynamics of another quantum system.



Ion Traps
(R. Blatt, Innsbruck)



Crystal of Atoms
Bound by Light



Superconducting
Devices
(J. Martinis, UCSB,
Google)

Control of single and few particles

Simulating Physics with Computers

Richard P. Feynman

Department of Physics, California Institute of Technology, Pasadena, California 91107

Received May 7, 1981

1. INTRODUCTION

On the program it says this is a keynote speech—and I don't know what a keynote speech is. I do not intend in any way to suggest what should be in this meeting as a keynote of the subjects or anything like that. I have my own things to say and to talk about and there's no implication that anybody needs to talk about the same thing or anything like it. So what I want to talk about is what Mike Dertouzos suggested that nobody would talk about. I want to talk about the problem of simulating physics with computers and I mean that in a specific way which I am going to explain. The reason for doing this is something that I learned about from Ed Fredkin, and my entire interest in the subject has been inspired by him. It has to do with learning something about the possibilities of computers, and also something about possibilities in physics. If we suppose that we know all the physical laws perfectly, of course we don't have to pay any attention to computers. It's interesting anyway to entertain oneself with the idea that we've got something to learn about physical laws; and if I take a relaxed

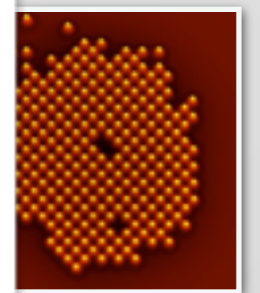
Sing

Challen



haroche

ystems



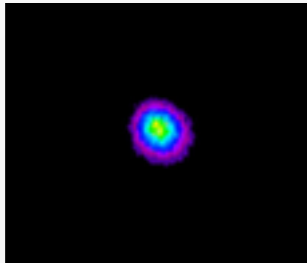
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conducting
Devices
rtinis, UCSB,
Google)



The Challenge of Many-Body Quantum Systems

Control of single and few particles



Single Atoms and Ions



Photons



D. Wineland

S. Haroche

Challenge: ... towards ultimate control of many-body quantum systems

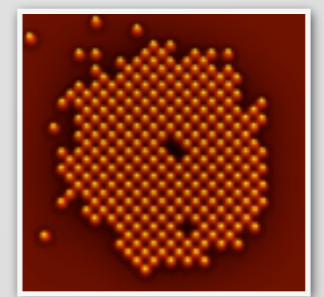


R. P. Feynman's Vision

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Crystal of Atoms
Bound by Light

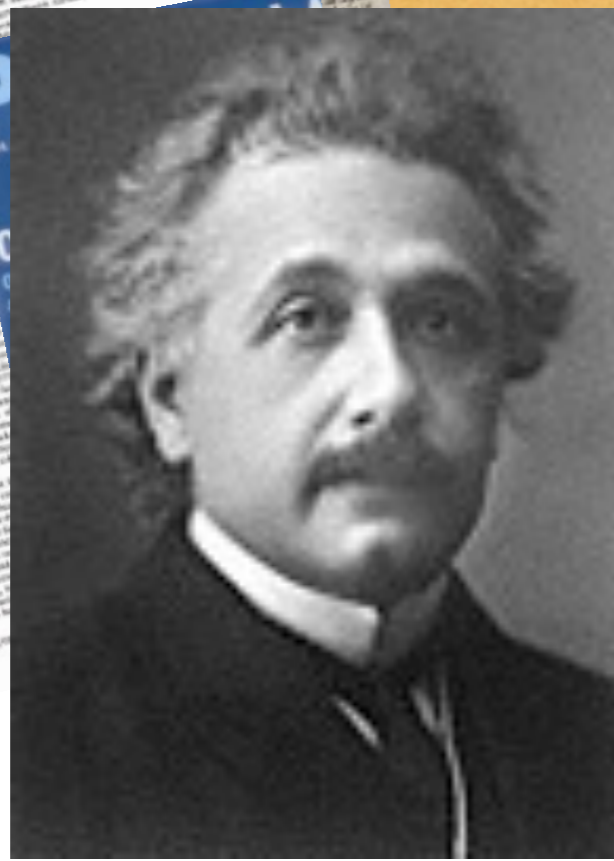
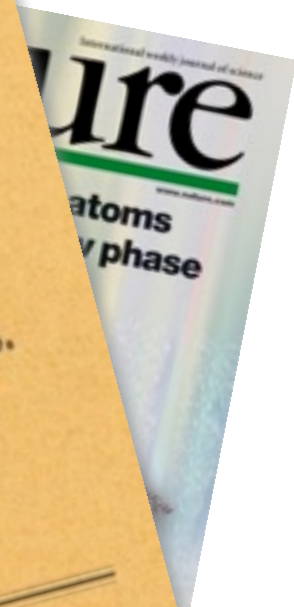
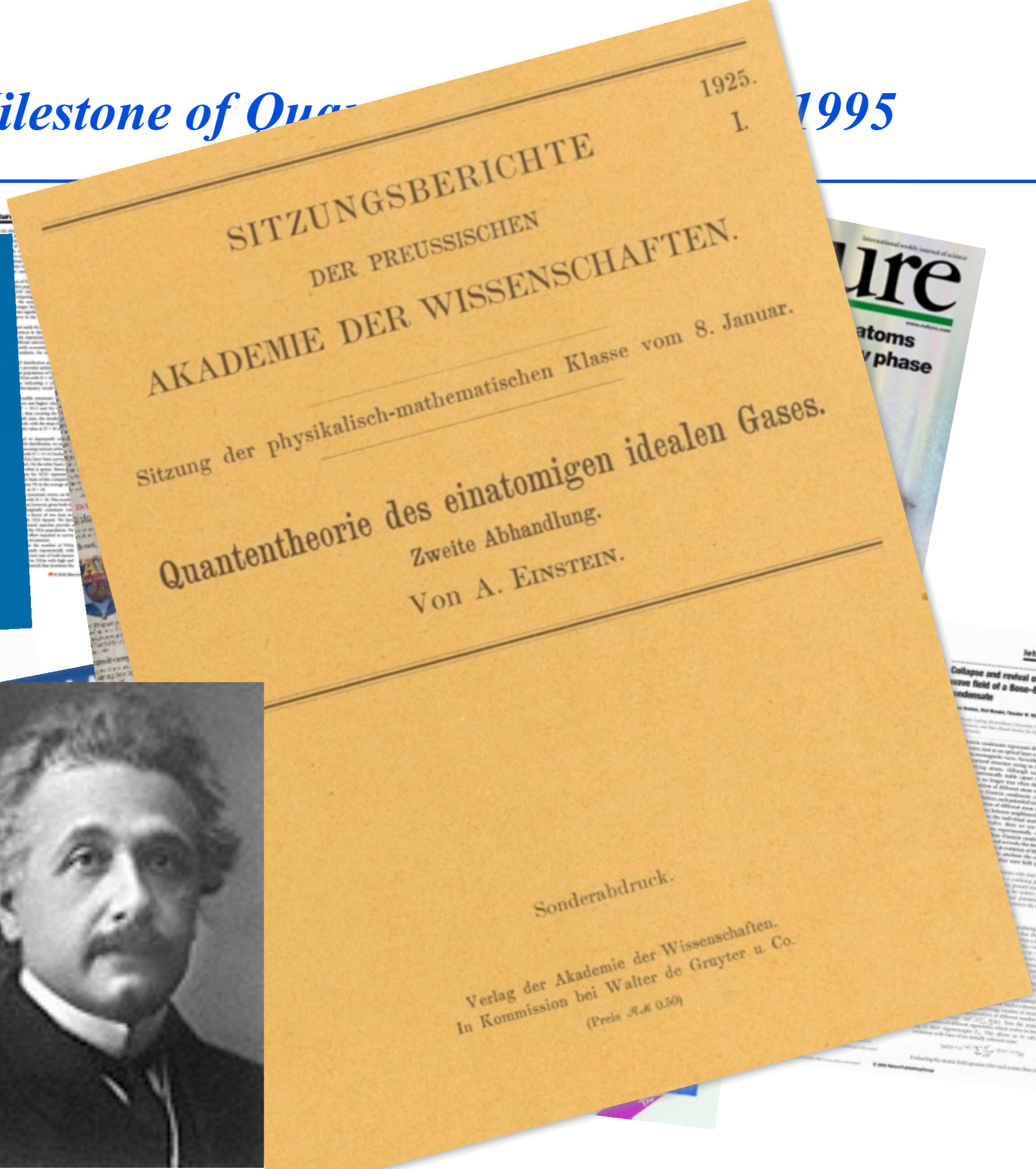


Superconducting
Devices
(J. Martinis, UCSB,
Google)

Ultracold Quantum Gases

A Milestone of Quantum

1995





Centennial Nobel Prize in Physics! (2001)

Original lab book entry from W. Ketterle!

* TOF not clean because of the Ar⁺ beam
 ⇒ install high-power AOM to switch Ar⁺ off during TOF

no stabilization of Ar⁺ position
 probe 198 MHz
 final RF 660 kHz
 66 kHz

1.17 Hz
 ~ 800 kHz
 ~ 740 kHz

again
 670 kHz
 660 kHz

off Ar⁺ during 660 kHz
 5 → 10 ms
 2e int x 4
 image defeated
 probe 197 → 192 MHz

TOF 10 → 7 ms
 final RF 660 kHz → 890 kHz
 final RF 990 kHz

5.49.59am
 5.50.26
 5.51.23
 5.52.56
 5.53.34
 5.54.52
 5.59.37
 6.00.56
 6.01.45
 6.02.42
 6.03.18
 6.04.29
 6.05.02

Ar⁺ on
 Ar⁺ off during TOF + probe
 Ar⁺ off during TOF + probe

darked bright image without atoms

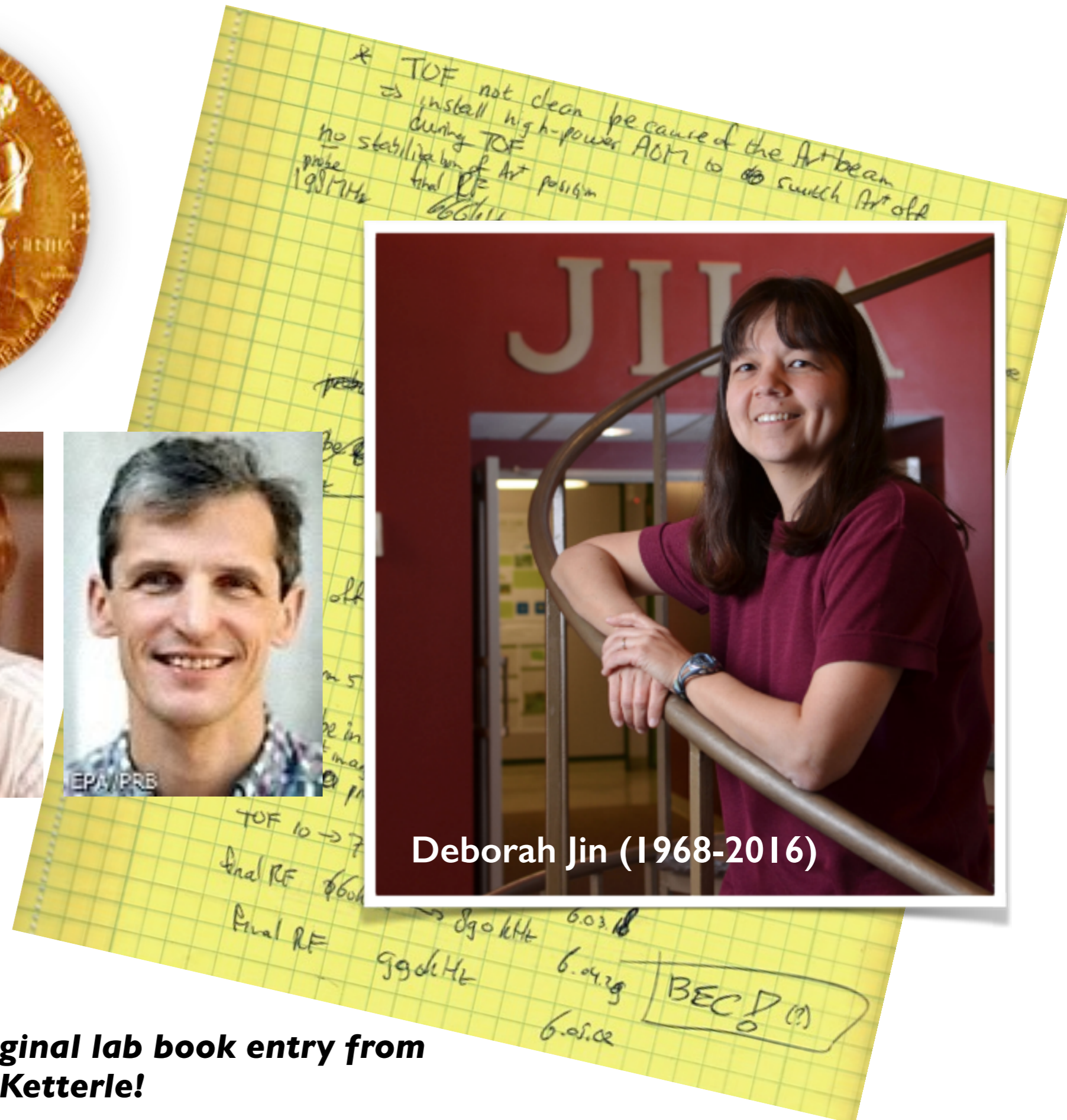
BECD (?)



Deborah Jin (1968-2016)

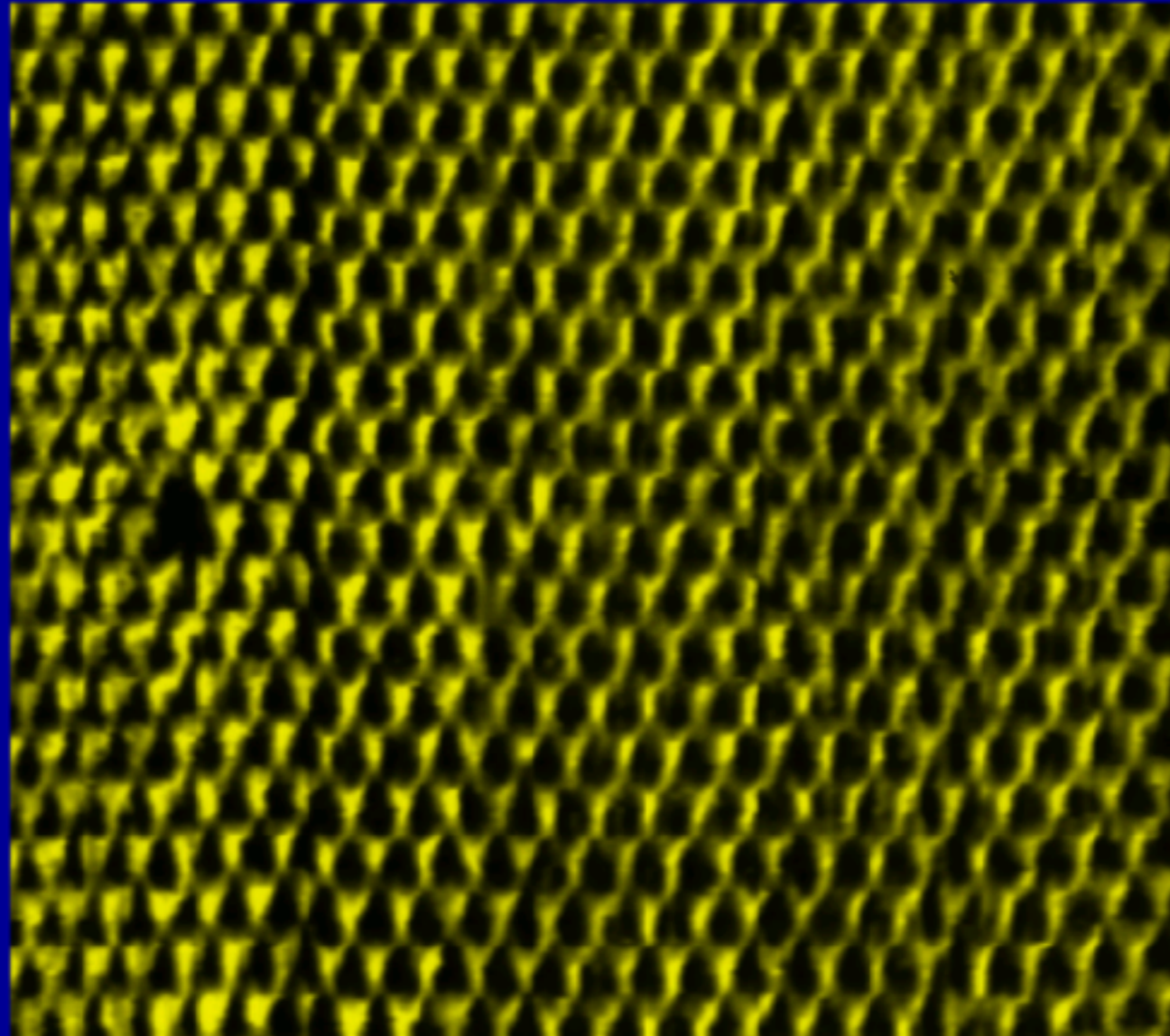
**Centennial Nobel Prize
in Physics! (2001)**

**Original lab book entry from
W. Ketterle!**



Molybdändisulfid

Schwefelatome unter dem Rastertunnelmikroskop



What is Matter ?



**Louis-Victor
de Broglie**
(1892-1987)

$$\lambda = \frac{h}{p} = \frac{h}{mv}$$

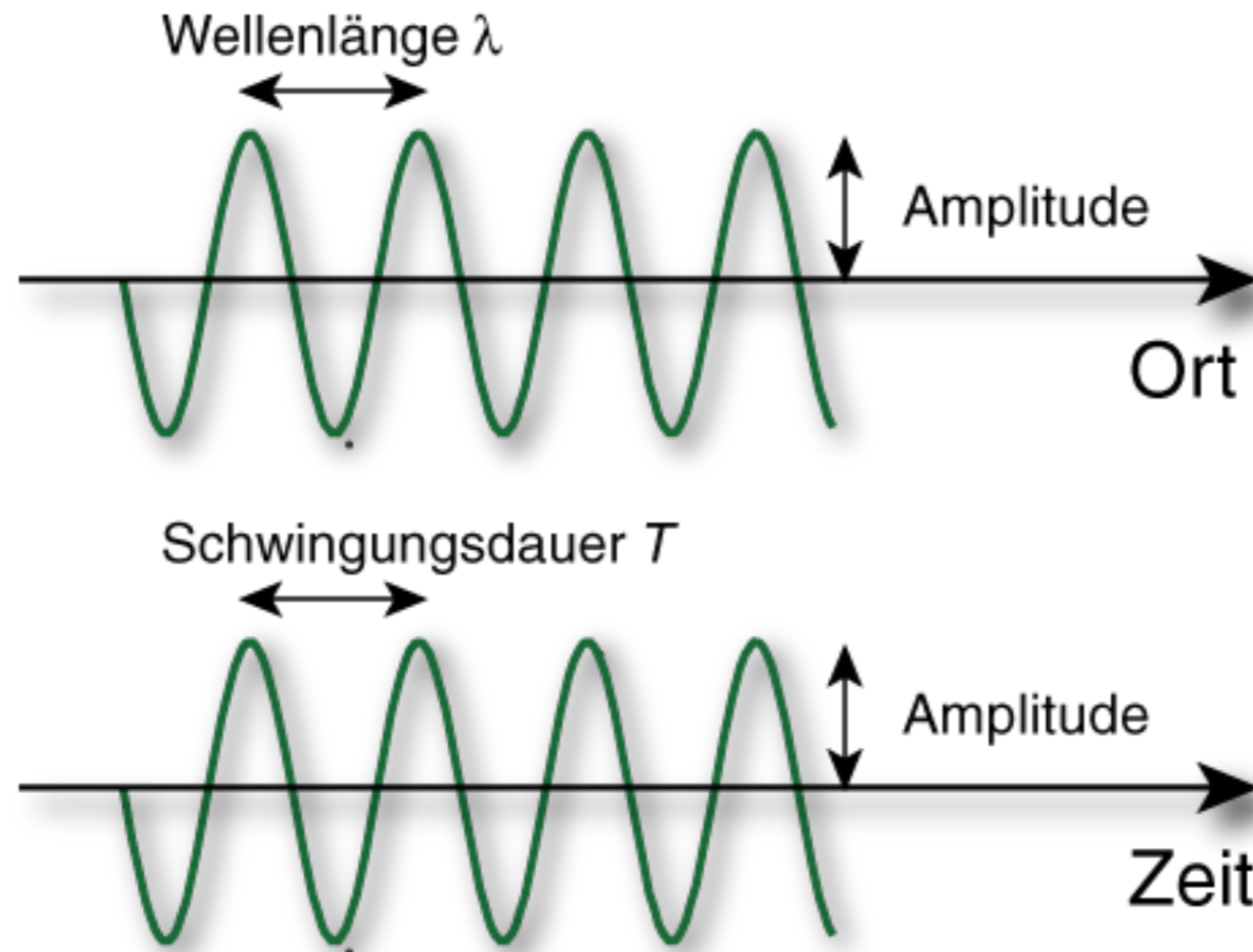


**Erwin
Schrödinger**
(1887-1961)

$$i\hbar \frac{\partial \Psi}{\partial t} = H\Psi$$



What characterizes a wave ?



Wave is a periodic oscillation in space and time !

Frequency (Oscillations per s)

$$\nu = 1/T$$

Propagation velocity:

$$c = \lambda \cdot \nu$$

1+1=2? or not ?

Matter



+

Matter

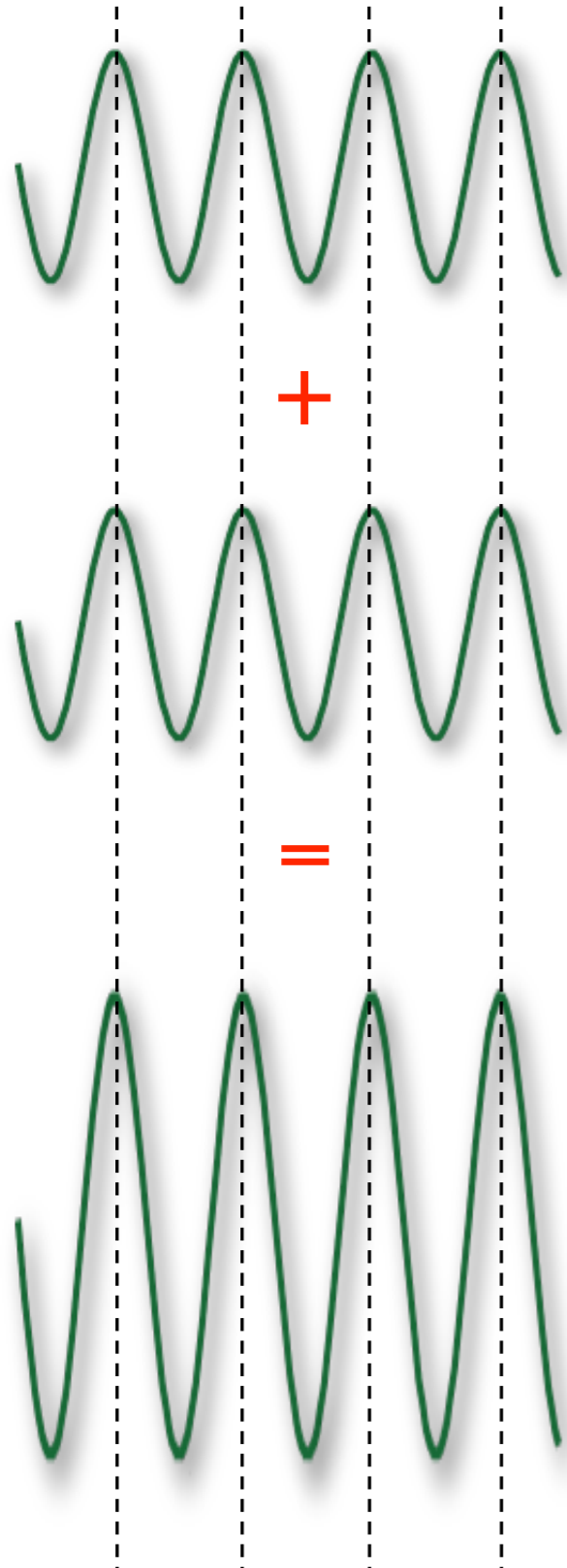


=

Twice as much matter

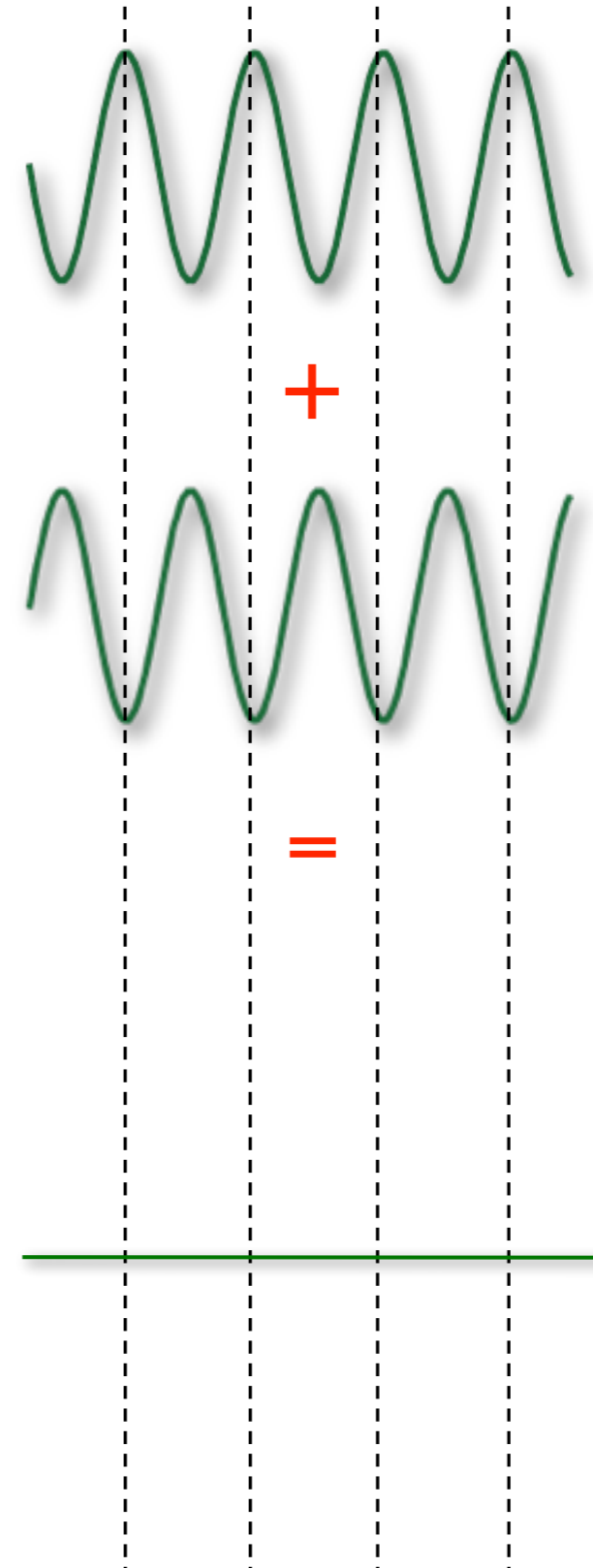


Superposition Principle for Waves



Waves can enhance each other!

constructive interference when two waves are added in phase

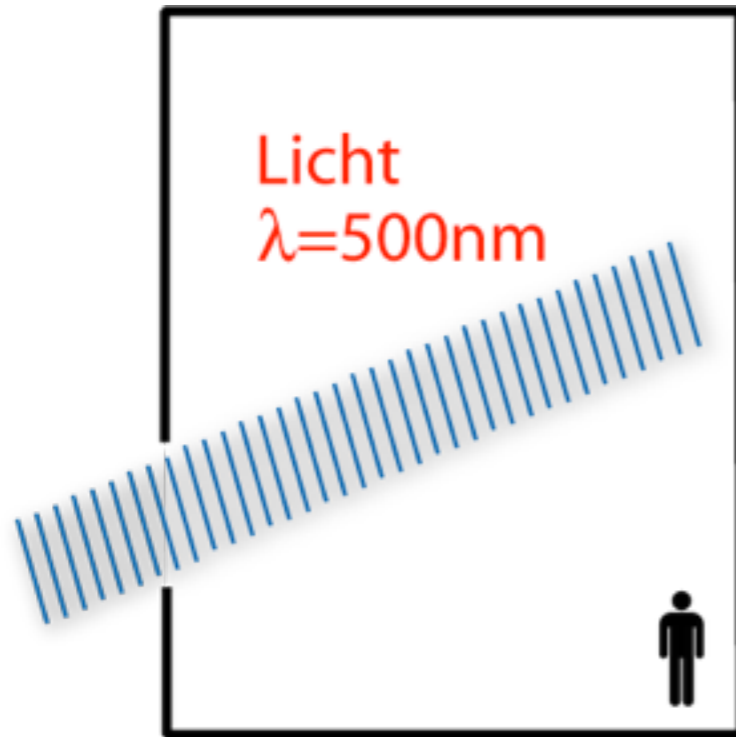


Waves can eliminate each other!

destructive interference when two waves are added $\lambda/2$ out of phase

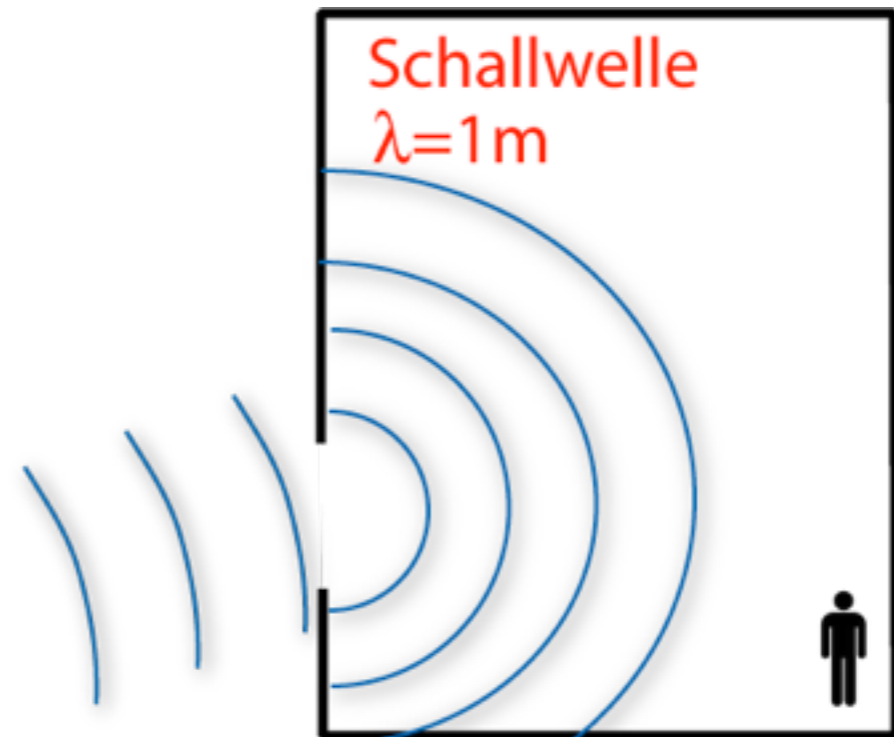
Go To Interference Program...

When can we perceive this wave character?



$\lambda \ll \text{Size of Object}$

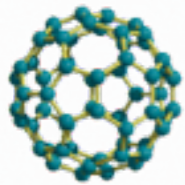
Propagation along straight lines



$\lambda \approx \text{Size of Object}$

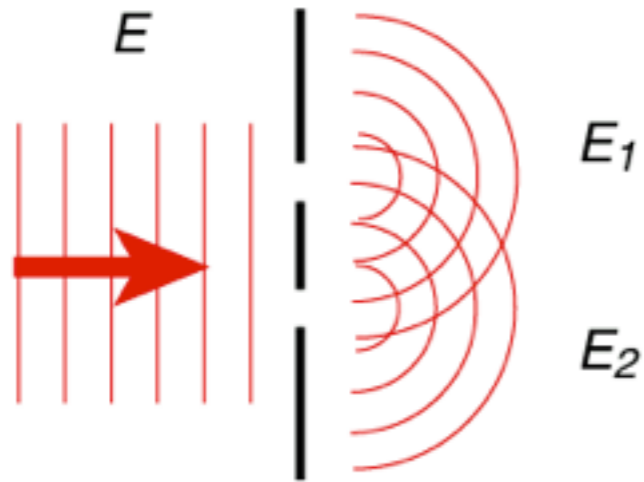
Waves are diffracted!

Objekt	m (kg)	v (m/s)	λ (mm)
Elektron	$9,1 \cdot 10^{-31}$	$2 \cdot 10^6$	$4 \cdot 10^{-7}$ (0,00000004)
Neutron	$1,7 \cdot 10^{-27}$	$4 \cdot 10^3$	$9 \cdot 10^{-8}$ (0,000000009)
⁸⁷ Rb Atom	$1,5 \cdot 10^{-25}$	270	$2 \cdot 10^{-8}$ (0,000000002)
C ₆₀	$1,2 \cdot 10^{-24}$	210	$3 \cdot 10^{-9}$ (0,0000000003)
Fussball	0,5	20	$7 \cdot 10^{-32}$ (0,000000000000000000 000000000000000000 007)



What is interfering in the case of matter waves?

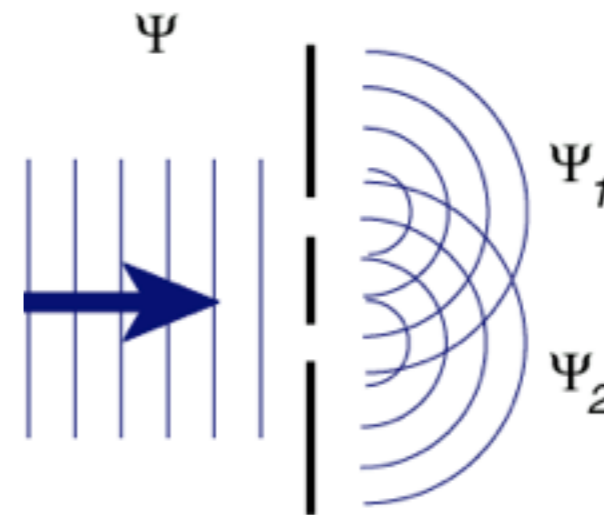
Elektromagnetische Felder



$$E_{det} = E_1 + E_2$$

$$I \propto |E_1 + E_2|^2$$

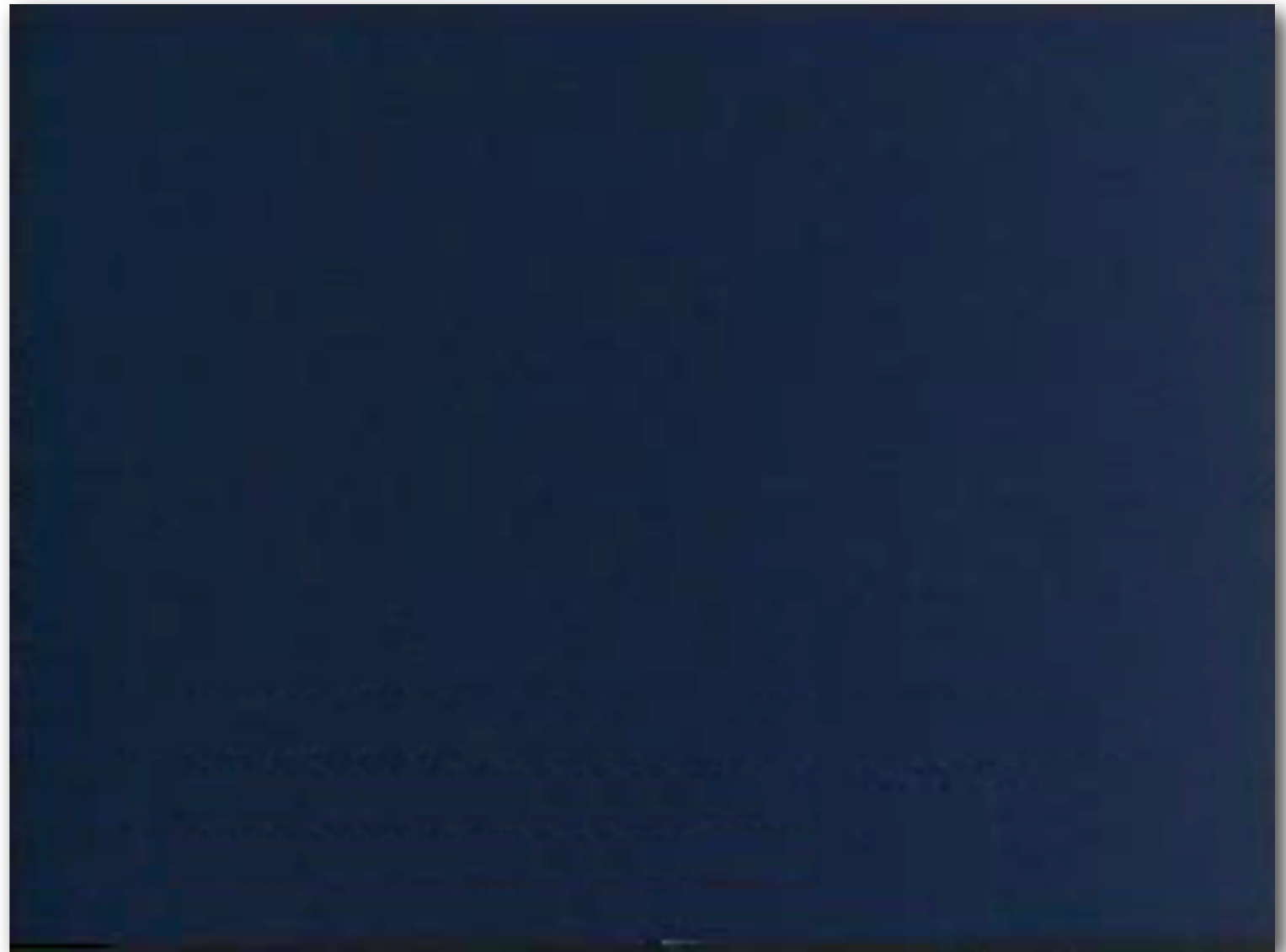
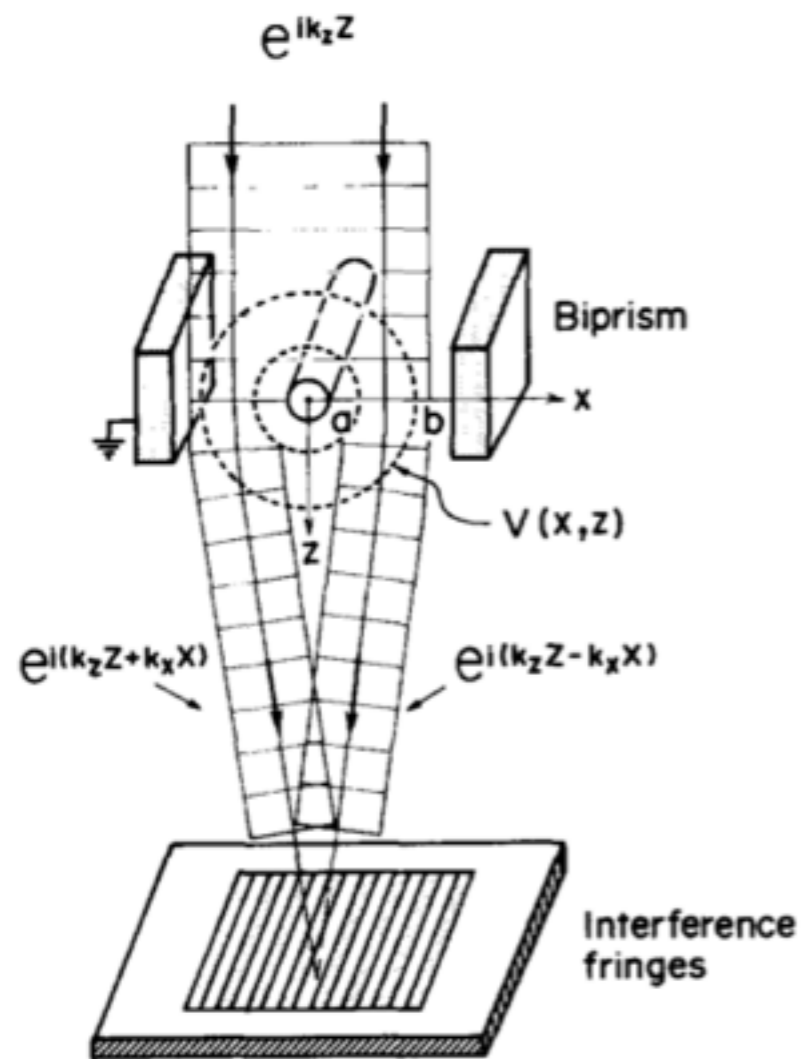
Quantenmechanische Wellenfunktionen



$$\Psi_{det} = \Psi_1 + \Psi_2$$

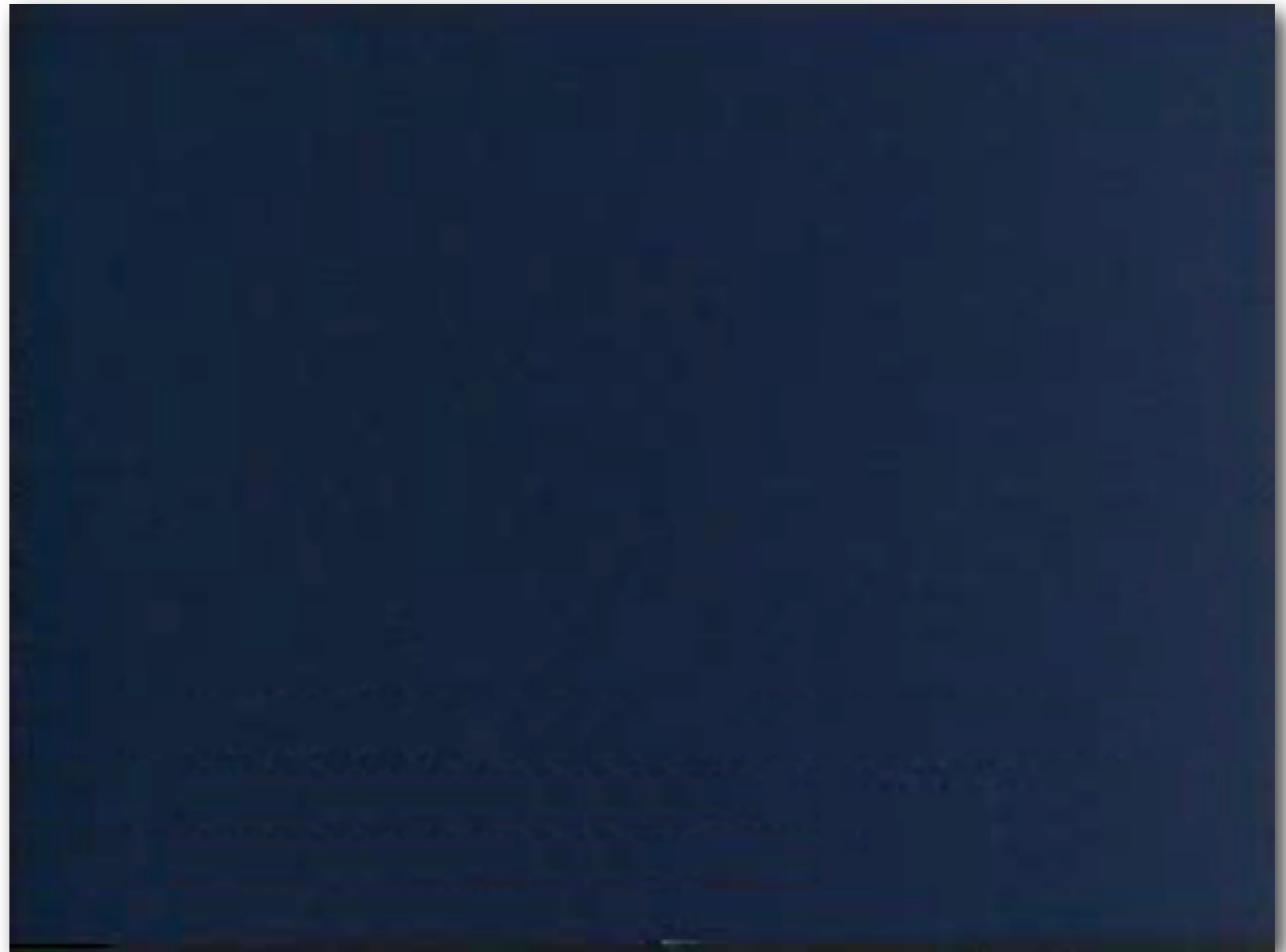
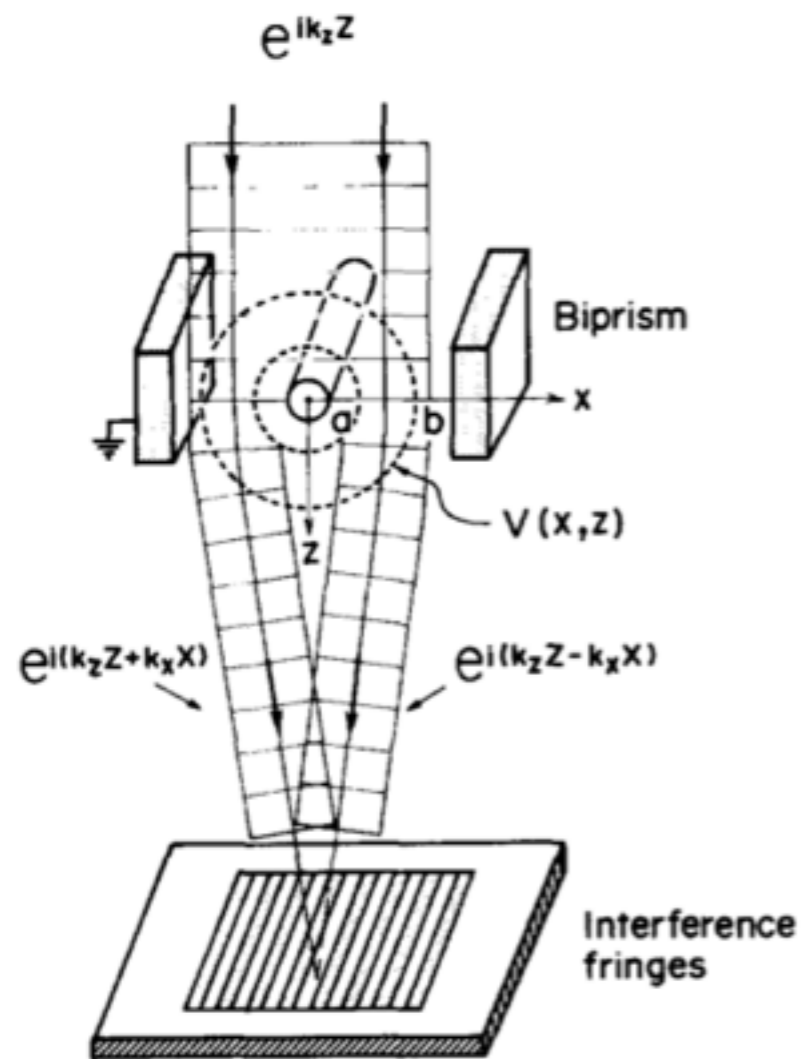
$$n \propto |\Psi_1 + \Psi_2|^2$$

Single Electron on Double Slit



A. Tonomura et al., Amer. J. Phys. **57** (1989) pp.117-120.

Single Electron on Double Slit



A. Tonomura et al., Amer. J. Phys. **57** (1989) pp.117-120.

Interference Phenomena with Matter Waves (2)

Beugung an einer Folie:

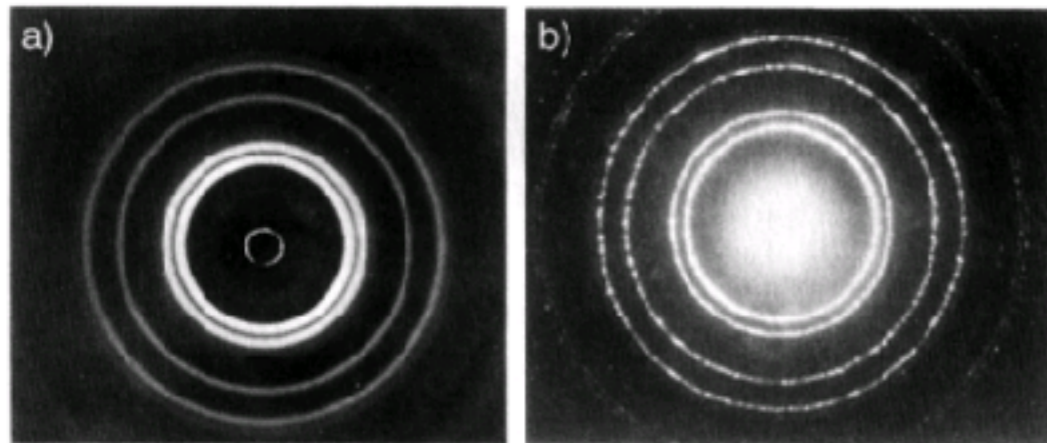
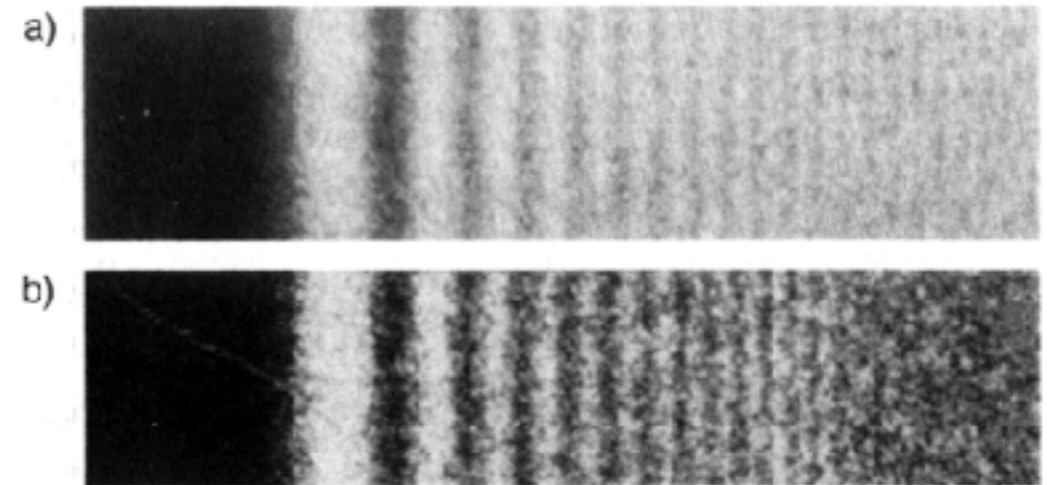
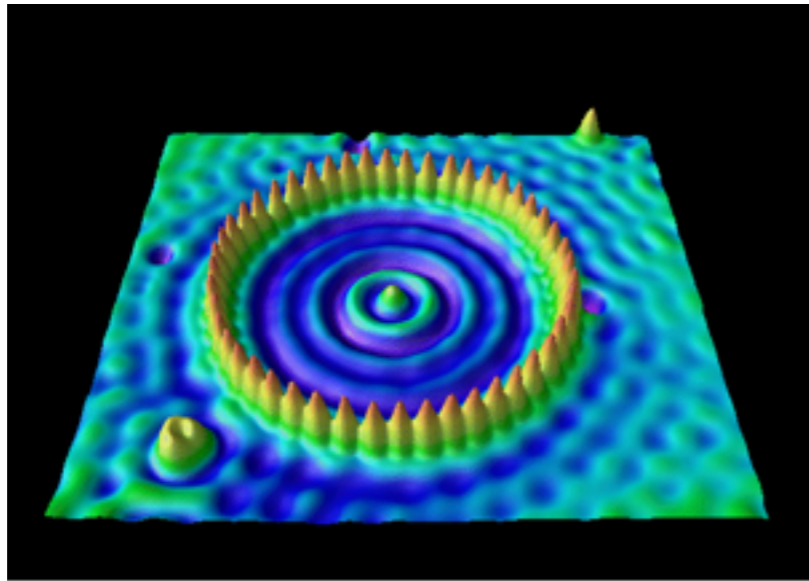


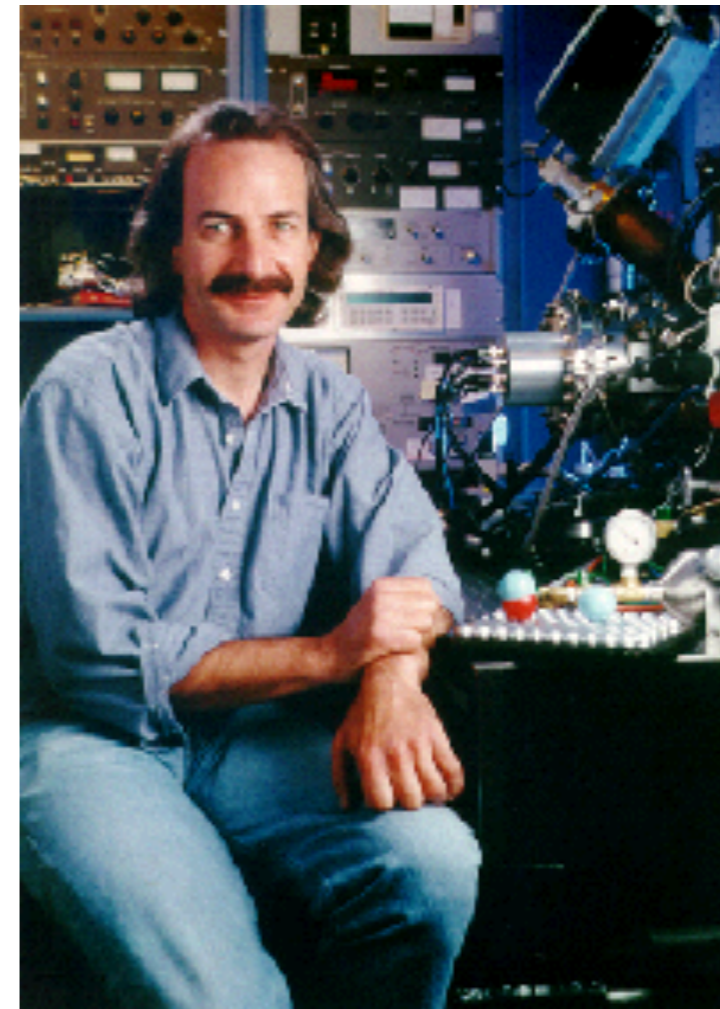
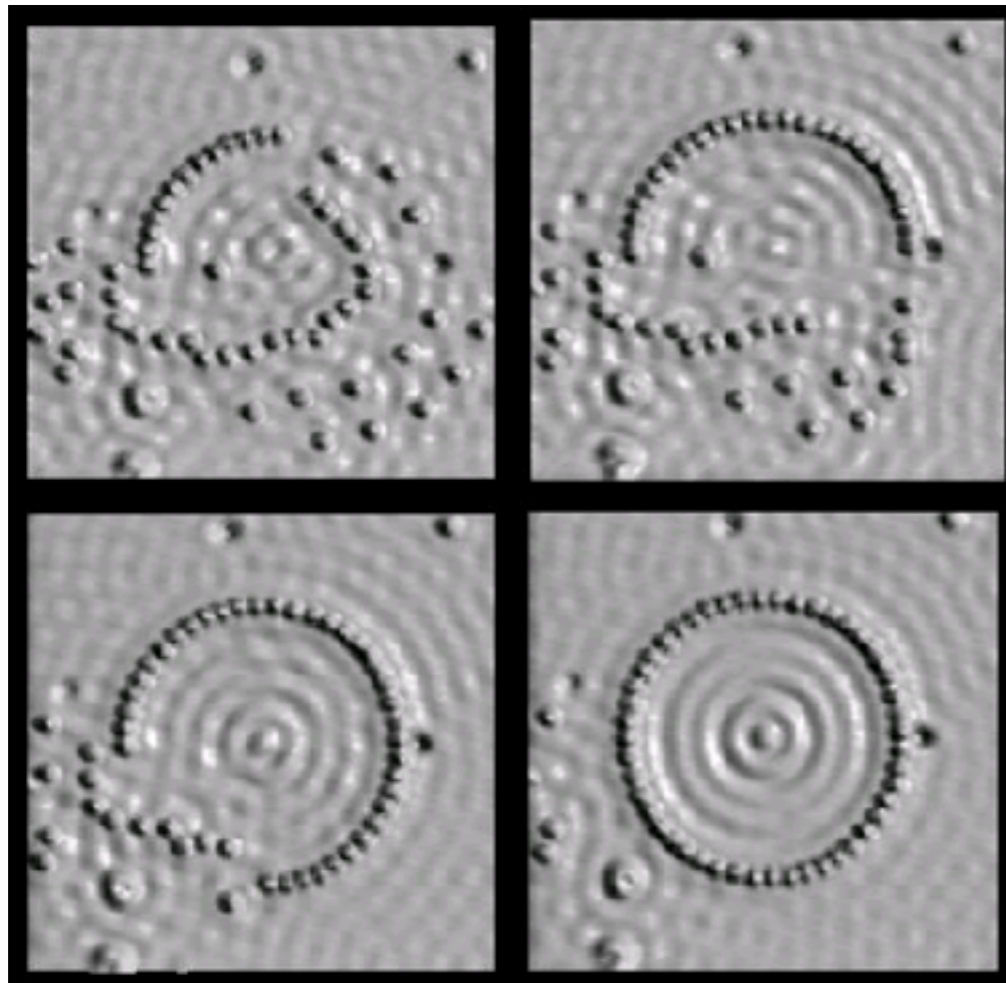
Abb. 3.18a,b. Vergleich (a) der Elektronenbeugung und (b) der Röntgenbeugung an einer dünnen Folie

Beugung an einer Kante:

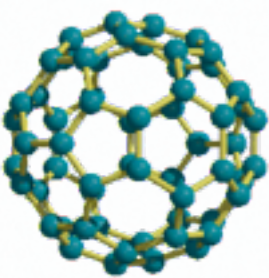




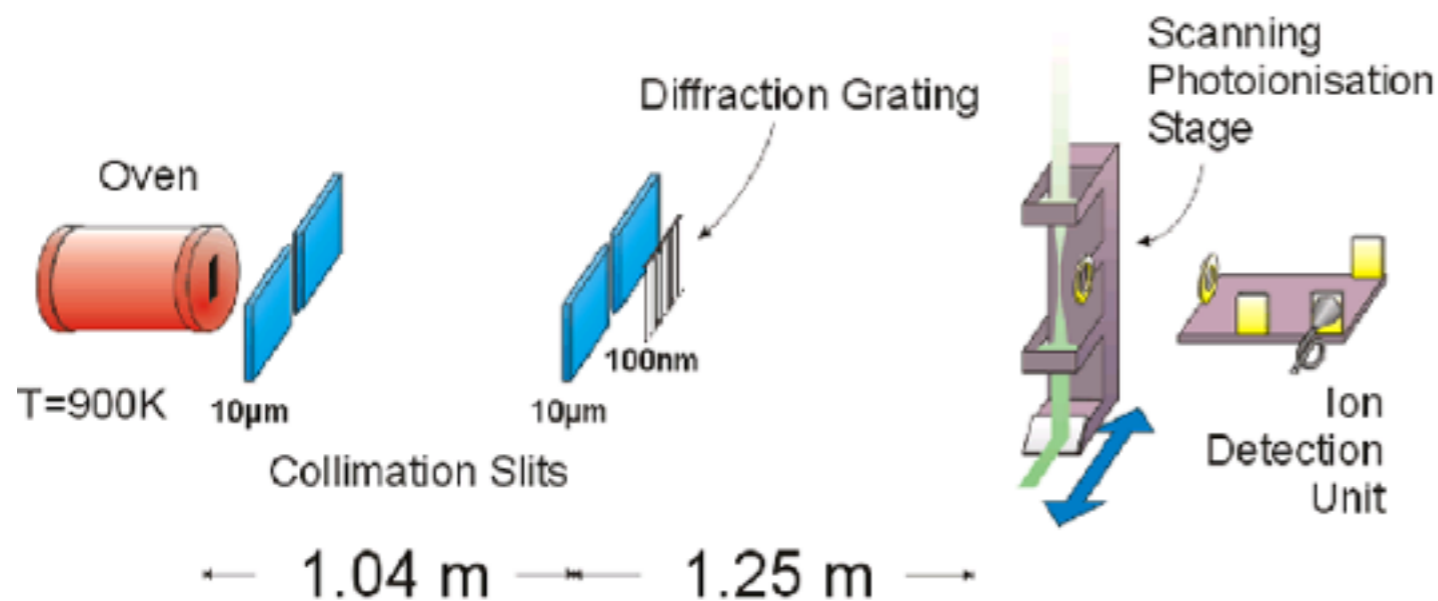
Fe auf Cu (111)



Don Eigler
IBM Almaden Research Labs
<http://www.almaden.ibm.com/vis/stm/>



Interference of C_{60} Matter Waves



Pressure $\sim 5 \cdot 10^{-7}$ mbar

C_{60} Parameter

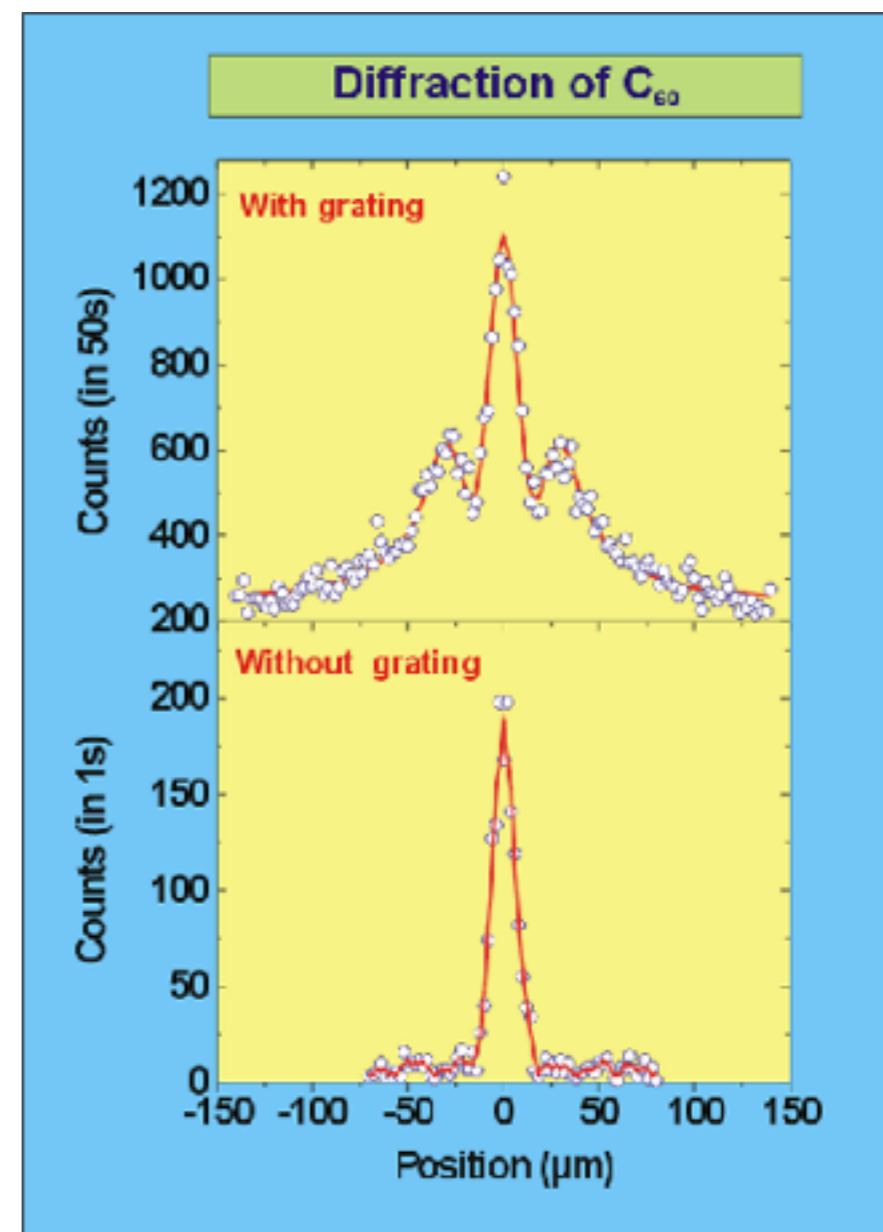
$$v = 220 \text{ m/s}$$

$$\lambda = 2,5 \text{ nm}$$

Gitter

Spaltbreite: 50 nm

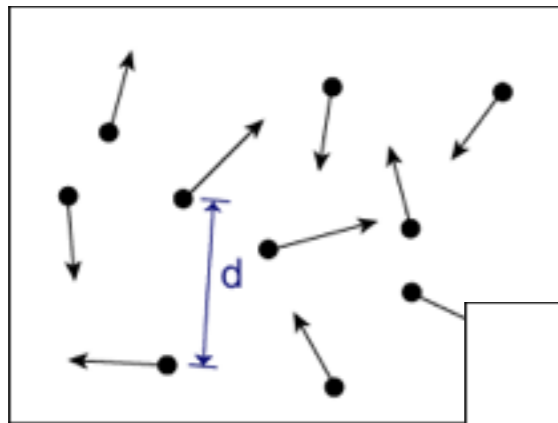
Spaltabstand: 100 nm



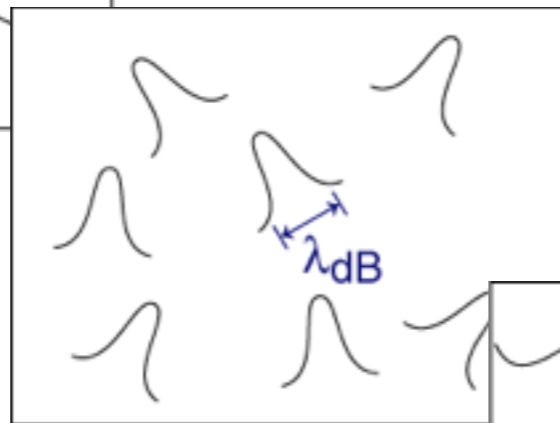
M. Arndt *et al.*

Nature **401**, ff. 680, 1999

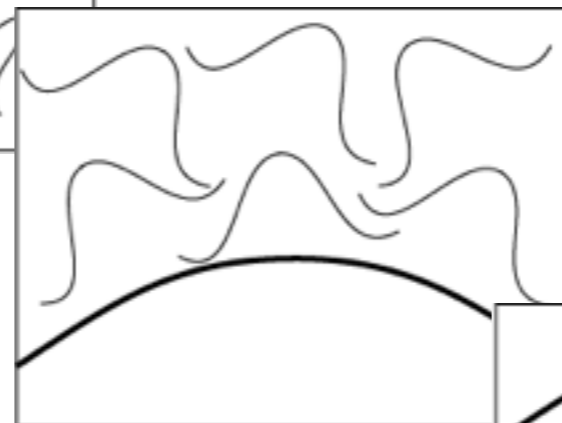
<http://www.quantum.univie.ac.at/>



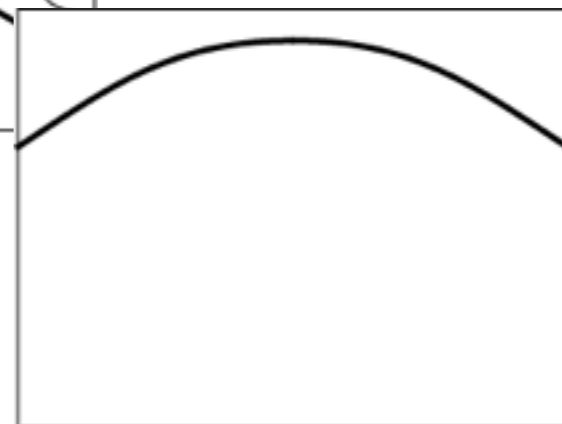
$T \gg T_c$
Classical Gas



$T > T_c$
 $\lambda_{dB} = h/mv \propto T^{-1/2}$

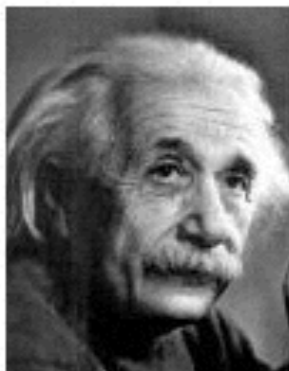


$T < T_c$
 $\lambda_{dB} \approx d$



$T = 0$
Coherent
Matter Wave

Predicted 1924...

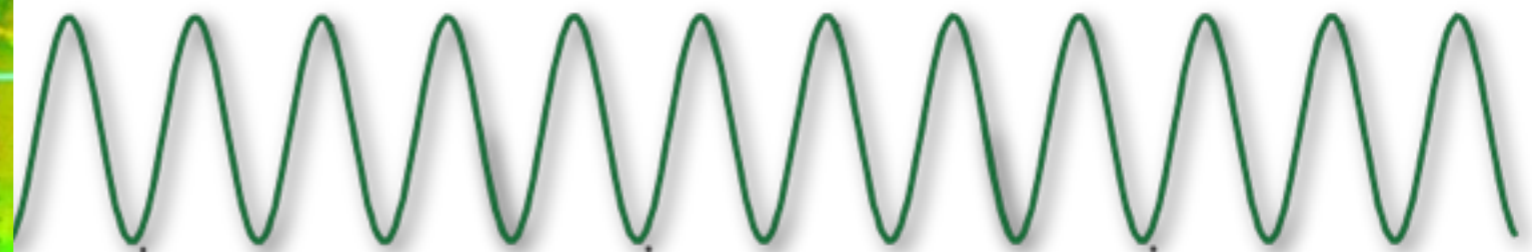
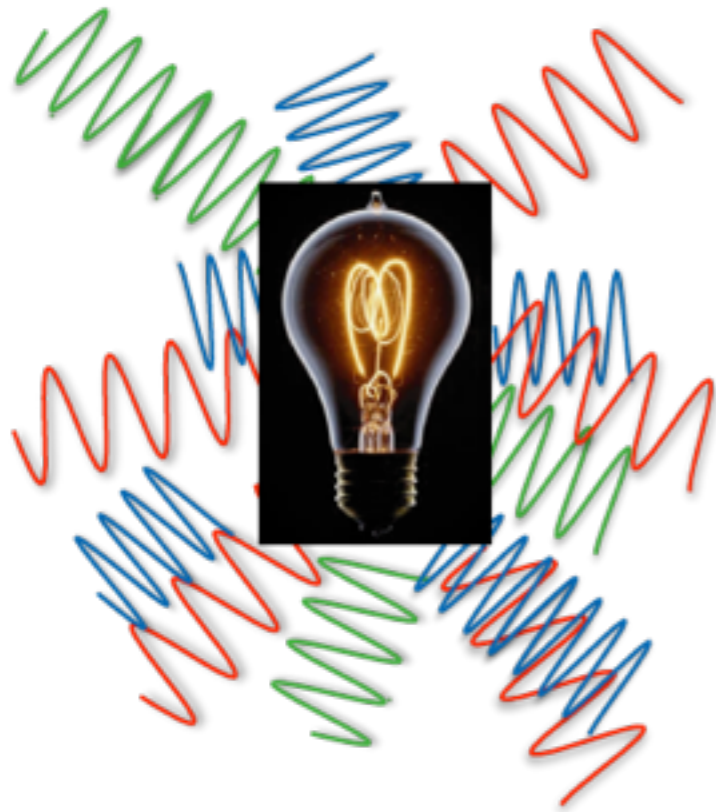


A. Einstein



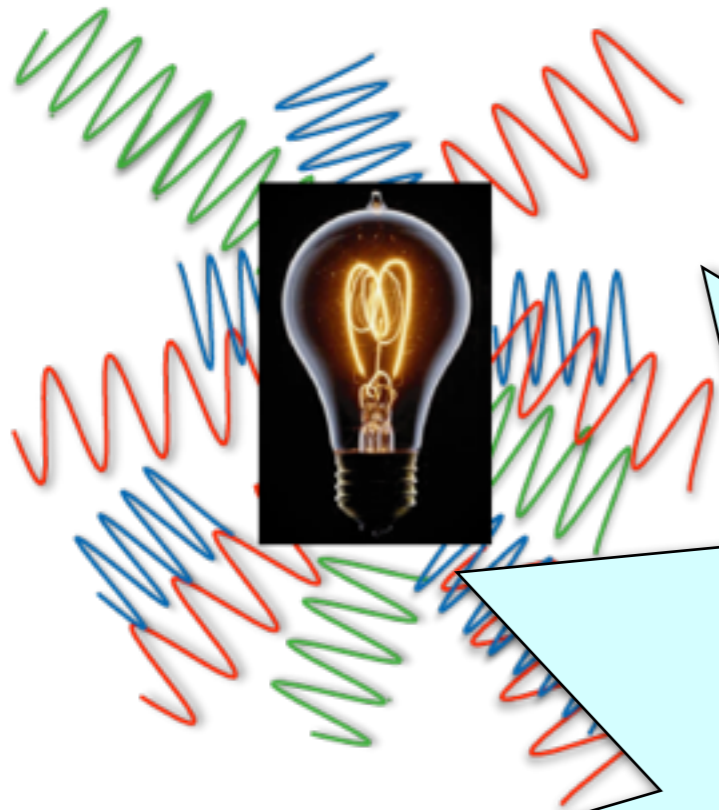
S. Bose



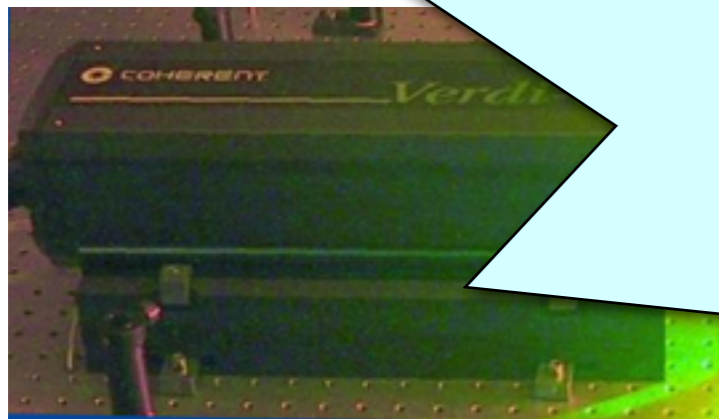


Laser emits one one continuous waveltrain with a perfectly defined frequency!

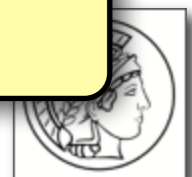




***BEC is for matter
what the laser is
for light!***



Laser emits one continuous wavetrain with a perfectly defined frequency!



Conditions for BEC:

$$n \cdot \lambda^3 \approx 1$$

z.B. Water

For a typical density of water $n_{\text{H}_2\text{O}}$ we obtain $T_c = 1\text{K}$

Problem: Water is a block of ICE @ 1K

Solution: Density has to be lowered by several orders of magnitude to prolong timescale for solid formation!



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Even lower temperatures are needed!



de Broglie Wavelengths

Thermal deBroglie wavelengths

$$\lambda = \frac{h}{\sqrt{2\pi m k_B T}}$$

273 K (0°C, 32°F)
Water freezes

77K (-197°C, -323°F)
Air liquifies

4K (-269°C, -452 °F)
He liquifies

T (K)

10000
100
1
10⁻¹
10⁻⁴
10⁻⁶
10⁻⁸

de Broglie Wavelengths of a typical atom

0.01 nm
0.1 nm
1 nm
0.01 μm
0.1 μm
1 μm
10 μm

These are temperatures we need to reach to create macroscopic matter waves !

Matter changes at low temperatures!

- **Matter can undergo a *Phase Transition* when lowering temperatures!**
 - **Gas** ⇒ **Liquid**
 - **Liquid** ⇒ **Solid**
 - **Normal Conductor** ⇒ **Superconductor**
 - **Normal Liquid** ⇒ **Superfluid**
 - **Classical Gas** ⇒ **Quantum Gas (BEC)**



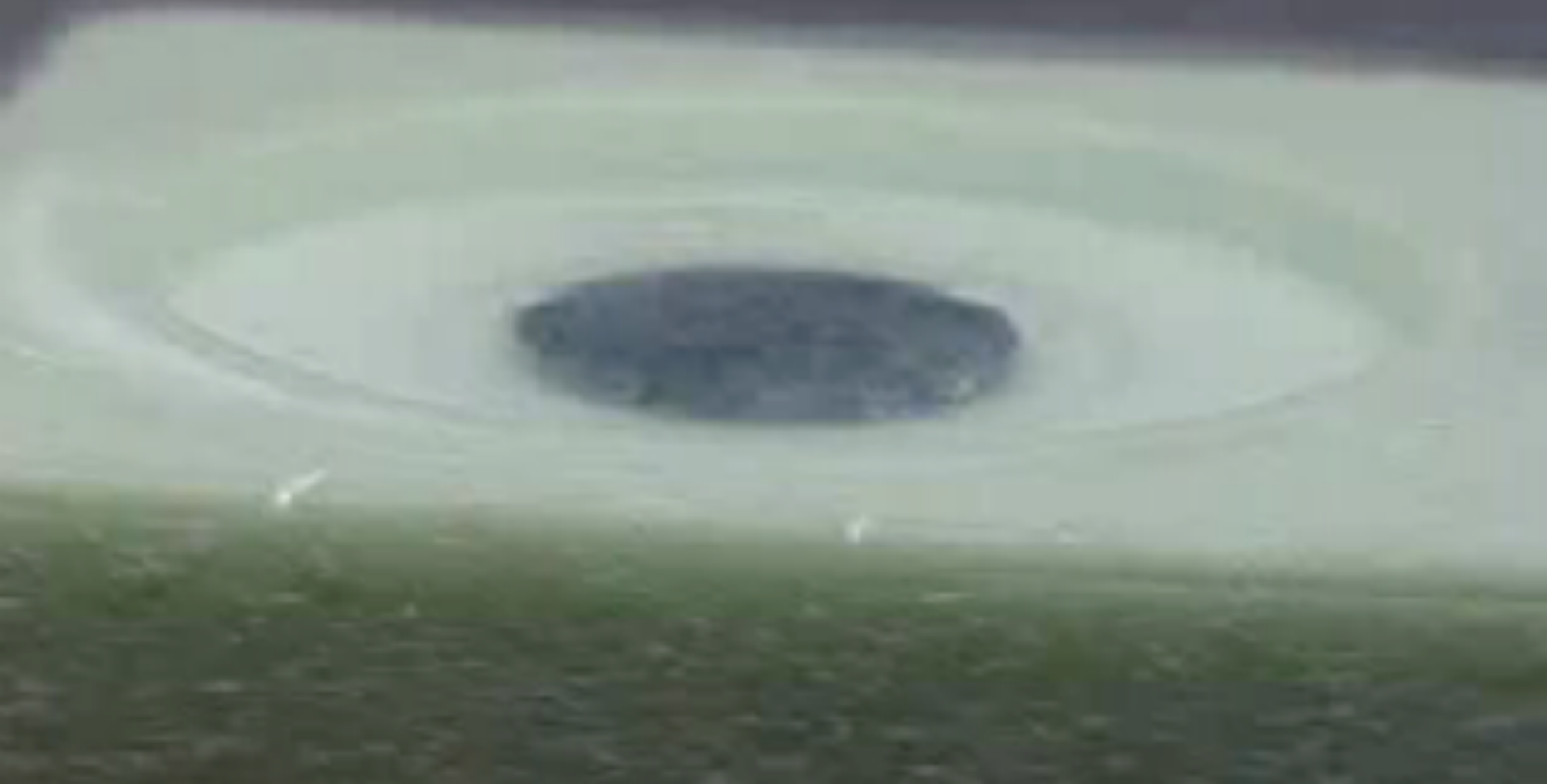
Superconductivity at Low Temperatures



At very low temperatures some materials can lose all resistivity!

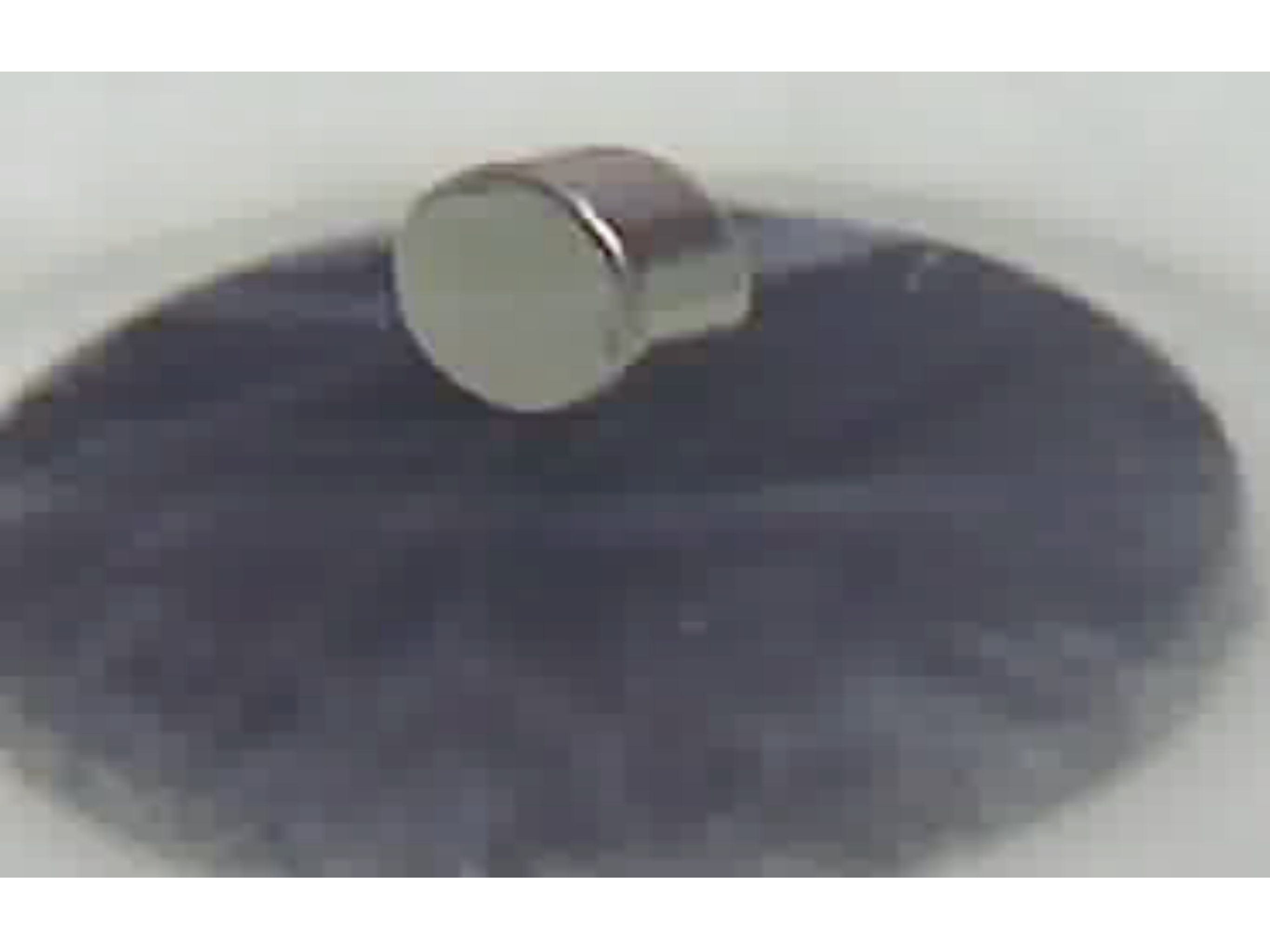
They become superconductors!

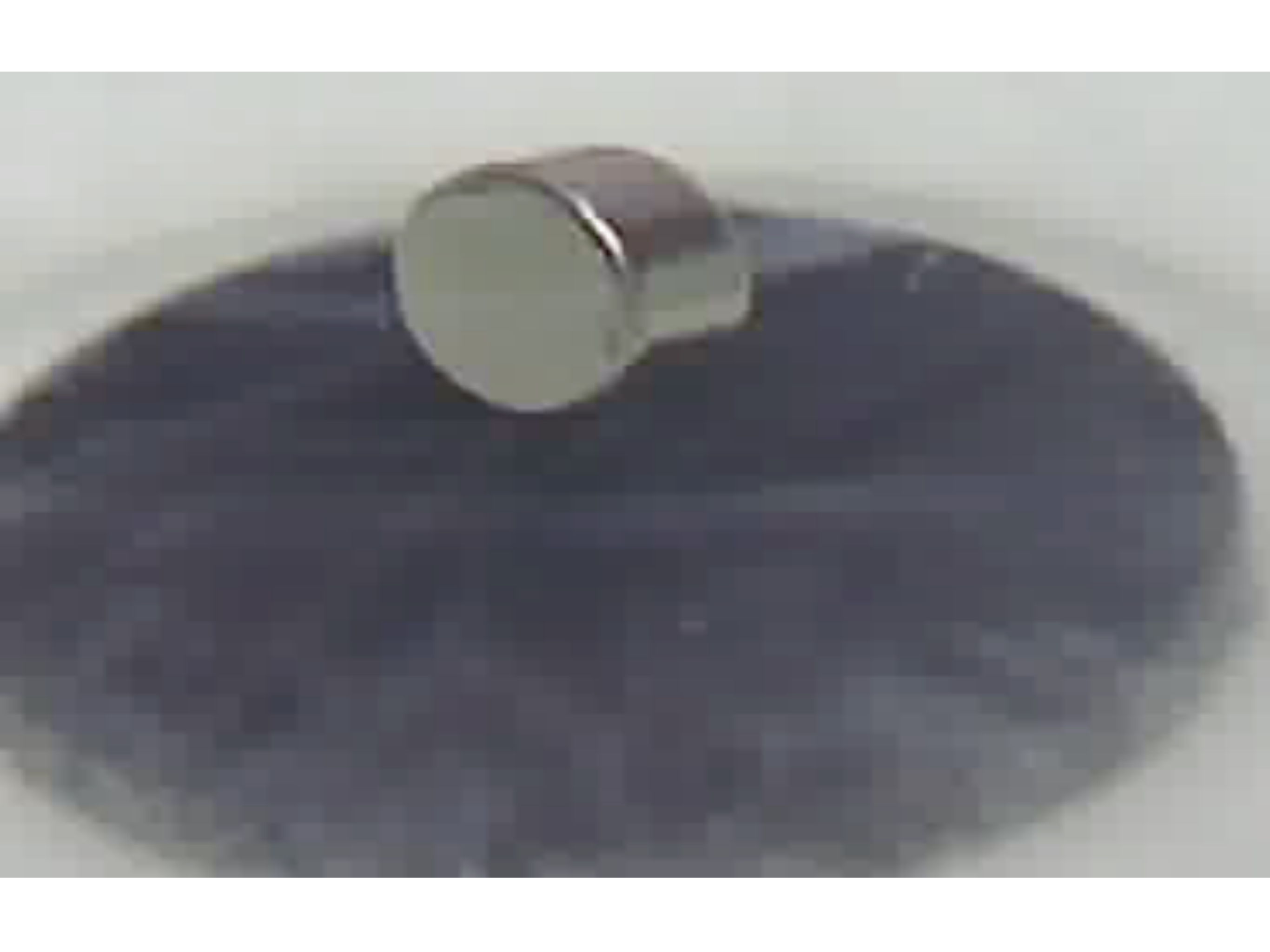
Meissner Effect



Meissner Effect







Radiation Pressure

Komet Hale-Bopp

A special way to cool!

Laser Cooling



T.W. Hänsch and A.L. Schawlow, *Opt. Comm.* 13, 68 (1975)

Laser Cooling



Nobel in Physics 1997



Steve Chu



Claude Cohen-Tannoudji



Bill Phillips



Maximum Acceleration

$$a_{\max} = \frac{\hbar k}{m} \times \frac{\Gamma}{2}$$

e.g. for ^{87}Rb

$$a_{\max} = 100000 \text{ m/s}^2$$

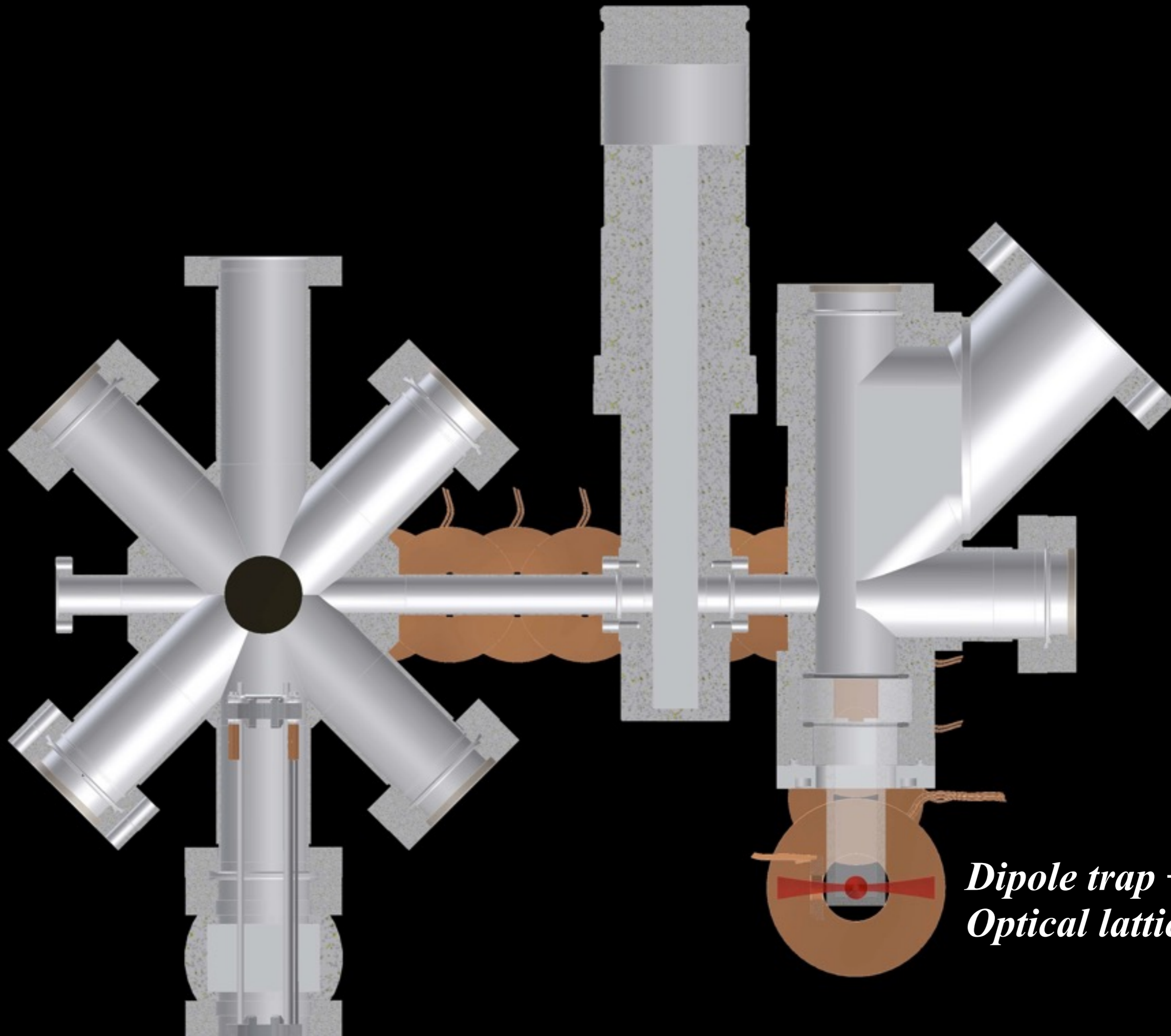
Minimum Temperature

$$T_{\min} \approx 10 \mu\text{K}$$



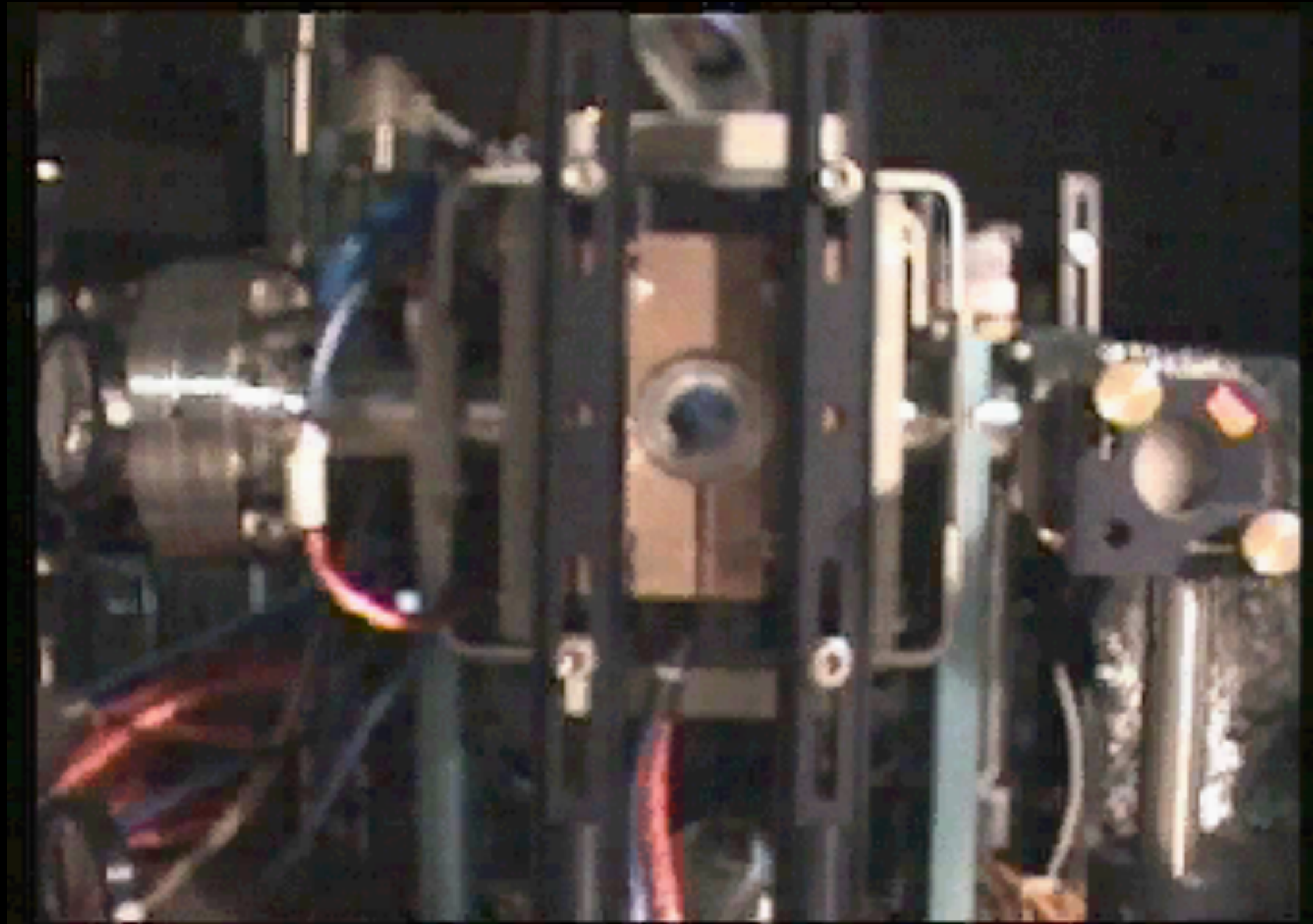
10000 g !



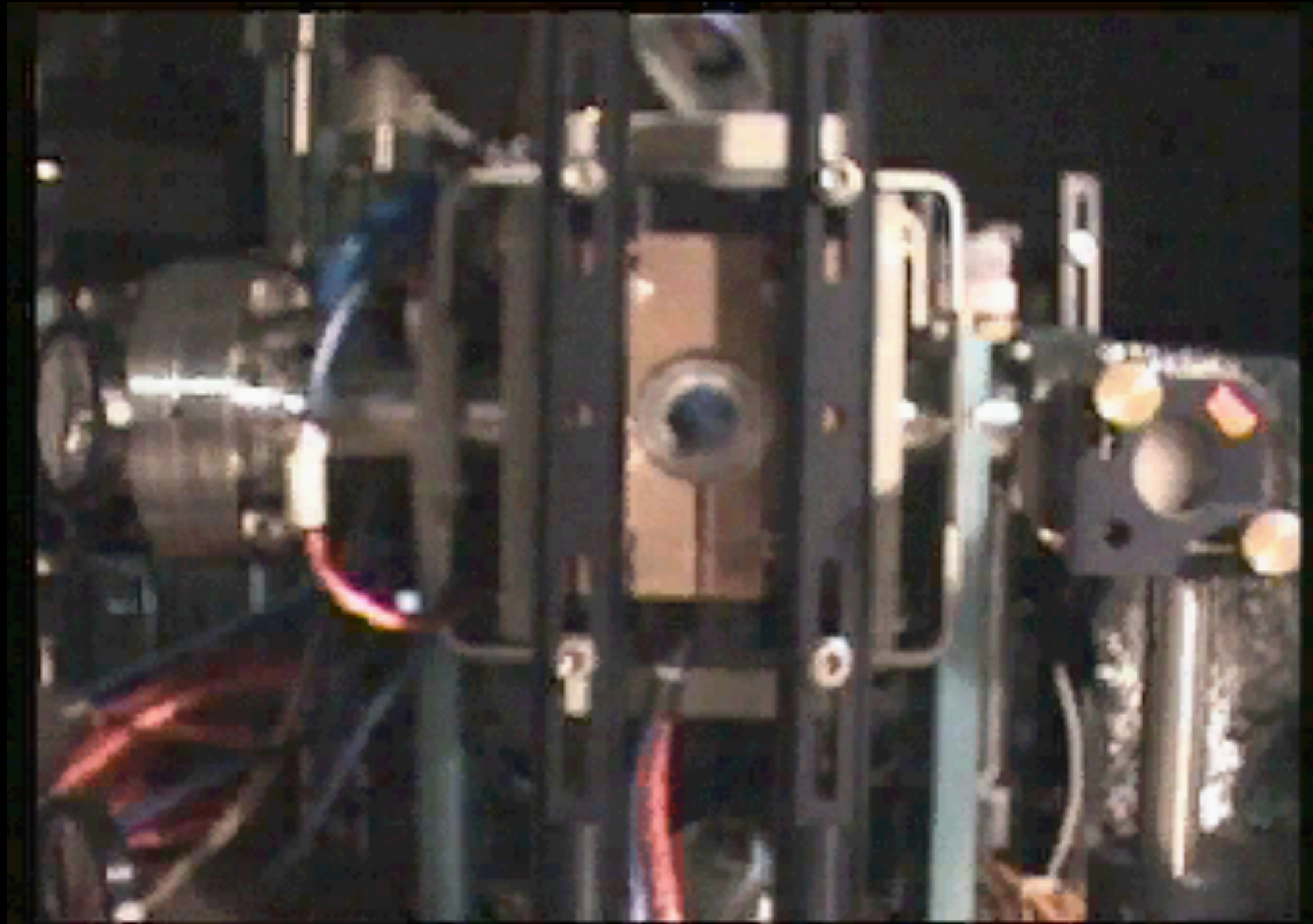


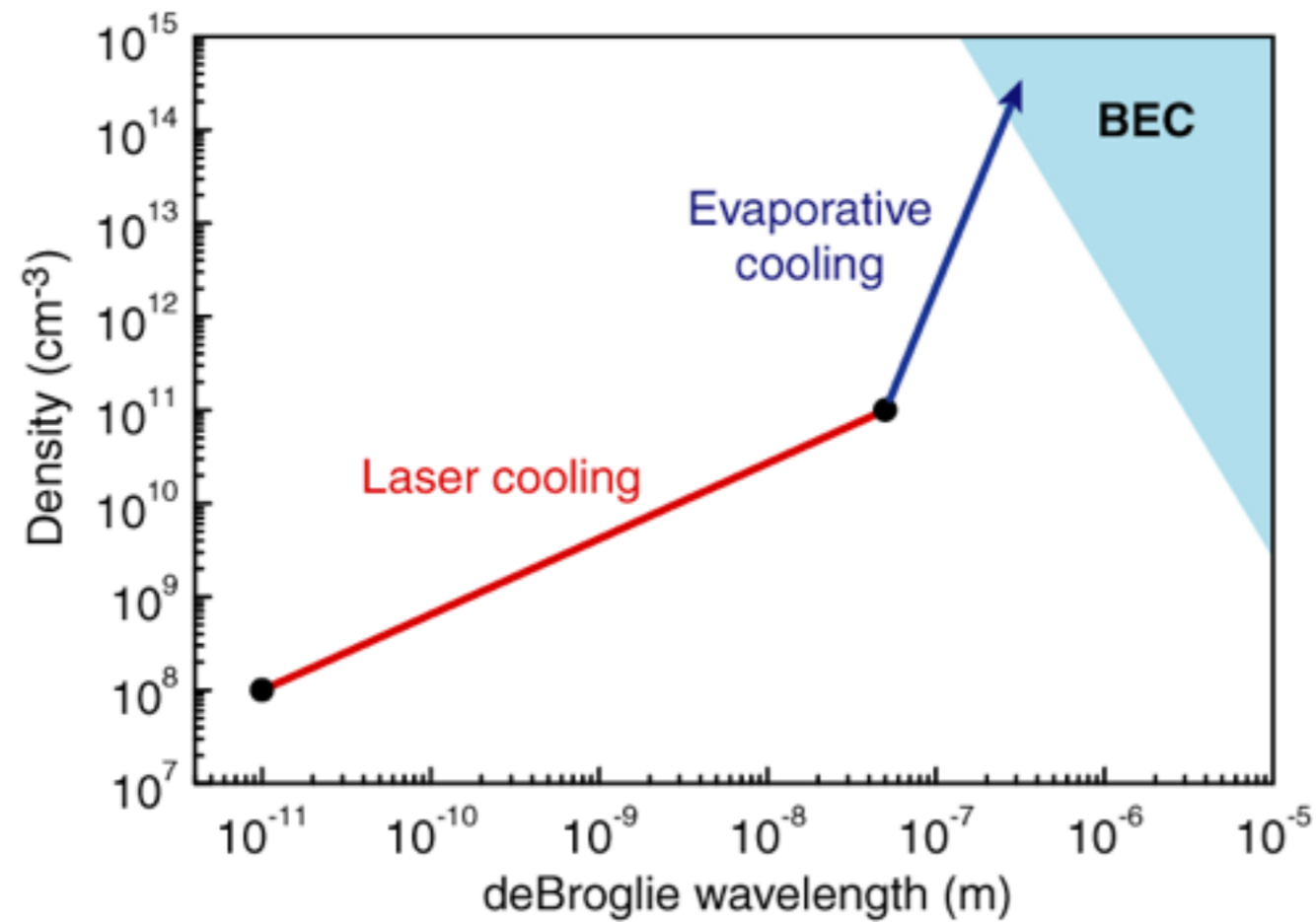
*Dipole trap +
Optical lattices*

Laser Cooling at Work

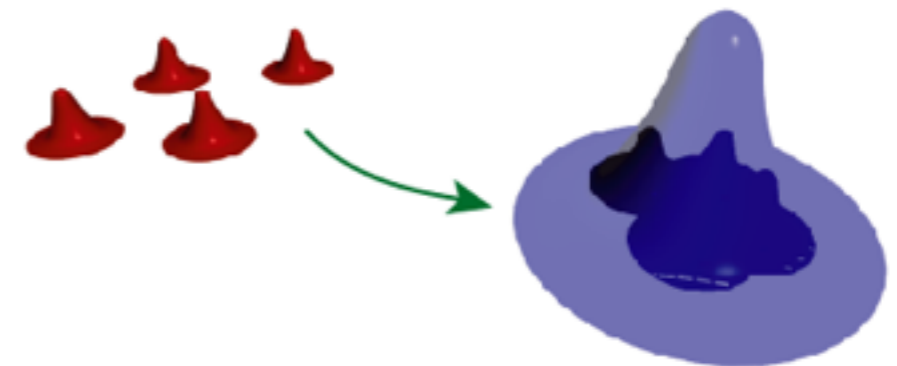


Laser Cooling at Work





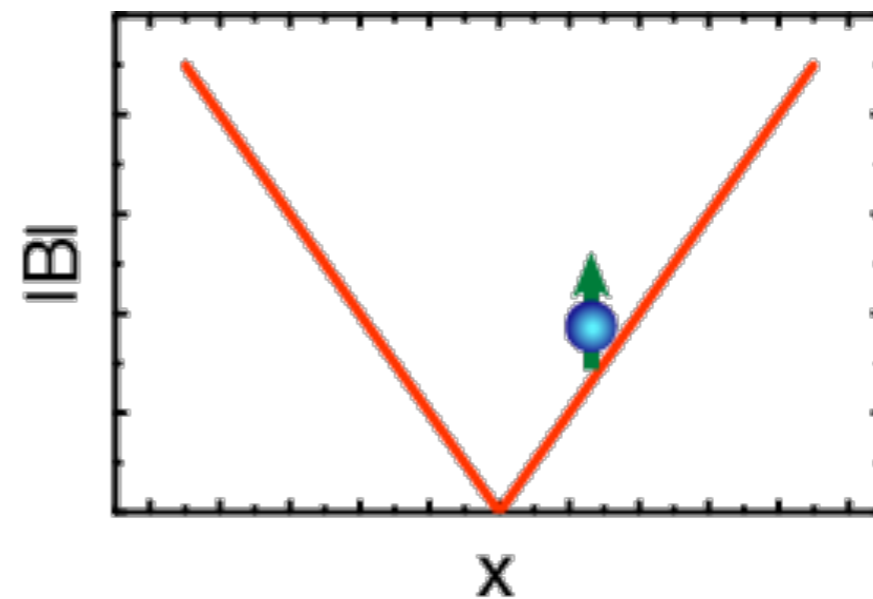
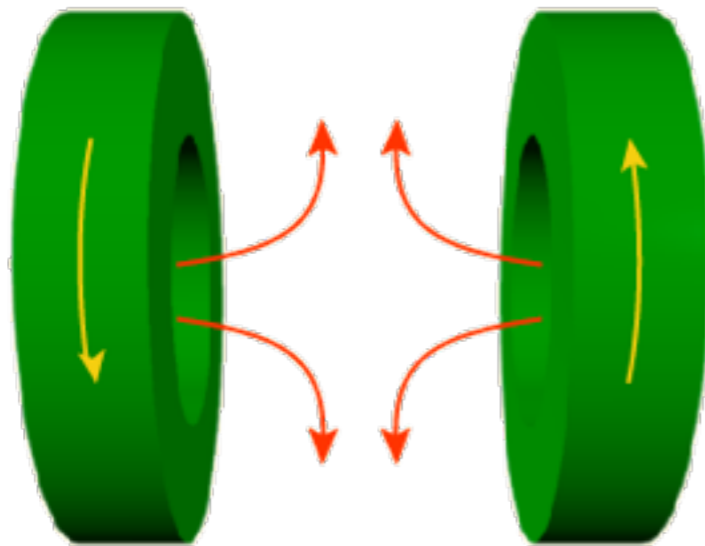
$$n \cdot \lambda^3 \approx 1$$

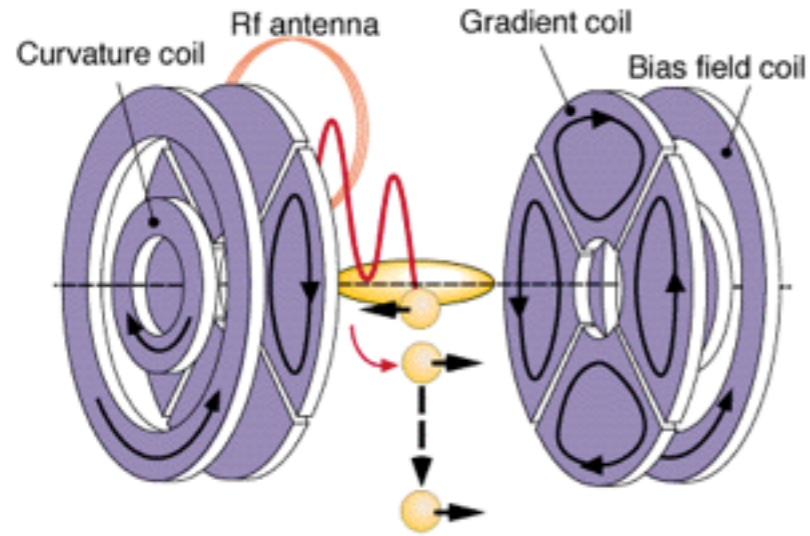




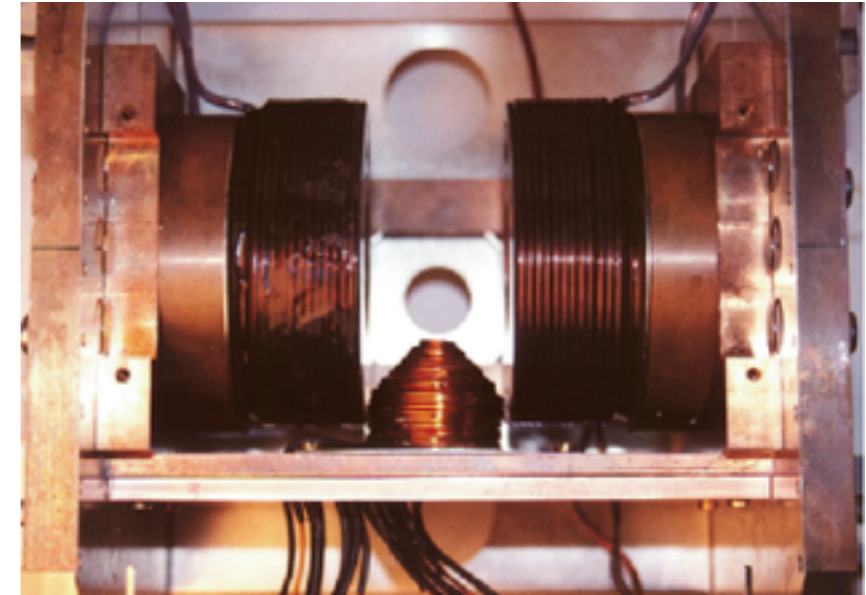
Energy of an atom
in an external magnetic field $E = -\vec{\mu} \cdot \vec{B}$

Force on an atom in an
inhomogeneous magnetic field $\vec{F} = -\mu \cdot \nabla B$



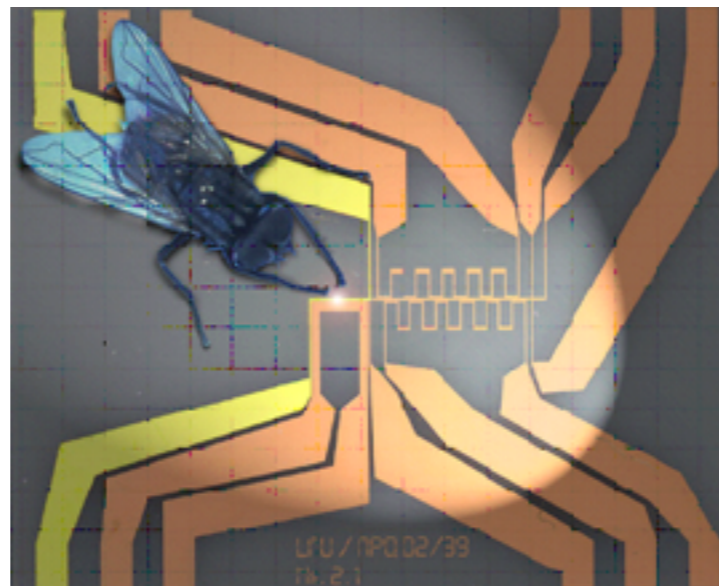


MIT, March '96 [M.-O. Mewes et al., PRL 77, 416 (1996)]



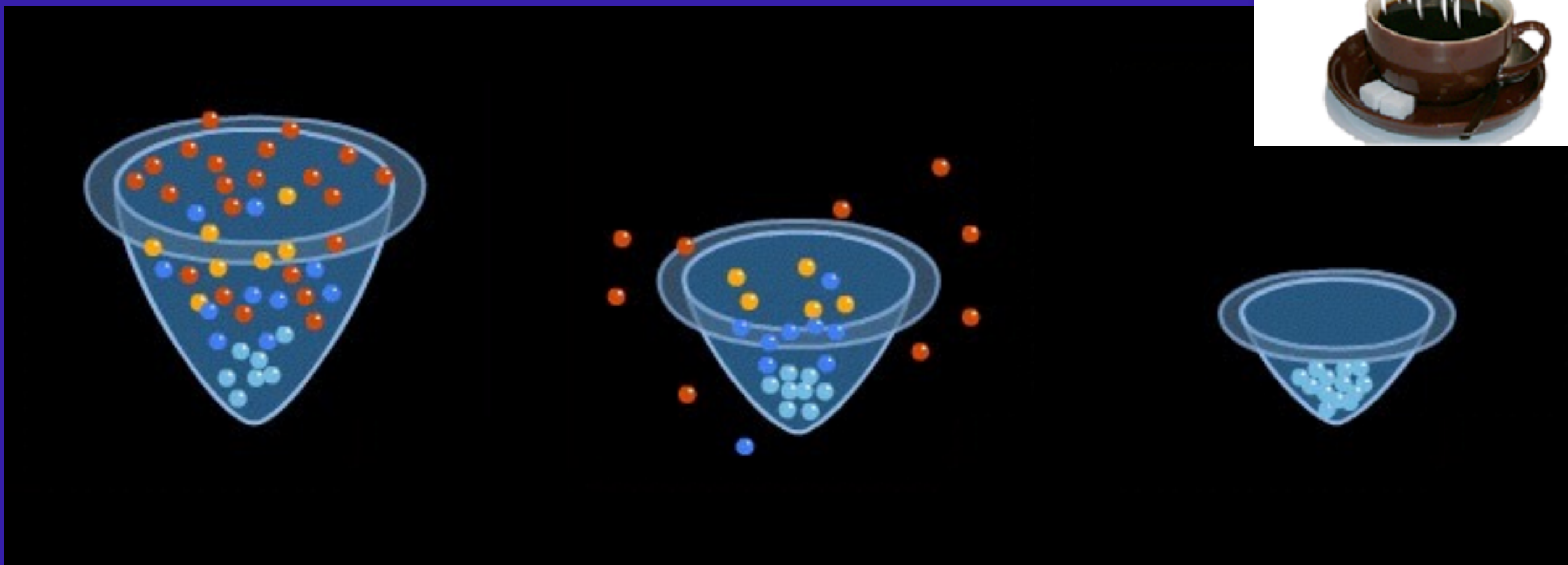
Cloverleaf Trap

QUIC-Trap



Miniaturized Magnetic Traps

Evaporative Cooling



Tom Greytak



Daniel Kleppner

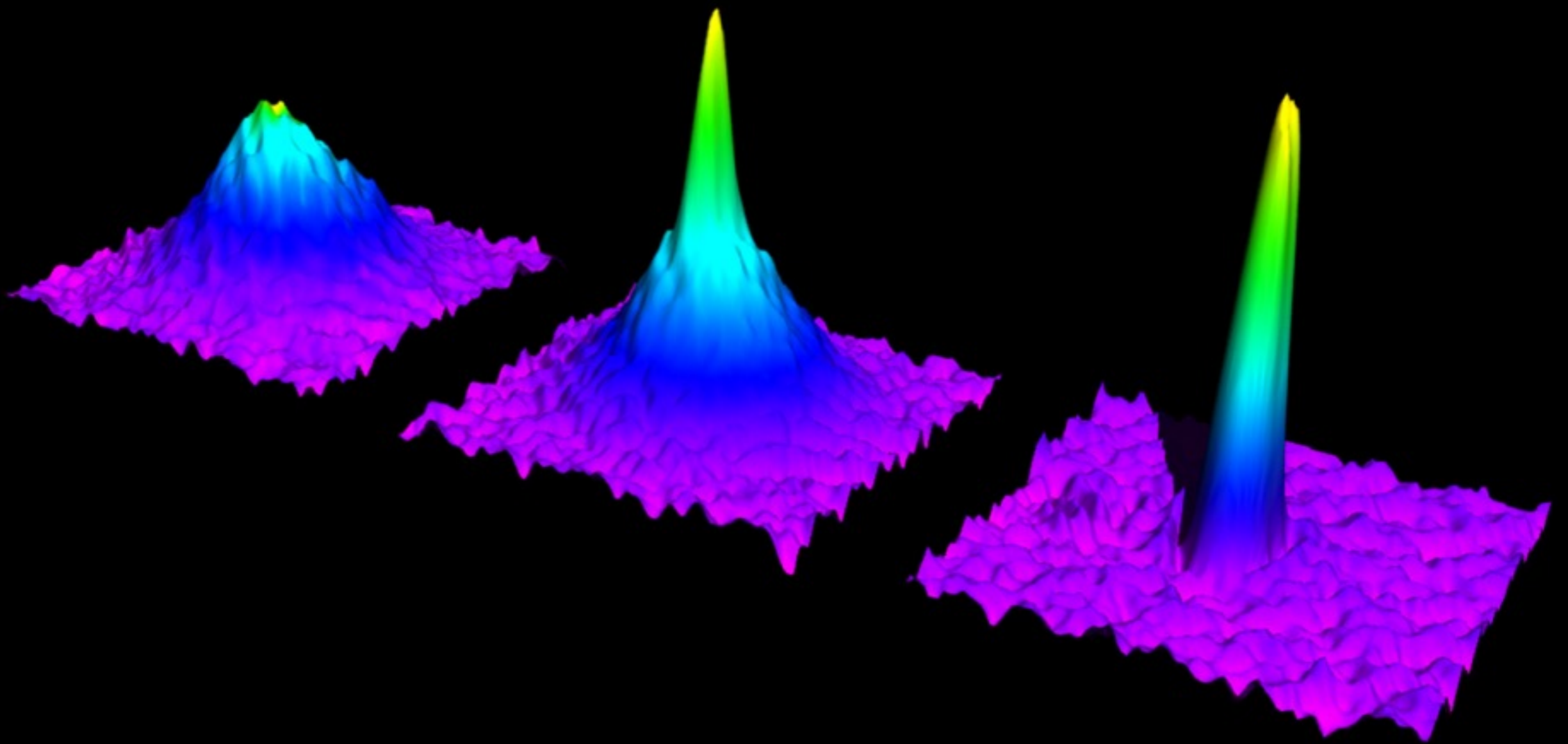
Go To Evap Applet...

Time-of-Flight Imaging



Time-of-Flight Imaging

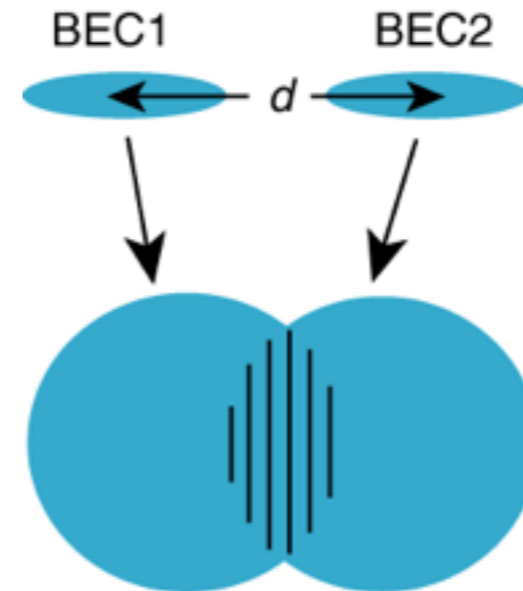




Interference of Two Bose-Einstein Condensates

***Trapped
BEC's***

***BEC's after
expansion time t***

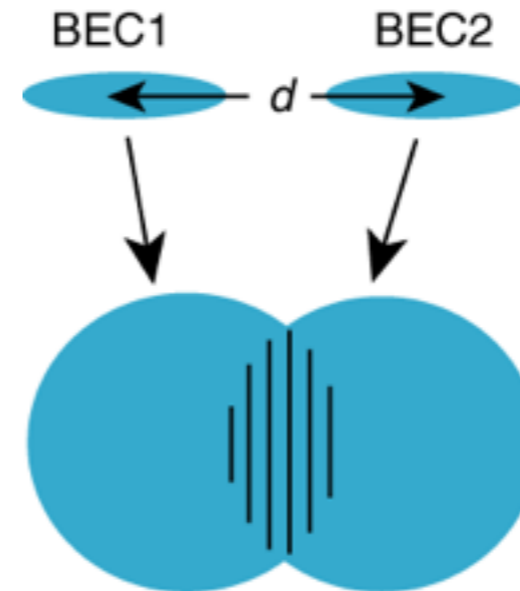


$$\lambda = \frac{h}{m\Delta v} = \frac{ht}{md}$$

Interference of Two Bose-Einstein Condensates

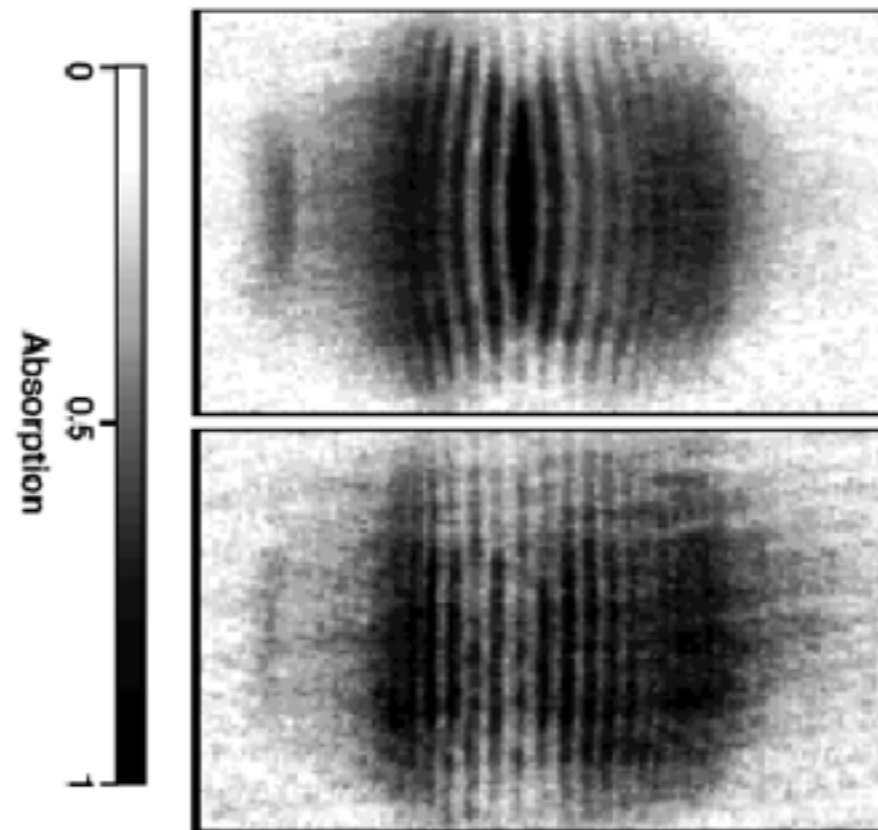
**Trapped
BEC's**

**BEC's after
expansion time t**

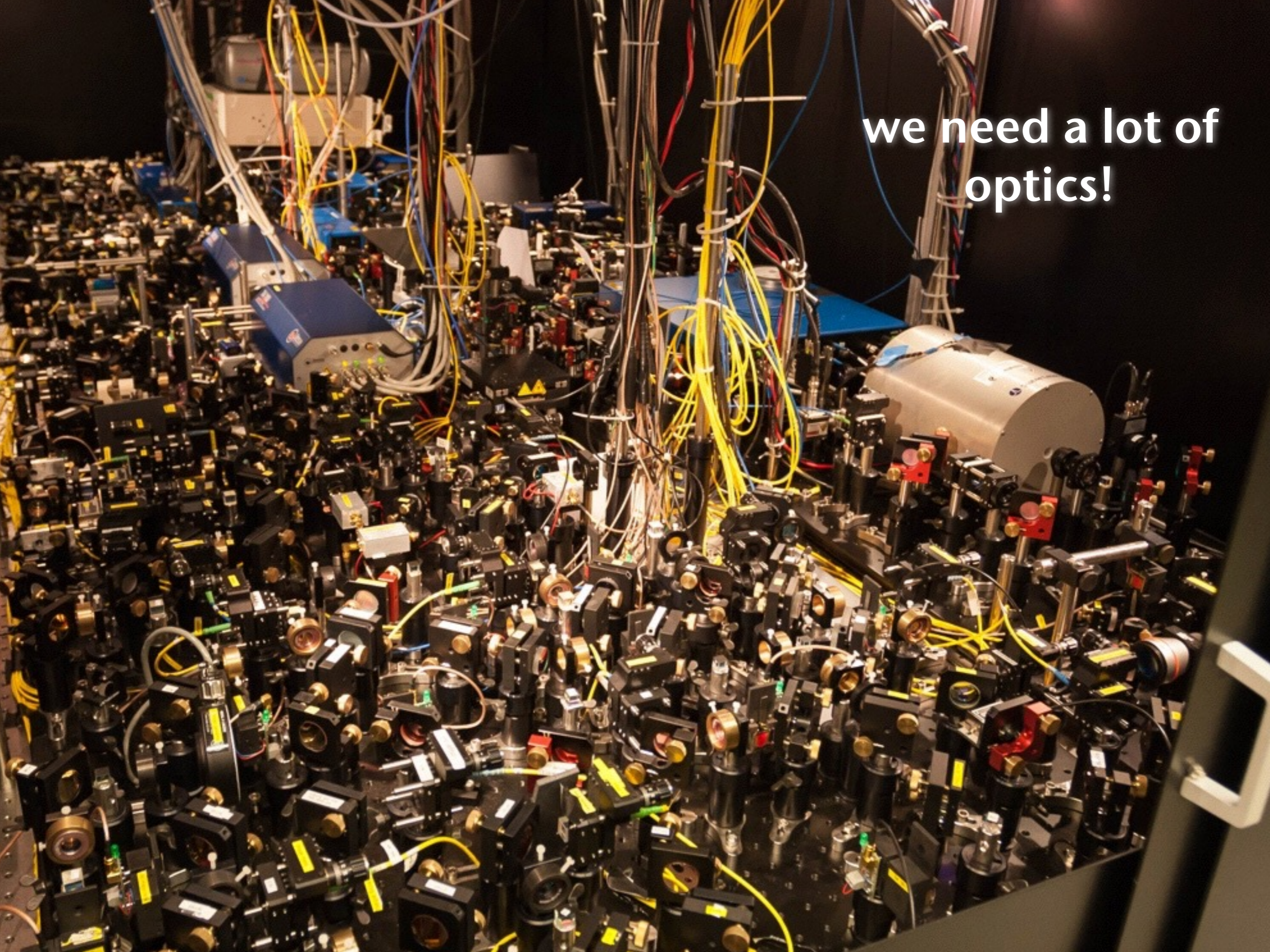


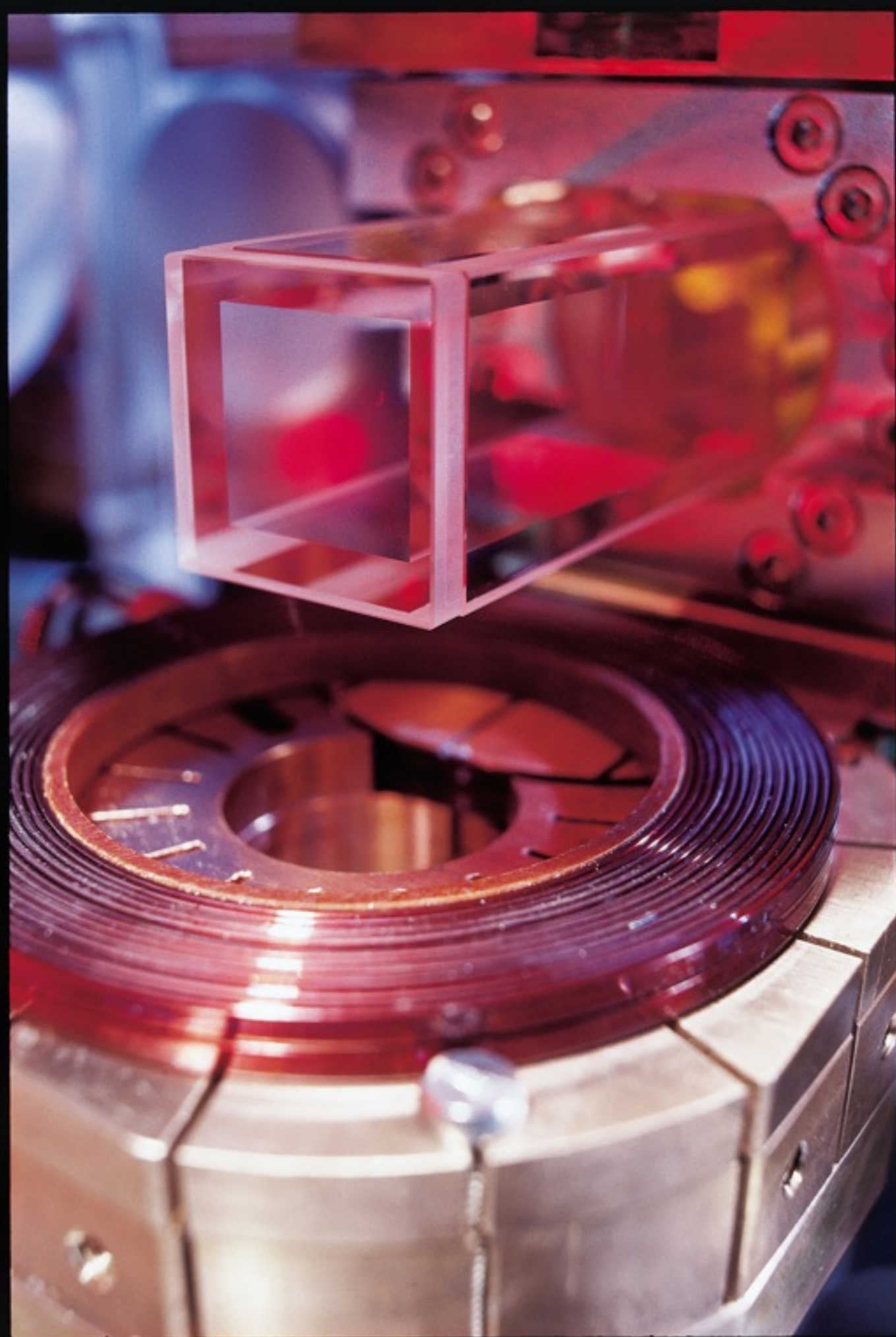
$$\lambda = \frac{h}{m\Delta v} = \frac{ht}{md}$$

M. R. Andrews *et. al.*
Science 275, ff. 637, 1997



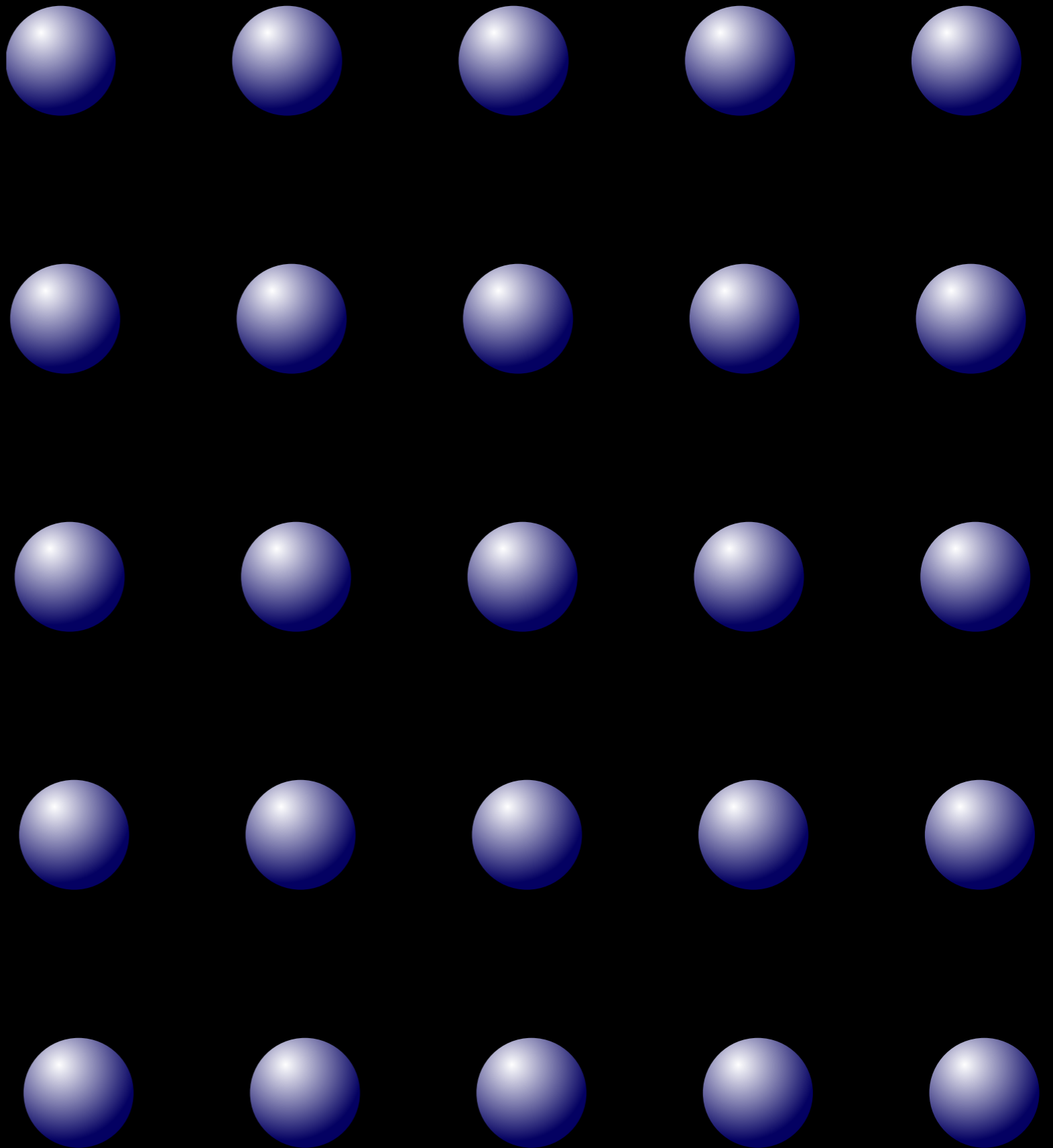
we need a lot of
optics!

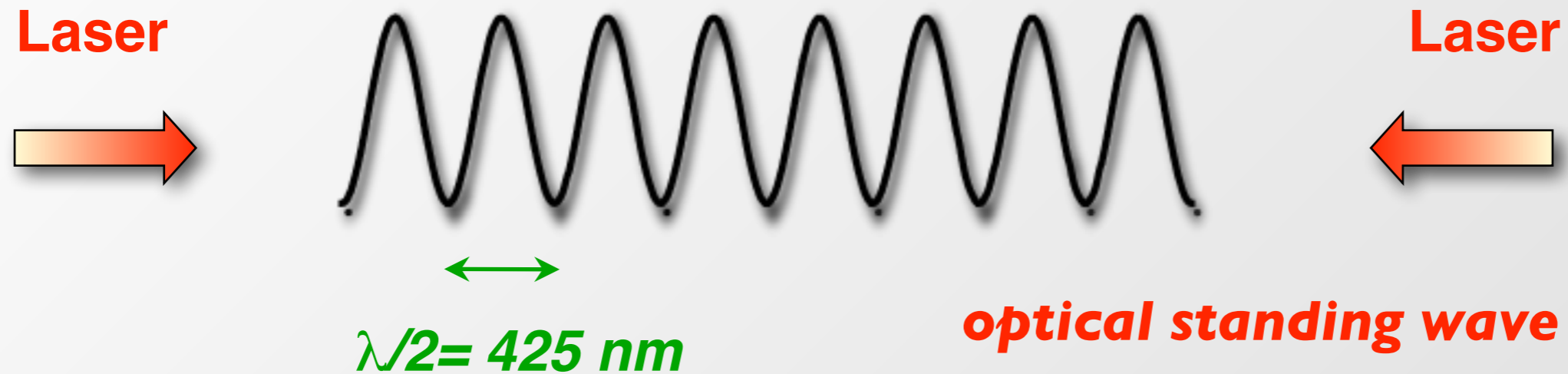






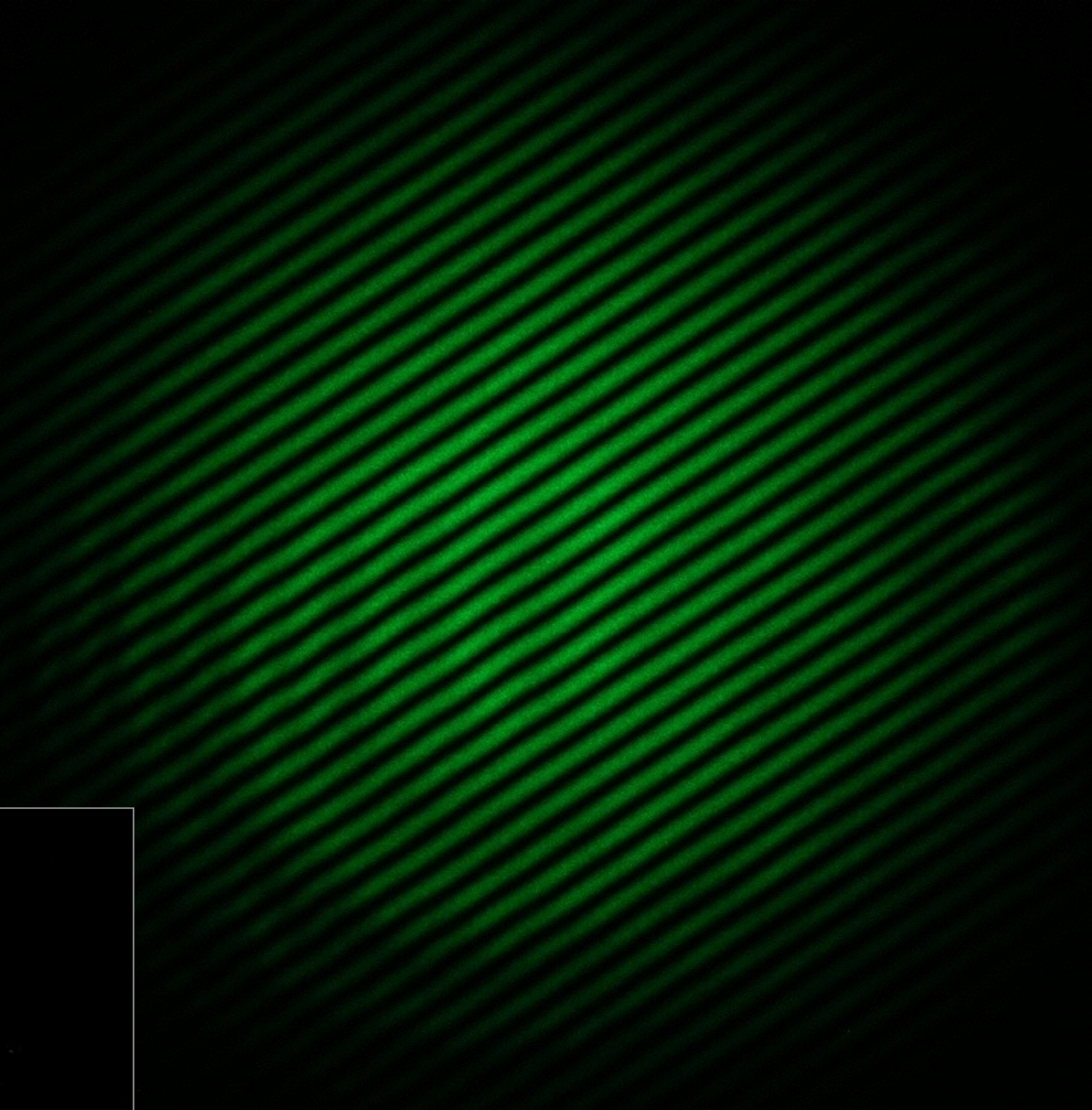
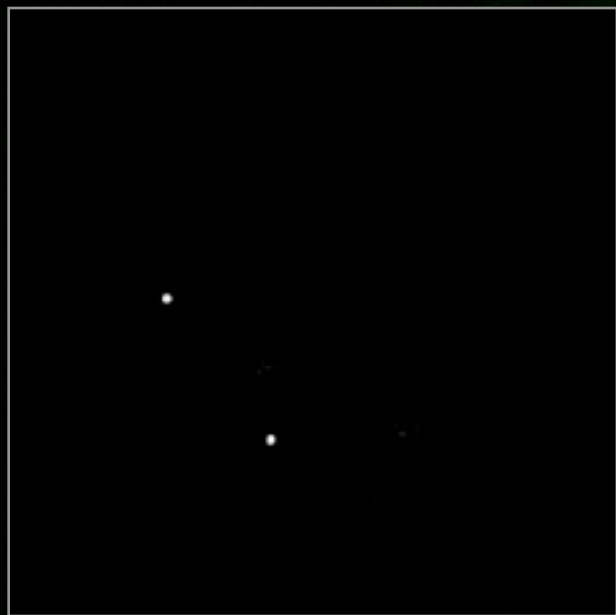
x10000



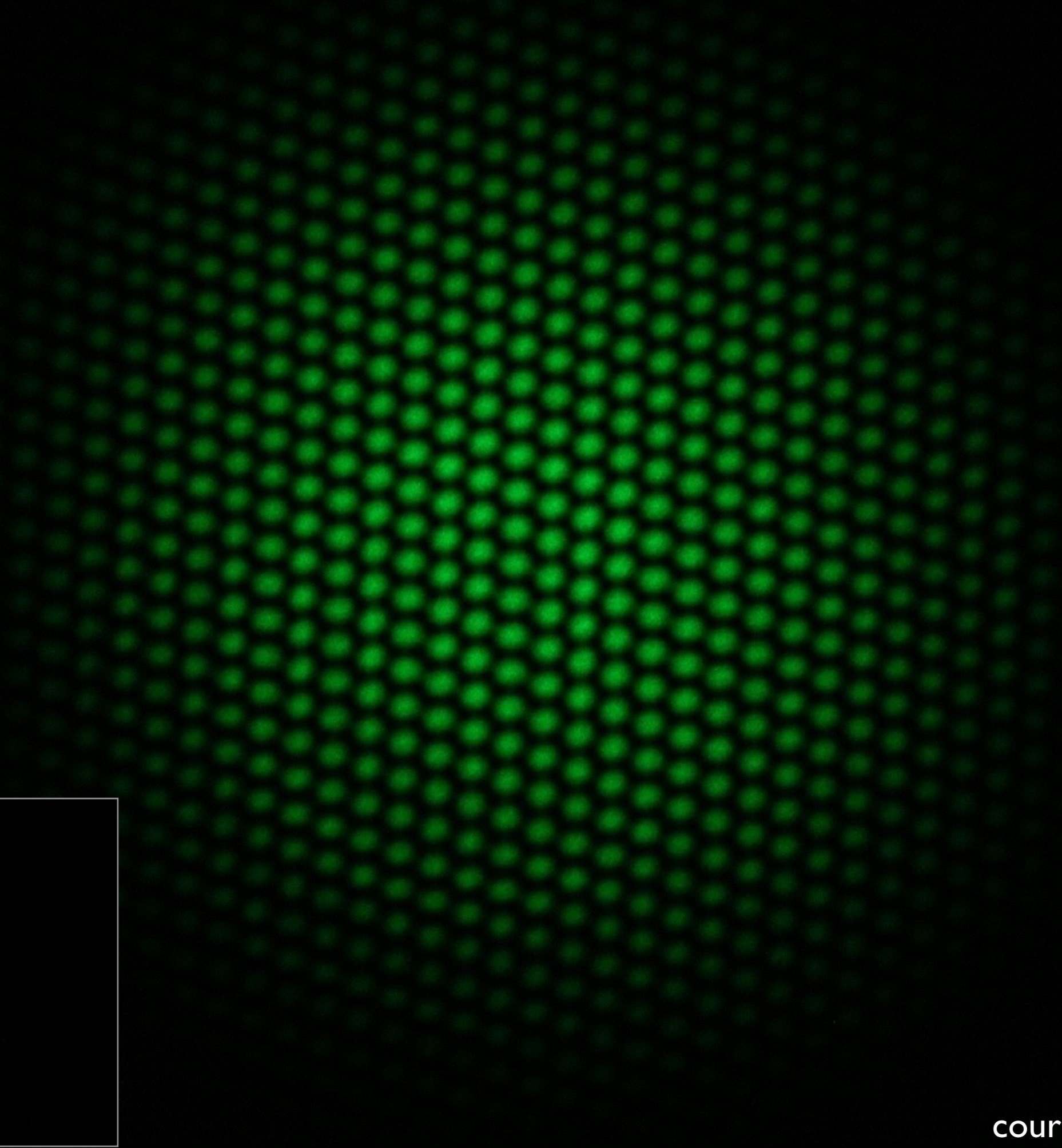
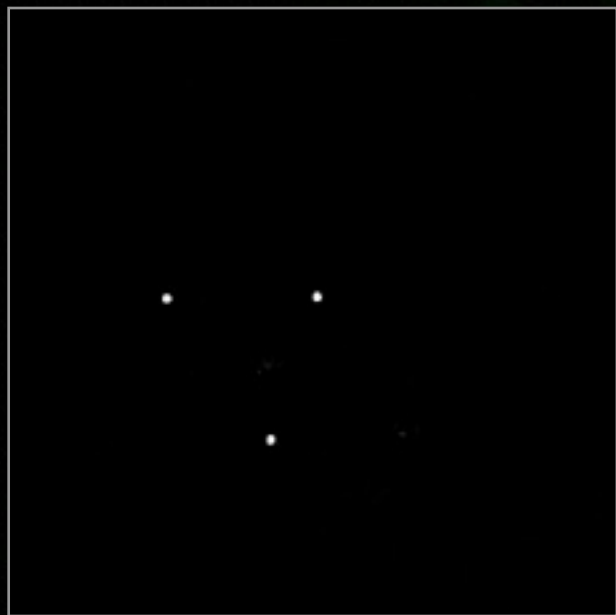


*Perfect model systems for a
fundamental understanding of
quantum many-body systems*

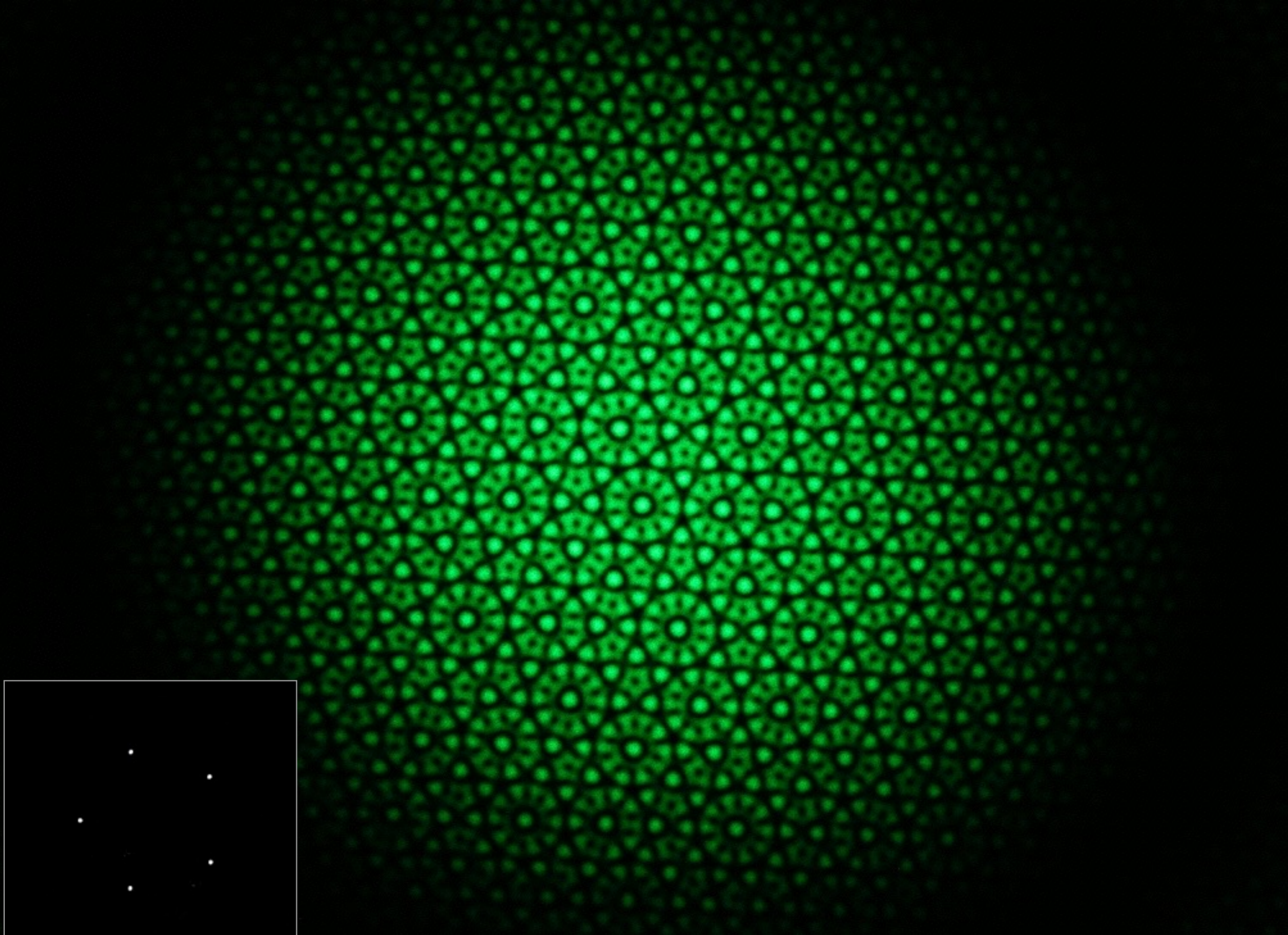
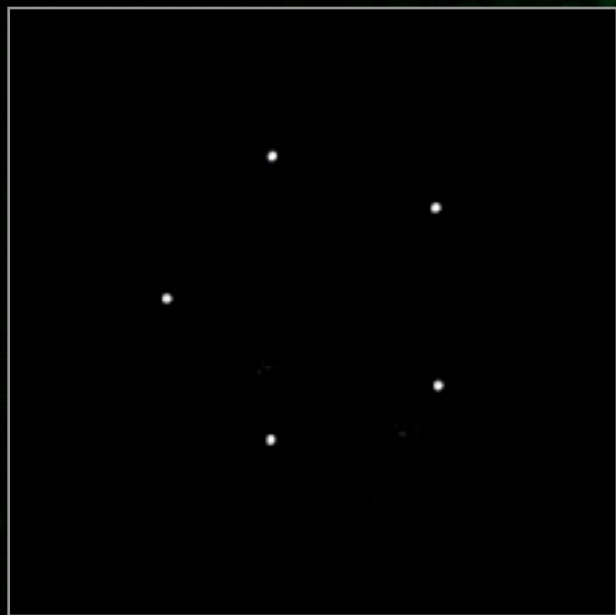


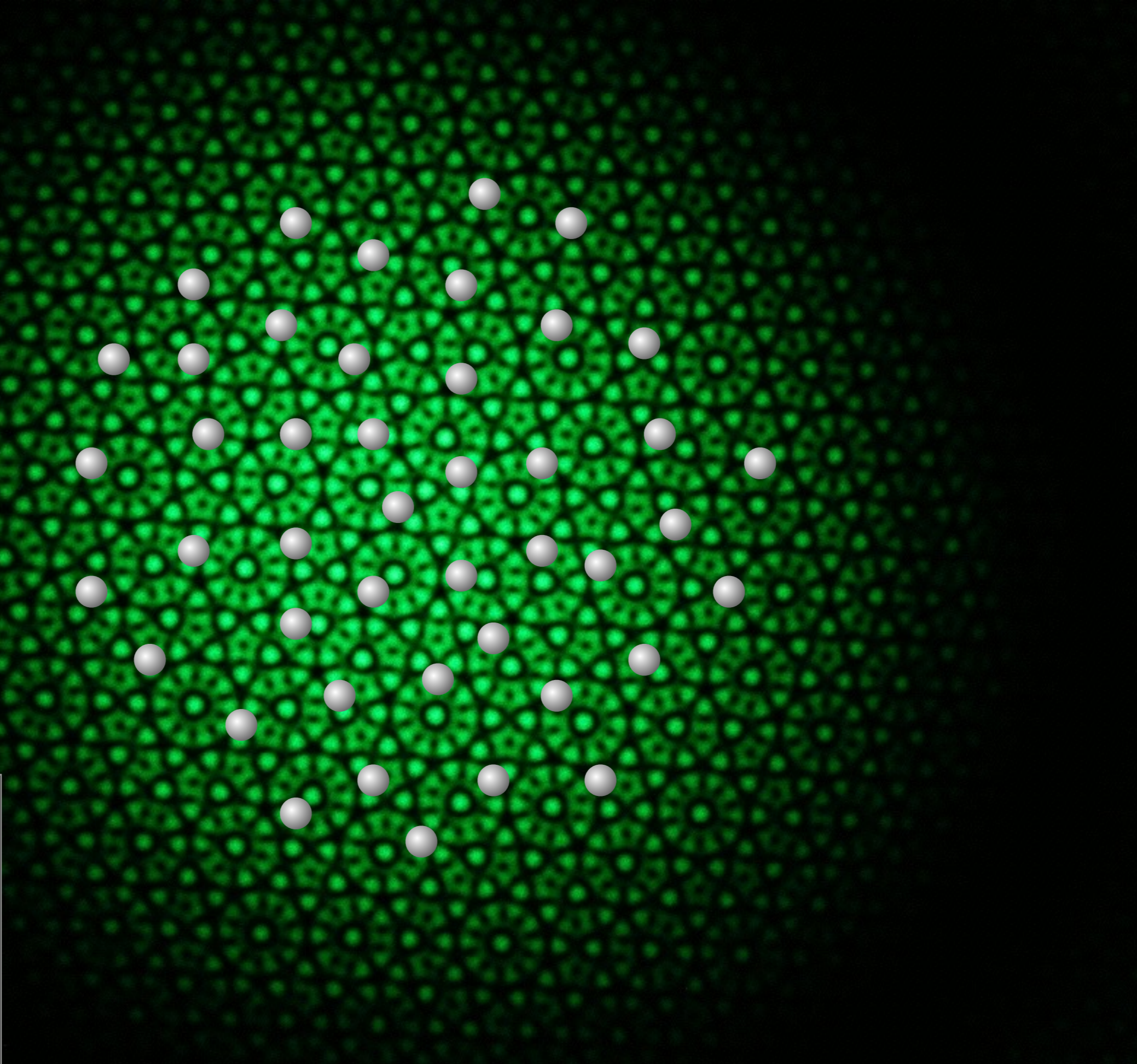
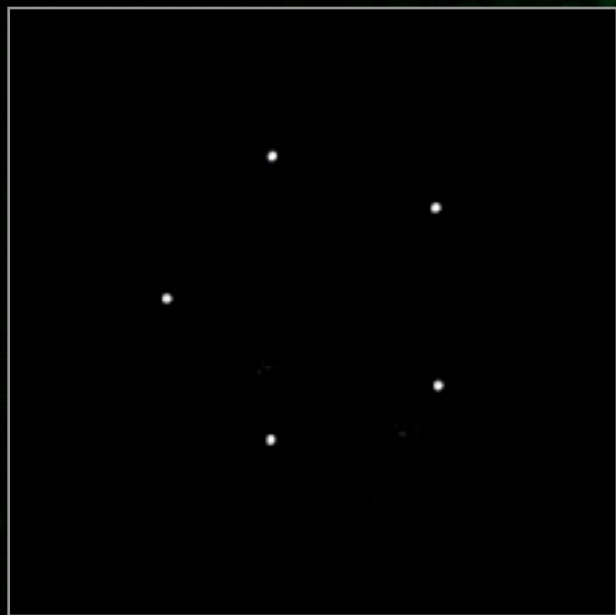


courtesy: T. Hänsch



courtesy: T. Hänsch



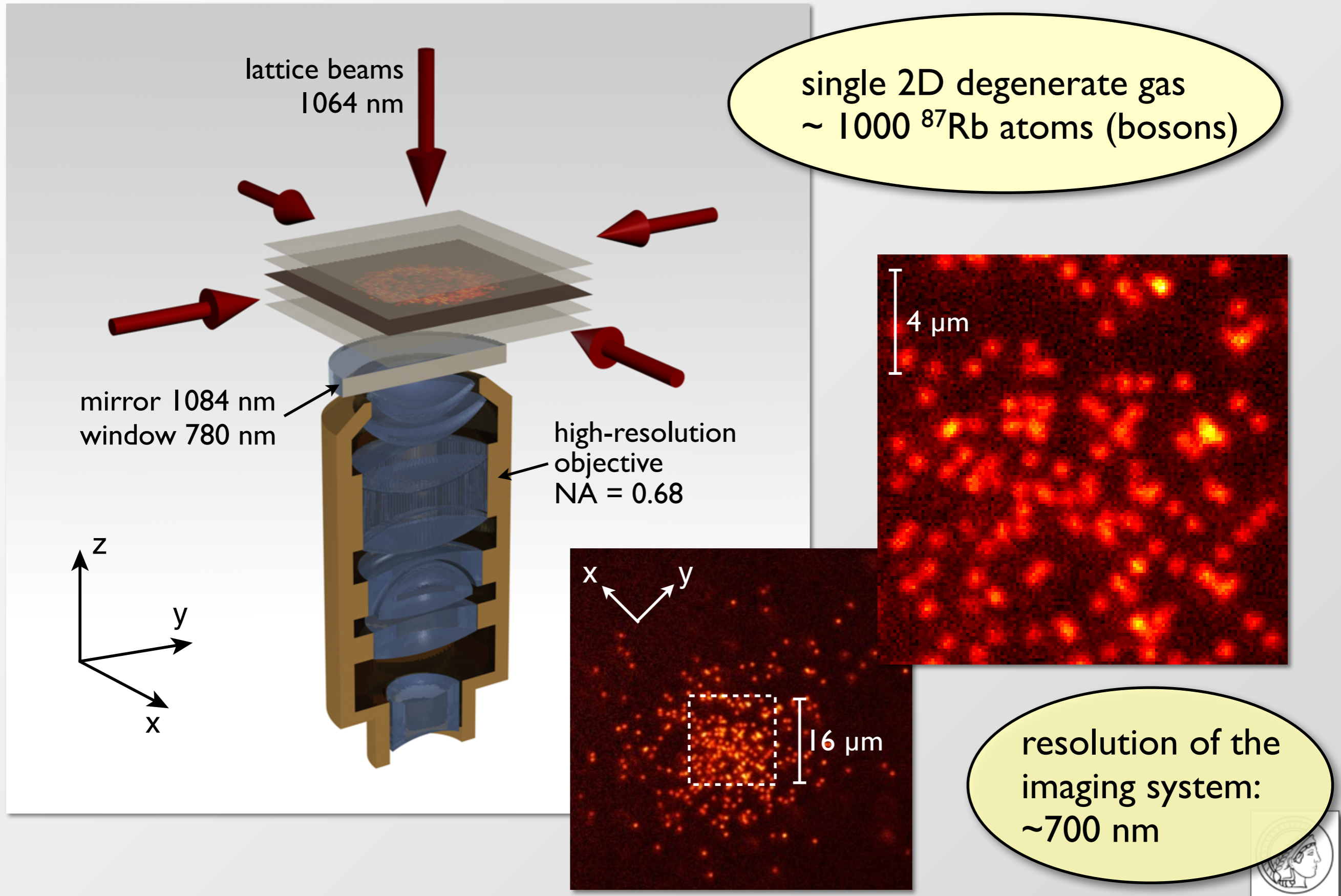


<https://www.youtube.com/user/SuperLaser123>

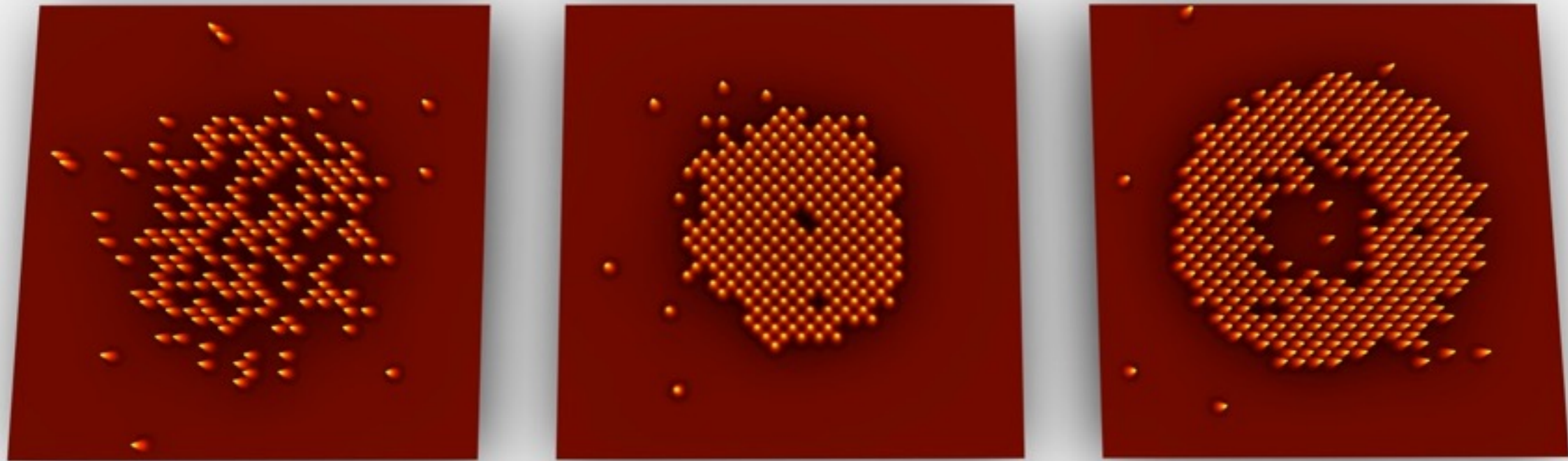
courtesy: T. Hänsch

Optical Lattices

Optical Lattices



Snapshot of an Atomic Density Distribution

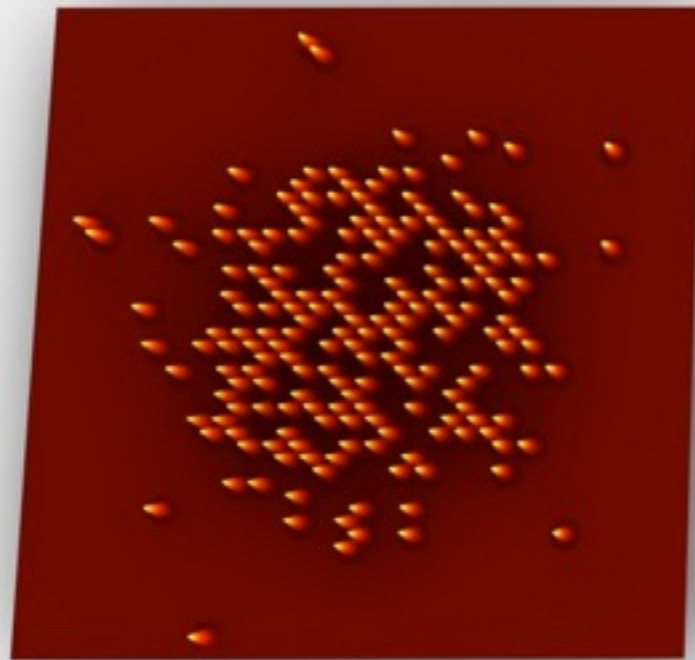


BEC

$n=1$
Mott Insulator

$n=1$ & $n=2$
Mott Insulator

Snapshot of an Atomic Density Distribution



BEC



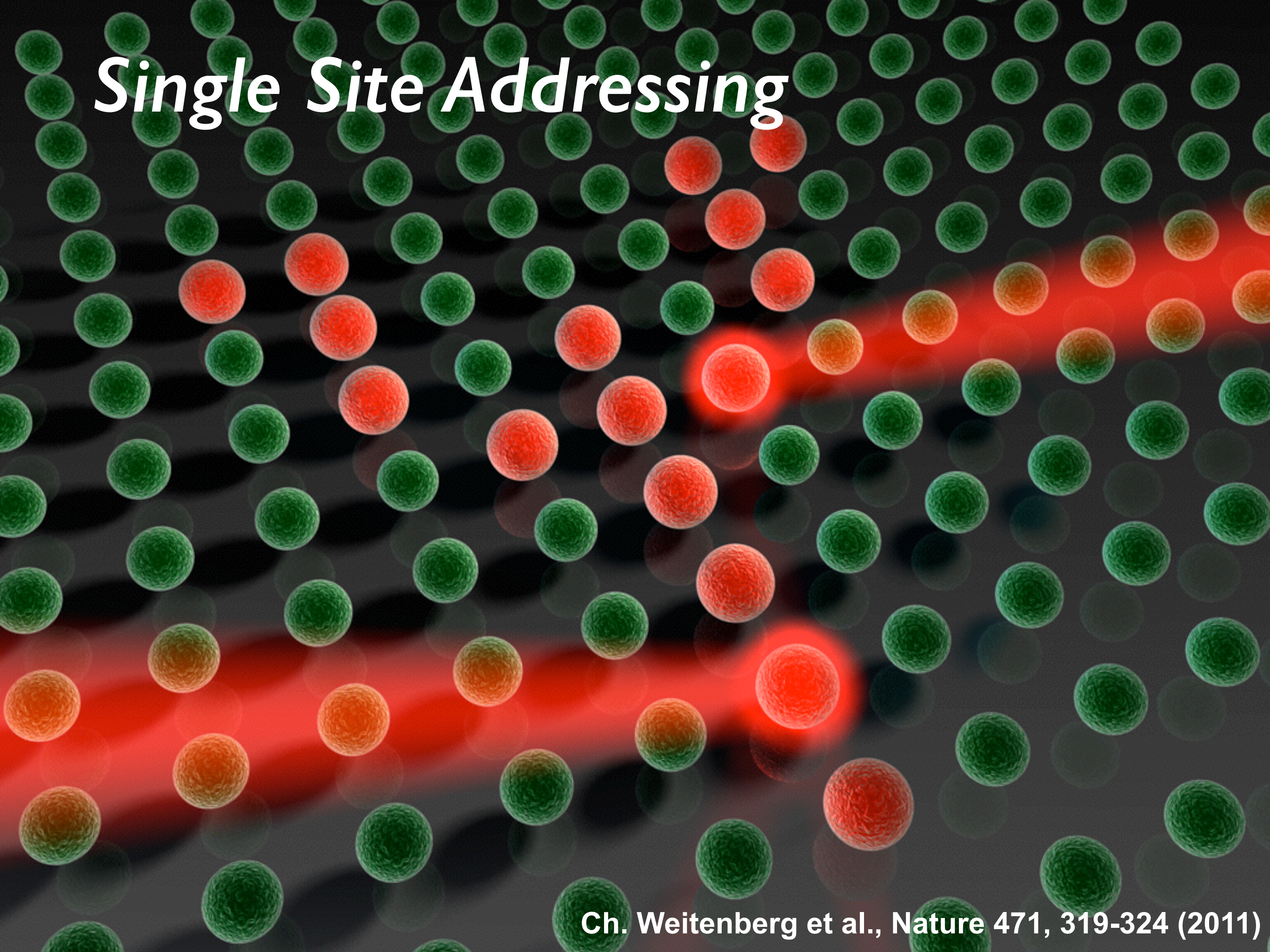
$n=1$
Mott Insulator

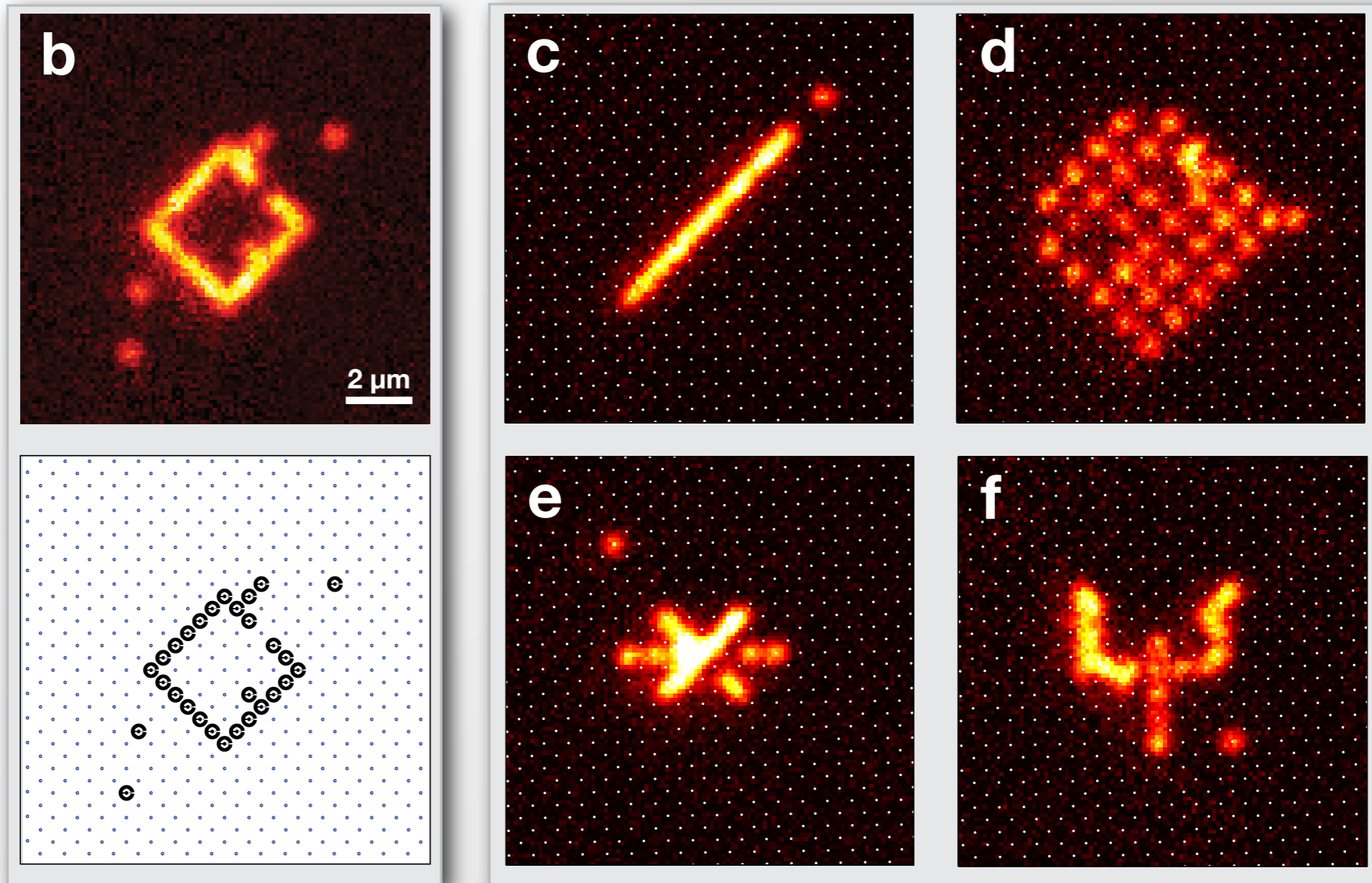


$n=1$ & $n=2$
Mott Insulator

Temperature
sensitivity
down to 50 pK!!

Single Site Addressing

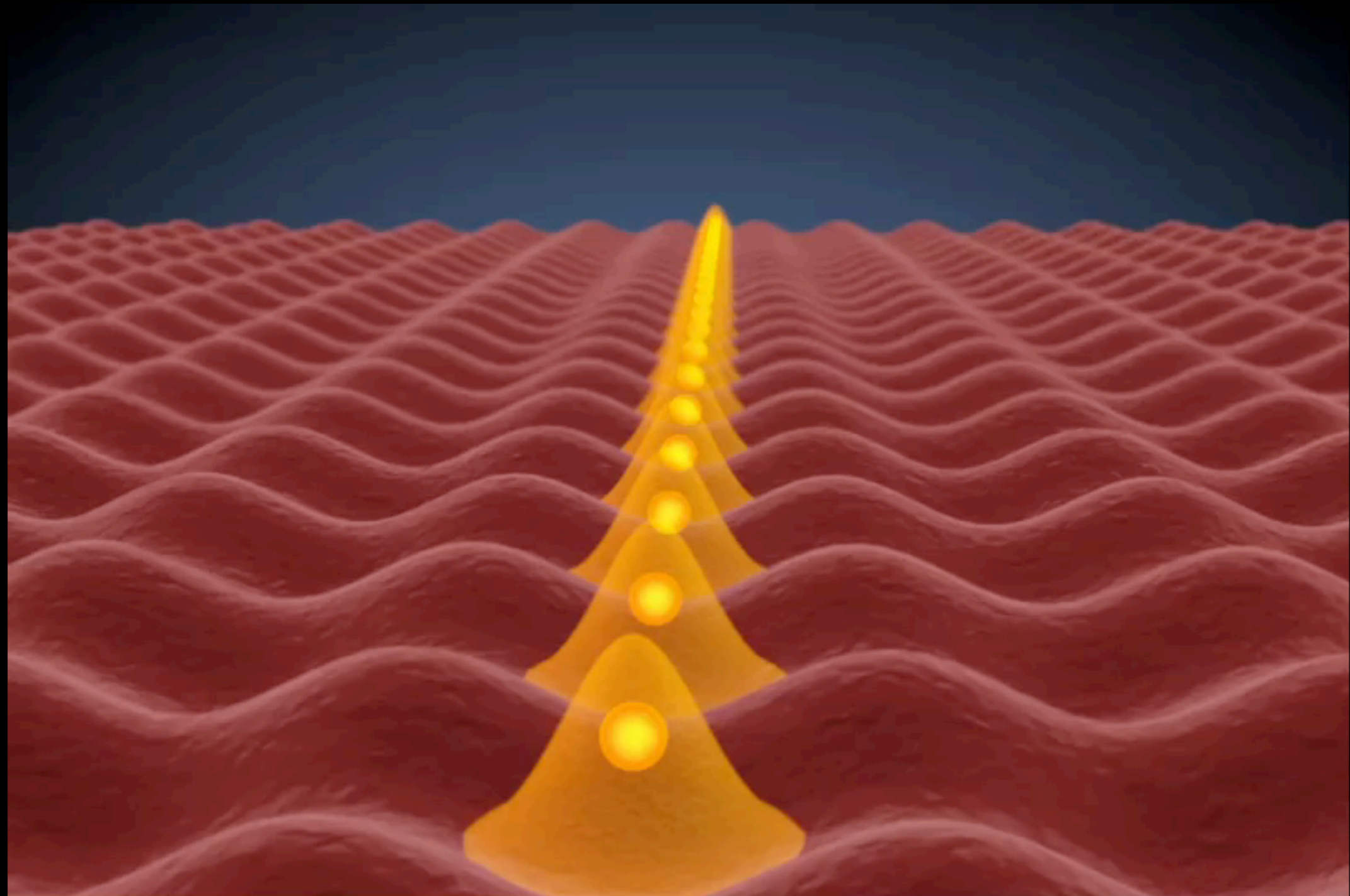
The image shows a 3D lattice of particles, represented as spheres. The majority of the spheres are green. A diagonal path of spheres, starting from the top center and moving towards the bottom right, is highlighted in red and orange. This path represents the 'single site addressing' mentioned in the title. The background is dark, and the lighting creates a sense of depth and perspective.



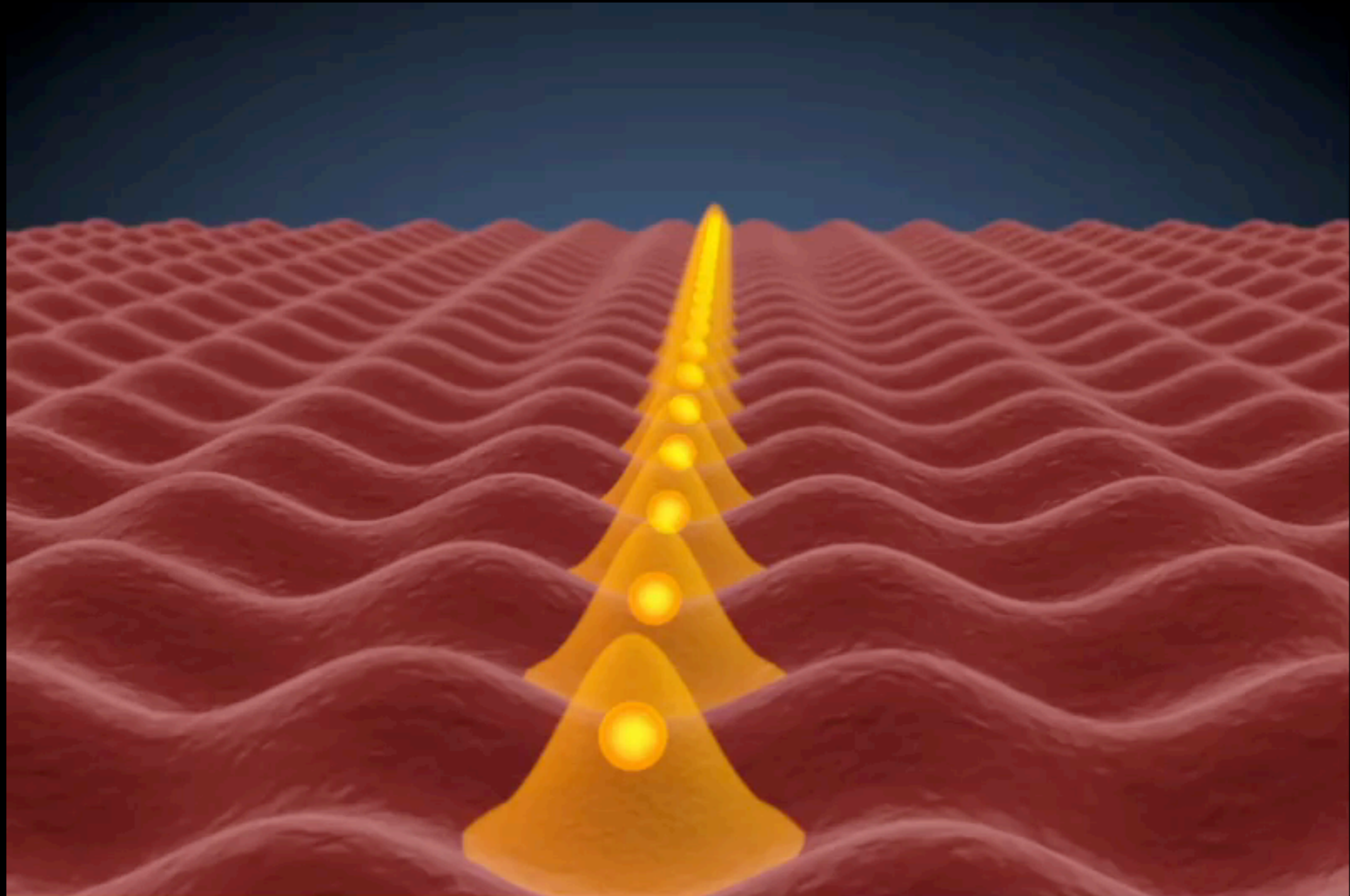
Subwavelength spatial resolution: 50 nm

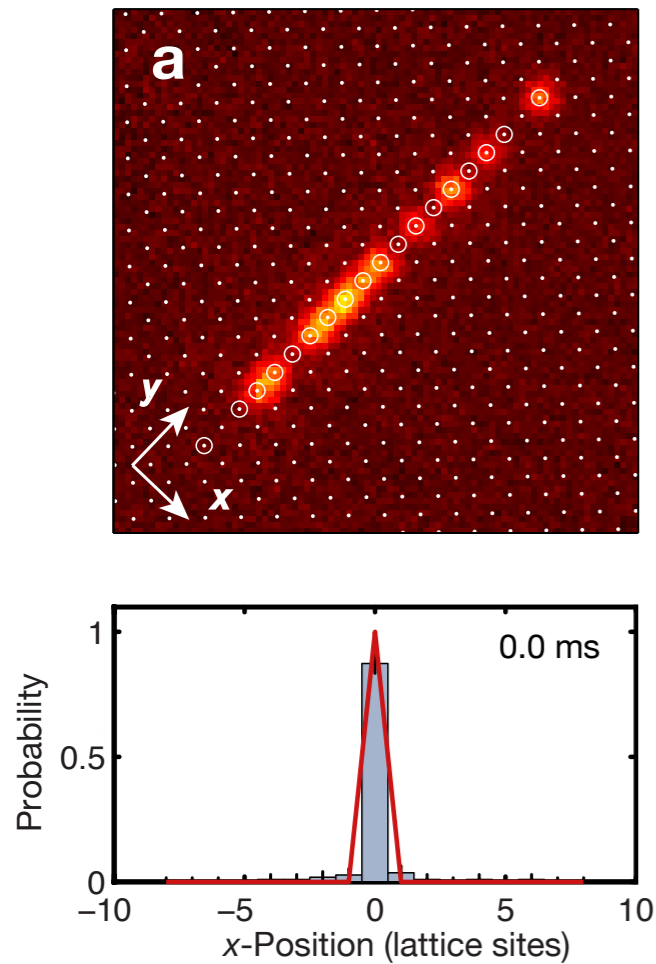


Single Atom Tunneling



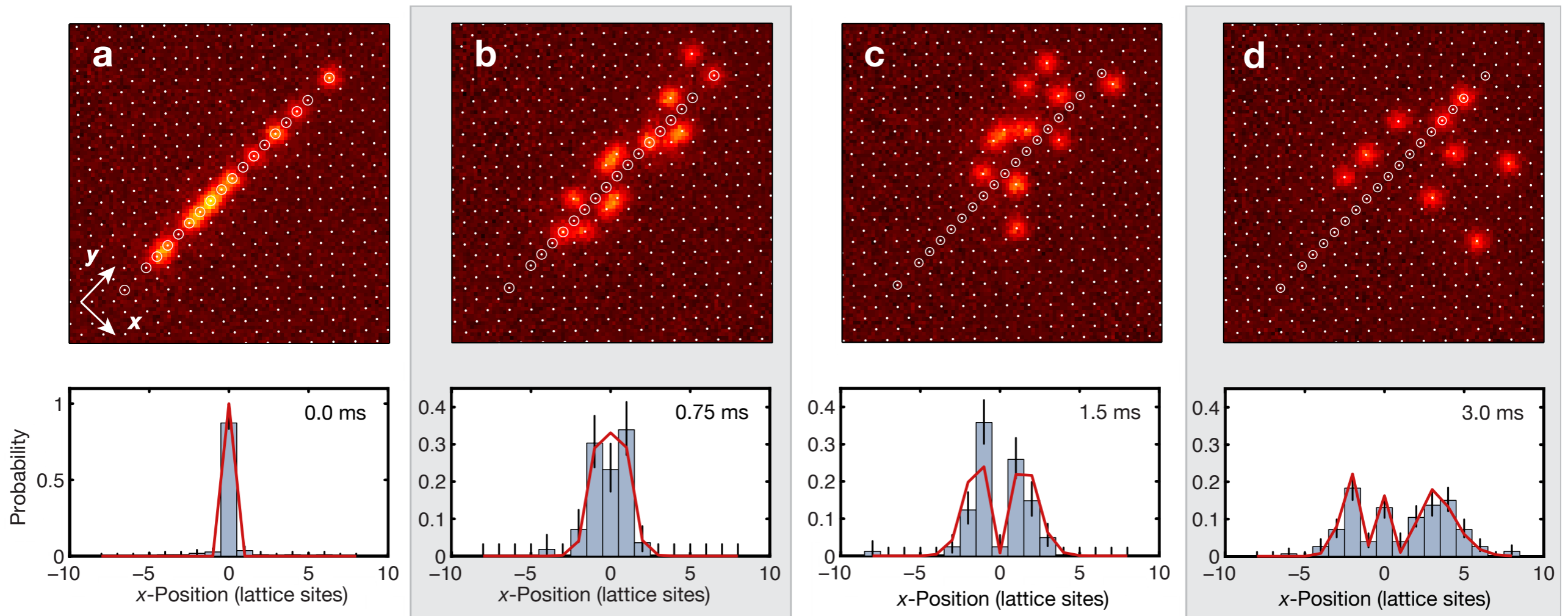
Single Atom Tunneling





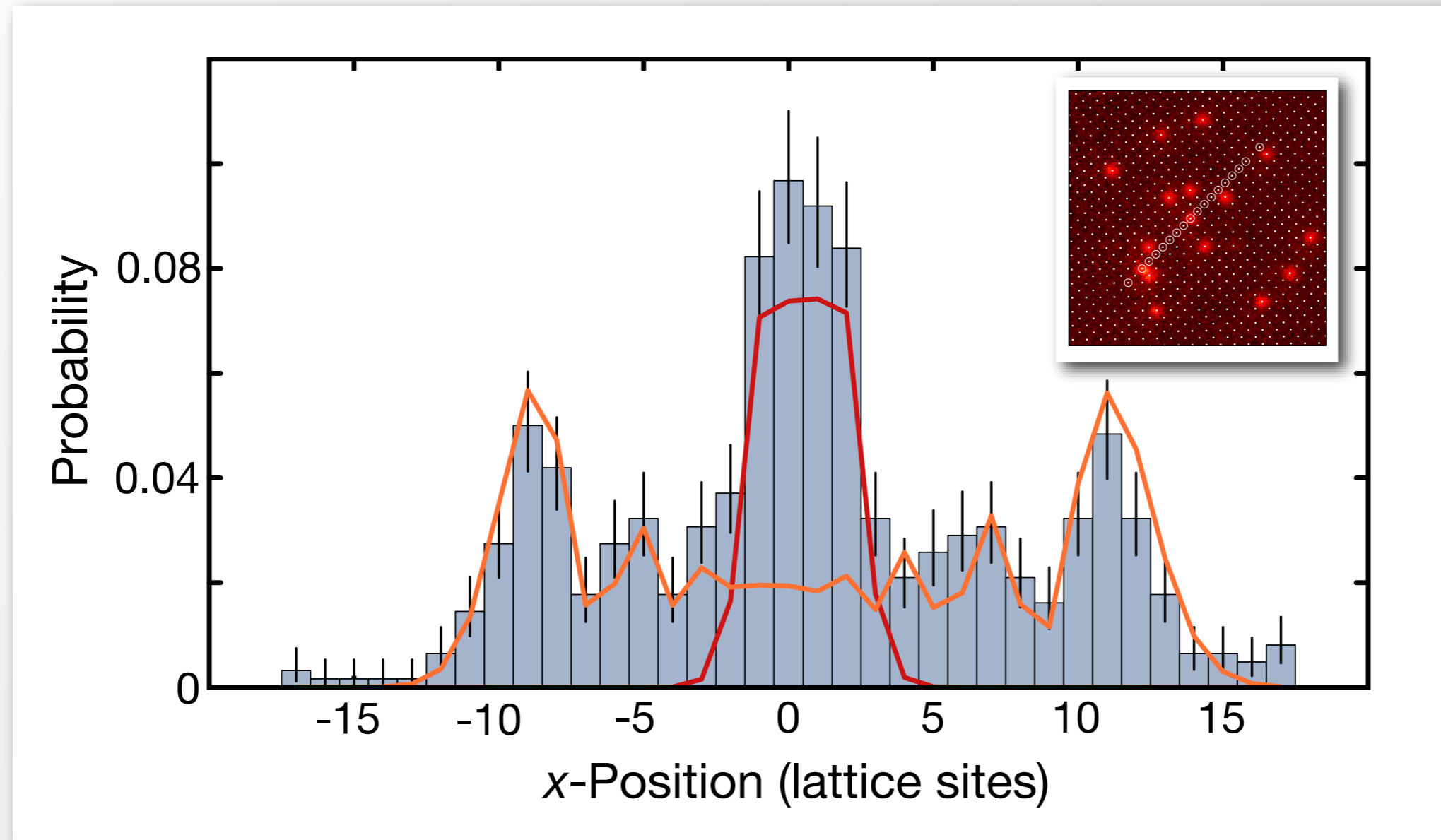
see exp: Y. Silberberg (photonic waveguides), D. Meschede & R. Blatt (quantum walks)...





see exp: Y. Silberberg (photonic waveguides), D. Meschede & R. Blatt (quantum walks)...

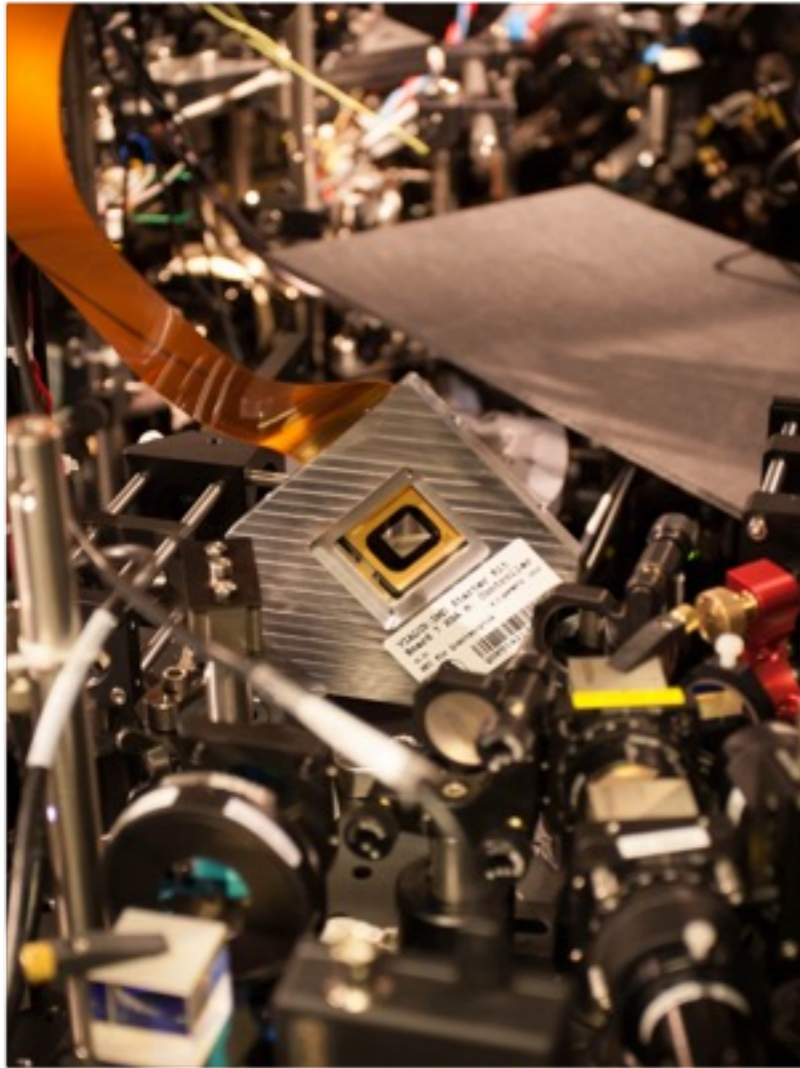




Excellent agreement with simulation.

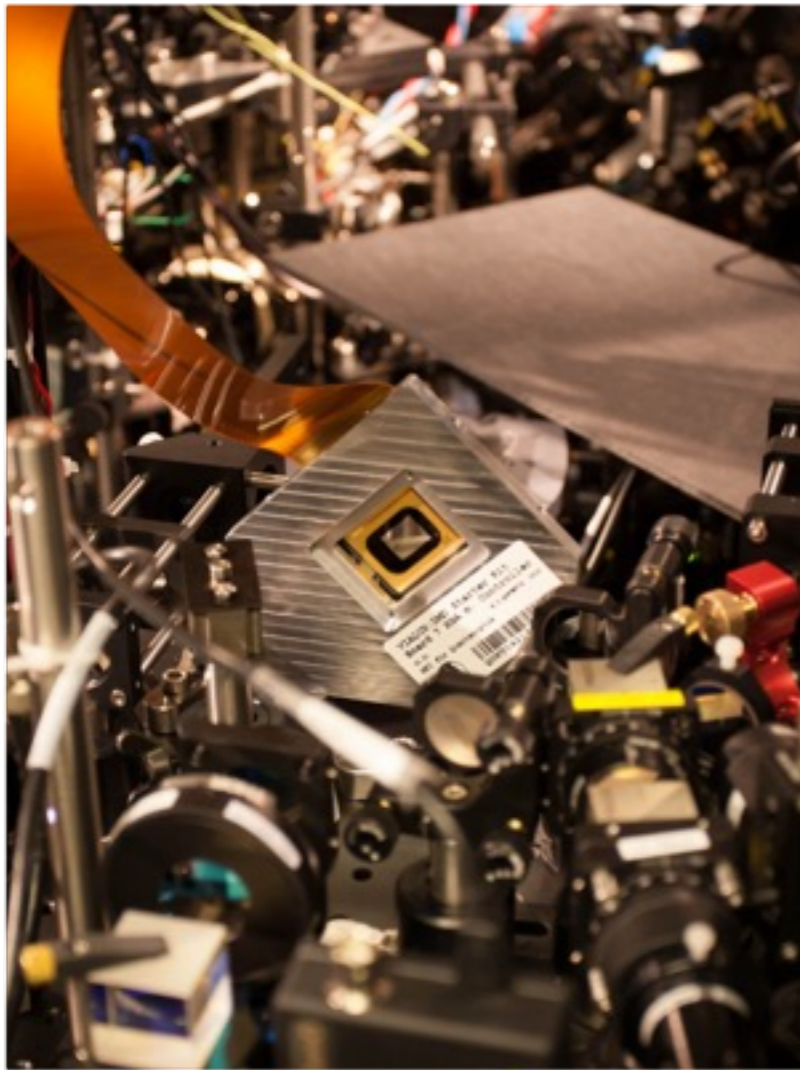
Interesting extension: Quantum walks of correlated atoms/spins...



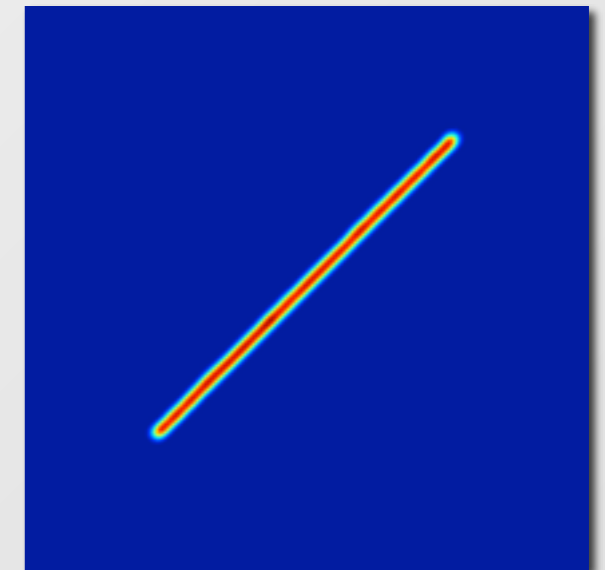
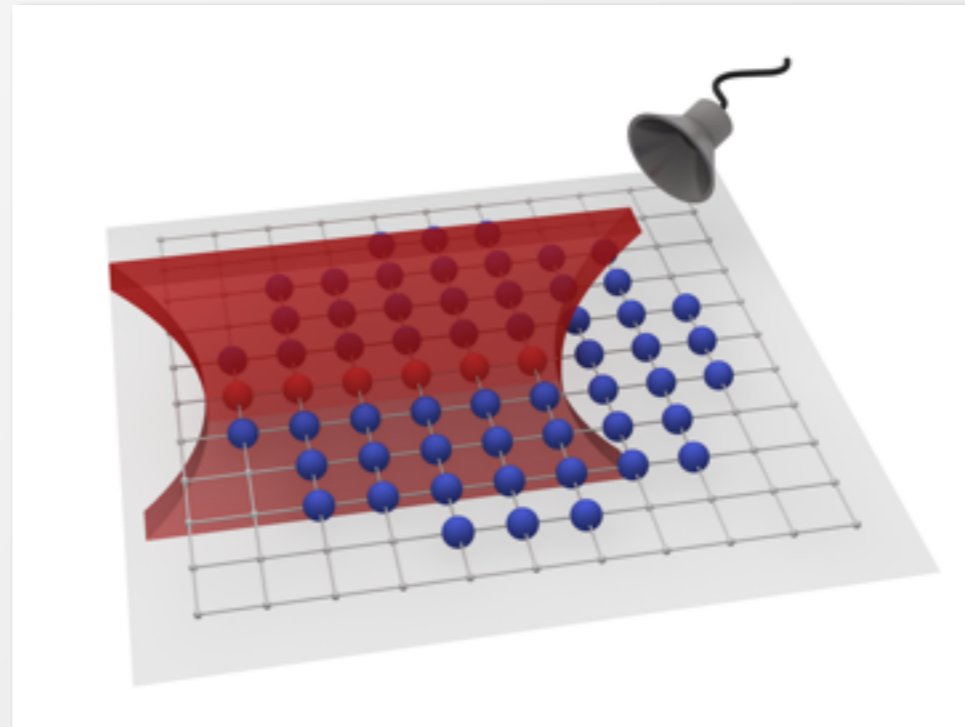


Digital Mirror Device
(DMD)



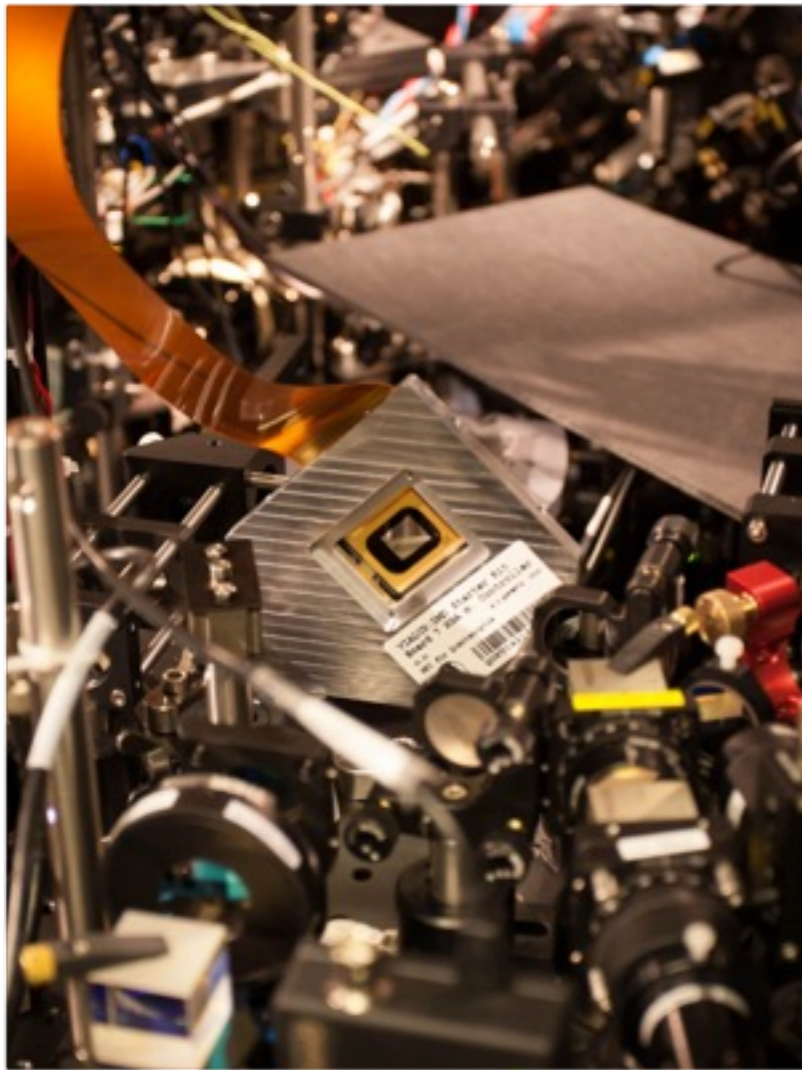


Digital Mirror Device
(DMD)

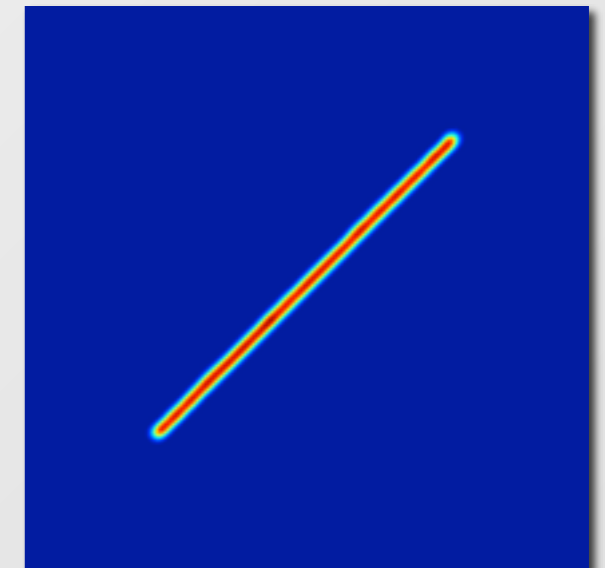
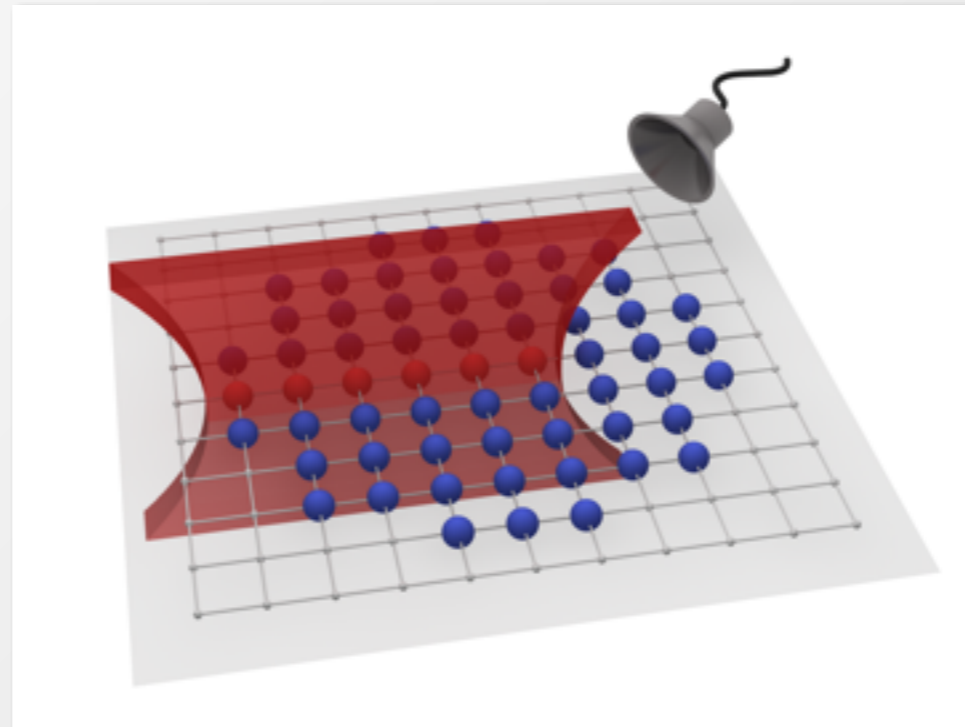


Measured Light Pattern

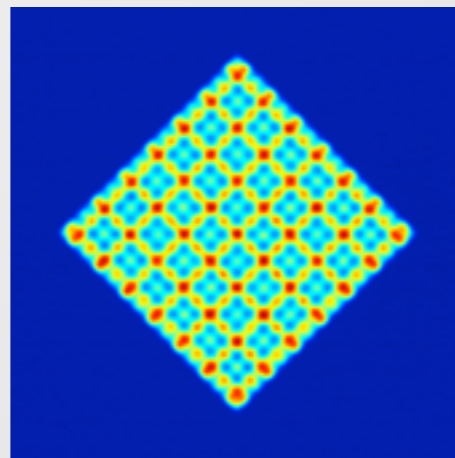




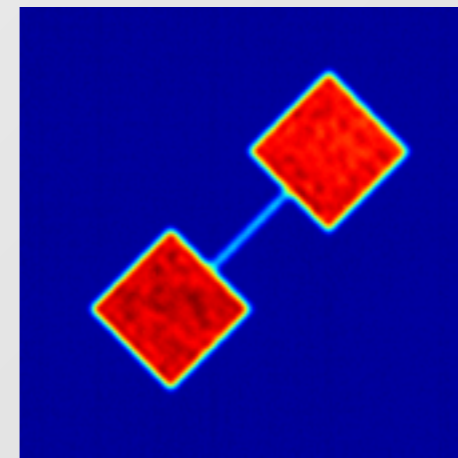
Digital Mirror Device (DMD)



Measured Light Pattern



Exotic Lattices



Quantum Wires

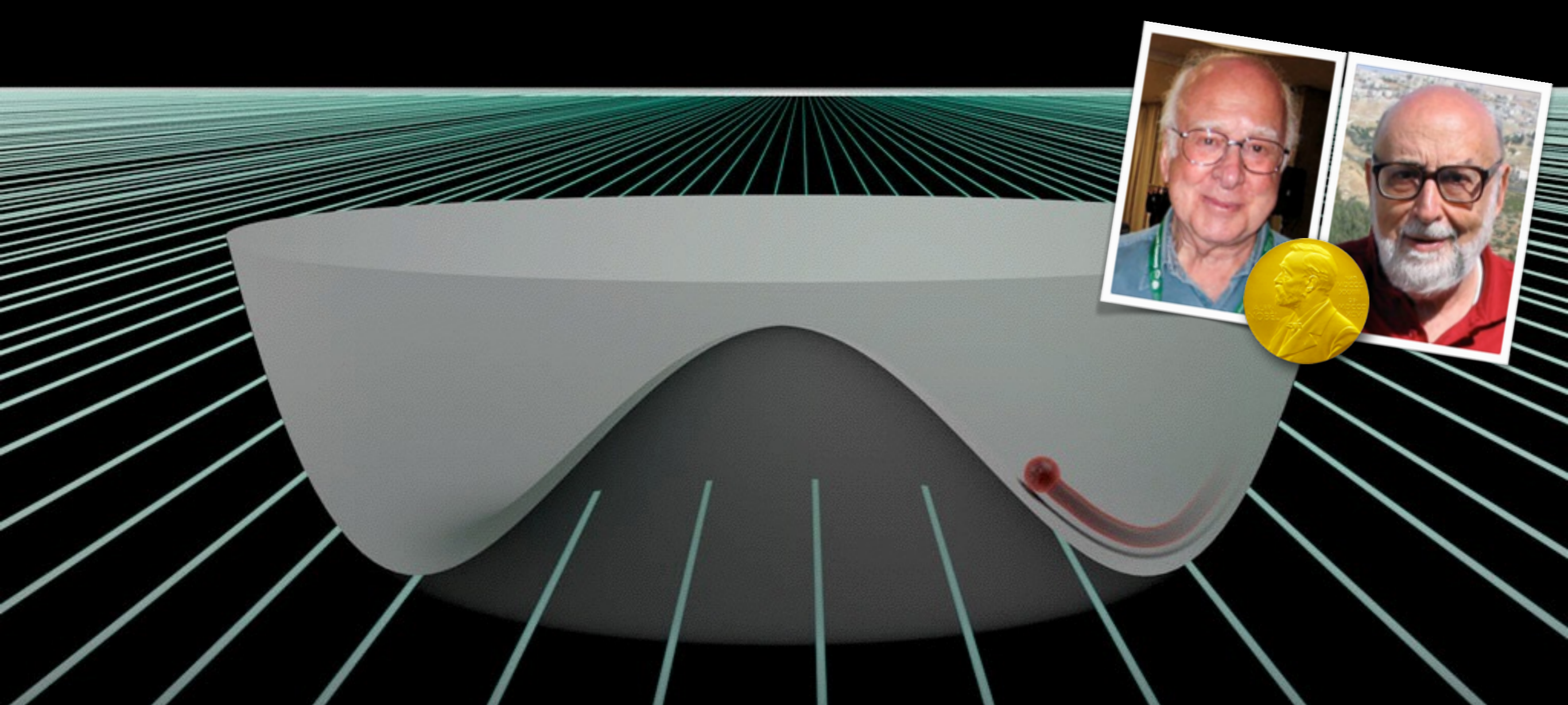


Box Potentials

Almost Arbitrary Light Patterns Possible!

Single Spin Impurity Dynamics, Domain Walls, Quantum Wires, Novel Exotic Lattice Geometries, ...





‘Higgs’ Amplitude Mode in Flatland

M. Endres, T. Fukuhara, M. Cheneau, P. Schauss, D. Pekker, E. Demler, S. Kuhr & I.B.

M. Endres et al. Nature (2012)

Chubukov & Sachdev, PRB 1993; Sachdev, PRB 1999; Zwerger, PRL 2004; Altman, Blatter, Huber, PRB 2007, PRL 2008; U. Bissbort et al. Phys. Rev. Lett. (2011); D. Podolsky, A. Auerbach, D. Arovas, PRB 2011



Quantum Matter at Negative Absolute Temperature

S. Braun, J.-P. Ronzheimer, M. Schreiber, S. Hodgman, T. Rom, D. Garbe, IB, U. Schneider

S. Braun et al. *Science* **339**, 52 (2013)

A. Mosk, *PRL* **95**, 040403 (2005), A. Rapp, S. Mandt & A. Rosch, *PRL* **105**, 220405 (2010)



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Science gets cold

By Charles Choi / February 24, 2013



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SCIENTIFIC METHOD / SCIENCE & EXPLORATION

Entropy drop: Scientists create "negative temperature" system



Negative Temperatures That Are Hotter Than The Sun

January 04, 2013 1:21 PM



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Science
MAGAZINE OF THE SOCIETY FOR

Explore

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Hottest temperature ever measured is a negative one
BY ANDREW GRANT 10:38PM, JANUARY 4, 2013

VIEWS

SCIENCE TICKER
Transport method within cells wins Nobel Prize in Medicine or Physiology

mea

Ultracold gas sets
BY ANDREW GRANT 10:38PM,
Magazine Issue: Februar

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Quantum gas goes below absolute zero

October 7, 2013
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Uncertain **PRINCIPLES**

with CHAD ORZEL 

PHYSICS, POLITICS, POP CULTURE

What Does "Negative Temperature" Mean, Anyway?

Posted by [Chad Orzel](#) on January 8, 2013

 (10)  Like 45  Tweet 31  +1 58  More »



3, 2013

Temperature?

... has an article entitled "Negative Temperature is measured in Kelvins (K)..."

... degrees Celsius...
... temperature of...
... would expect...

American Physical Society Sites: [APS](#) | [Journals](#) | [PhysicsCentral](#) | [Physics](#)



[Explore the Science](#) • [Ask & Experiment](#) • [Physics Buzz](#)

Explore the Science


- Physics in Action
- Physics +

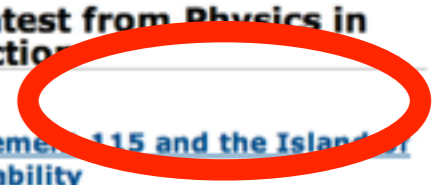
Below Absolute Zero: Negative Temperatures Explained

Absolute zero, or 0 degrees Kelvin, is the temperature where all motion stops. It's the lowest limit on the temperature scale, but recent news articles have heralded a dip below that limit in a physics lab. Is absolute zero less absolute than we thought? Read on to find out.

Latest from Physics in Action

[Element 115 and the Island of Stability](#)

Ununpentium, the 



Last 24 Hrs

Inc
PHYSICS.



(10)



Negative Temperatures are HOT - Sixty Symbols

 Sixty Symbols

[Subscribe](#) 592,824

727,265 views

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PS
EUN

degrees Ce
perature of
would exp

The world best clocks:

- **Navigation, Positioning**

GPS, GLONASS, deep space probes

- **Geodesy**

- **Datation of millisecond pulsars**

- **VLBI**

- **Synchronisation of distant clocks**

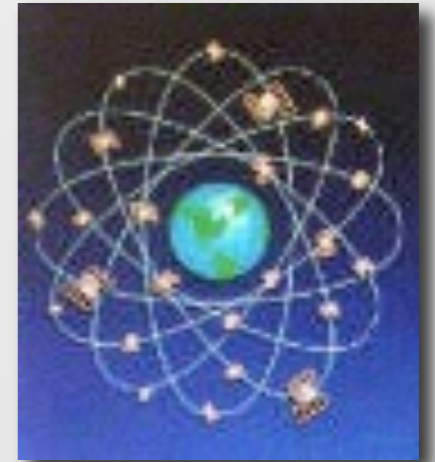
IAT

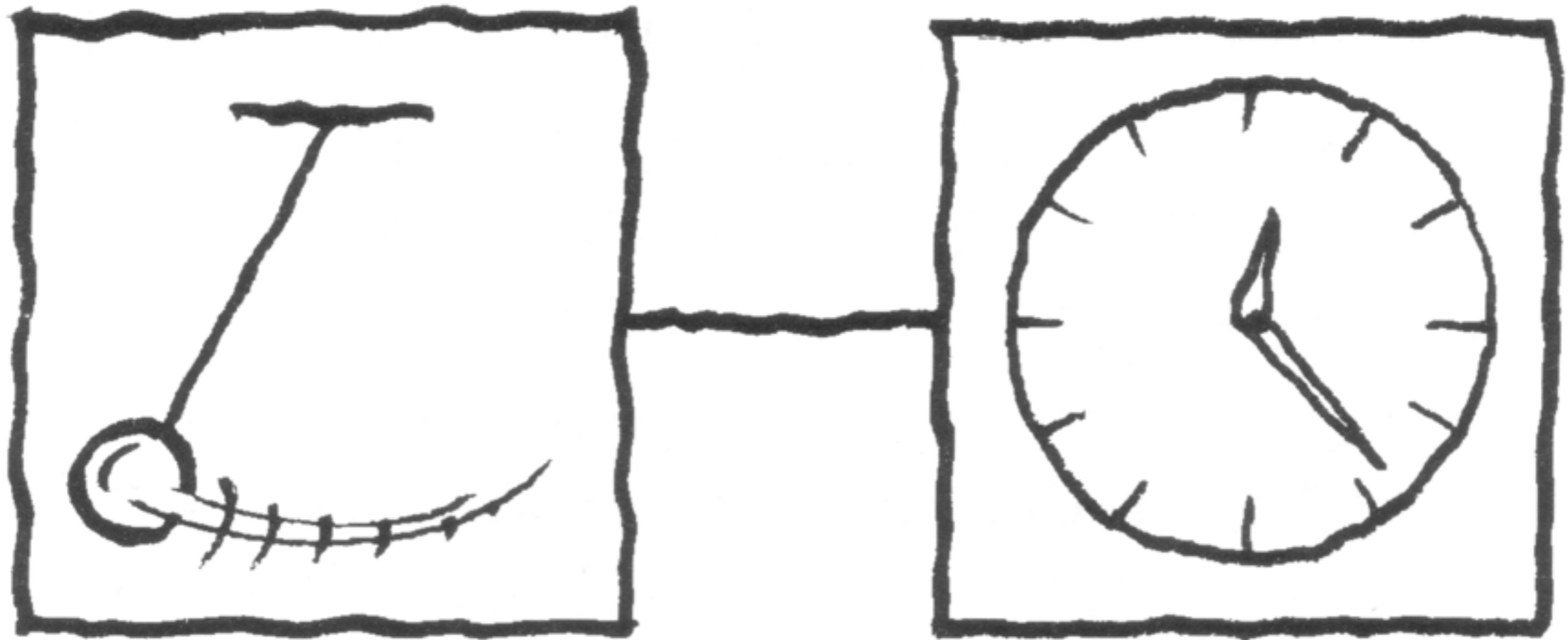
- **Fundamental physics tests**

Ex : general relativity

Search for a drift of the fine structure constant α :

$$\alpha^{-1} d\alpha / dt \text{ at } 10^{-16} / \text{year}$$





Clock = Oscillator + Counter

Sundial since 3500 v. Chr.
One period per dat



Sundial since 3500 v. Chr.
One period per day



Pendulum clock since 1656
One period per second

Sundial since 3500 v. Chr.
One period per day



Quartz oscillator since 1918
32.768 periods per second



Pendulum clock since 1656
One period per second

Sundial since 3500 v. Chr.
One period per day



Quartz oscillator since 1918
32.768 periods per second

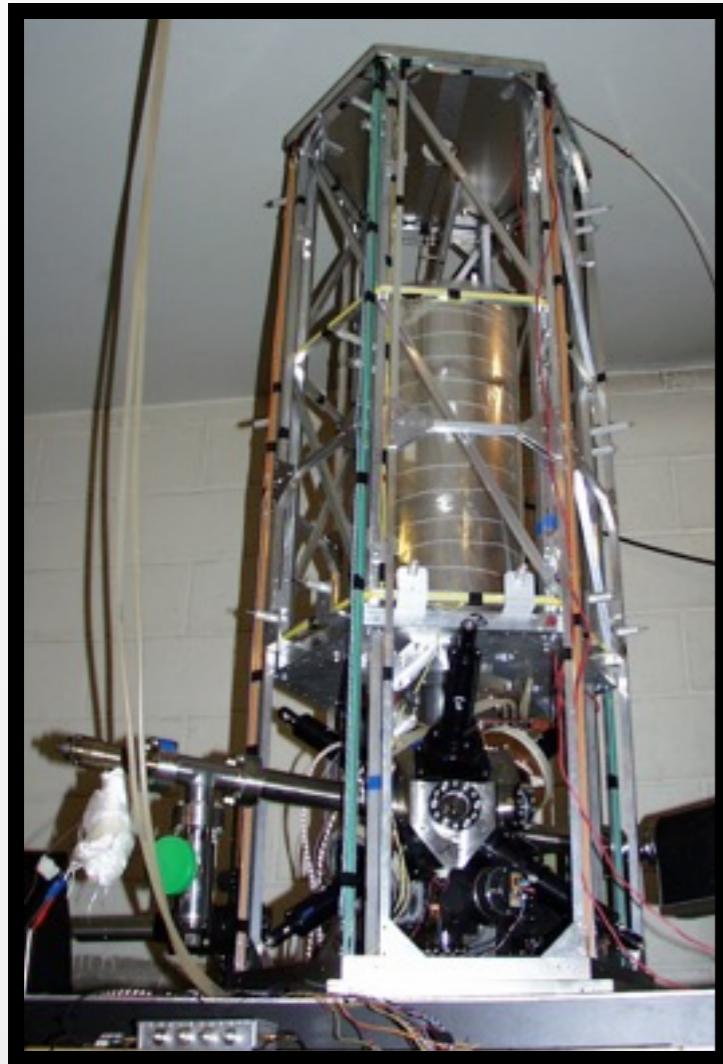


Pendulum clock since 1656
One period per second



Cesium atomic clock since 1955
9.192.631.770 oscillations per second

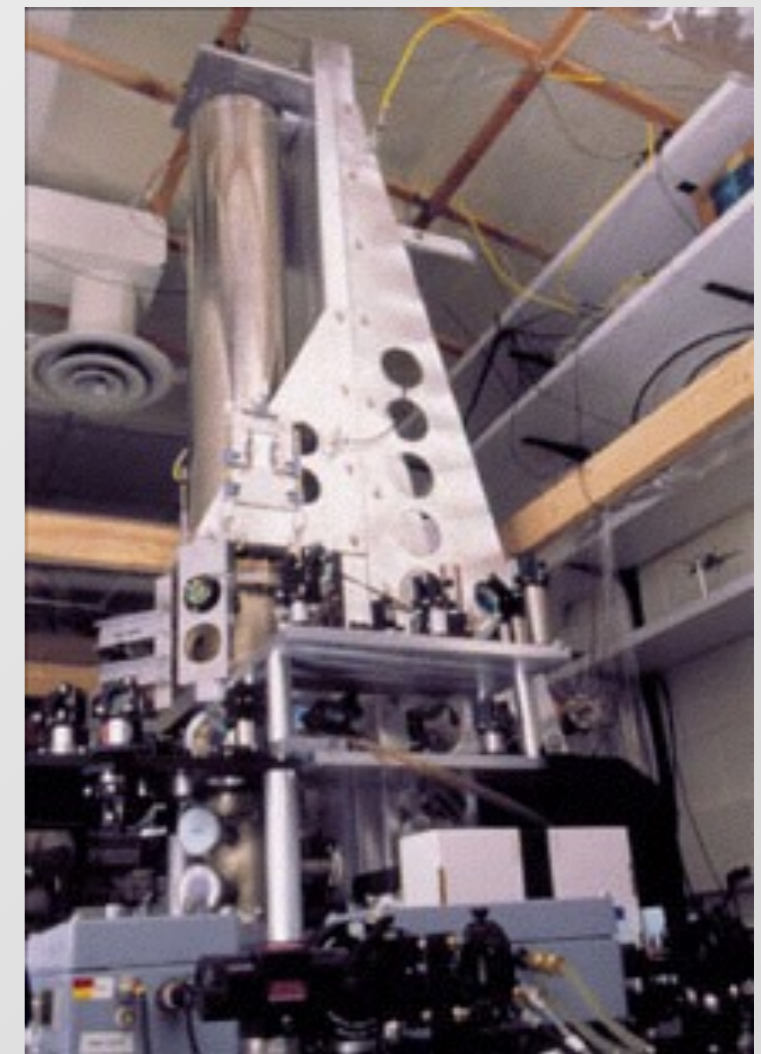
8 fountains in operation at SYRTE, PTB, NIST, USNO, Penn St, IEN, ON. 5 with accuracy at $1 \cdot 10^{-15}$. More than 10 under construction.



BNM-SYRTE, FR



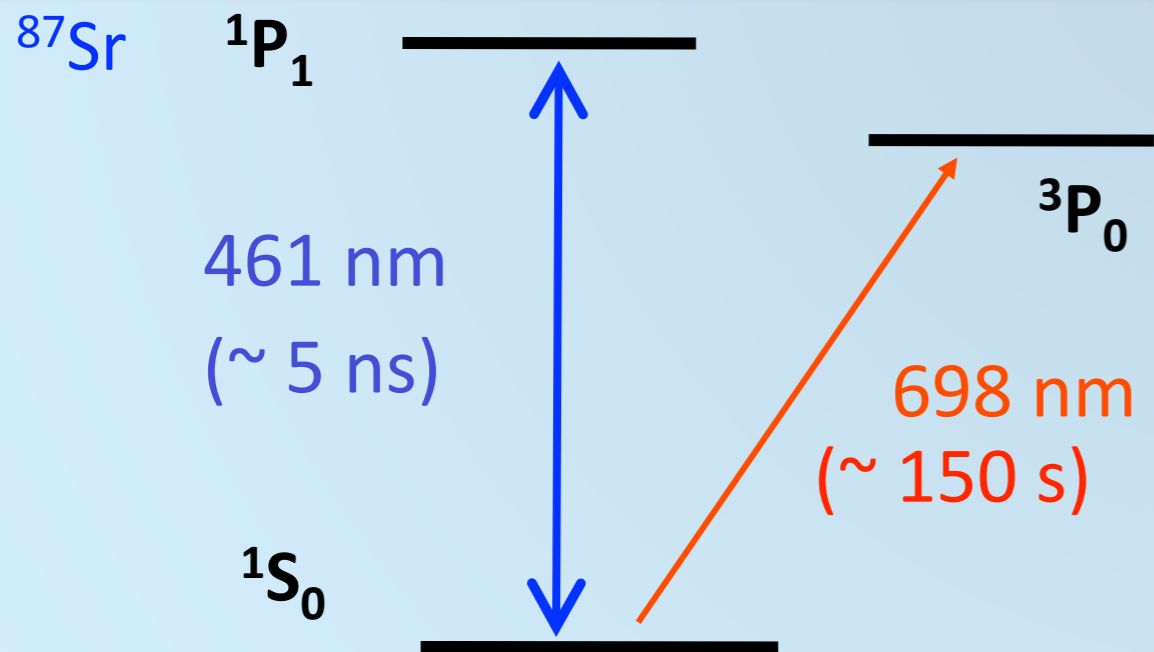
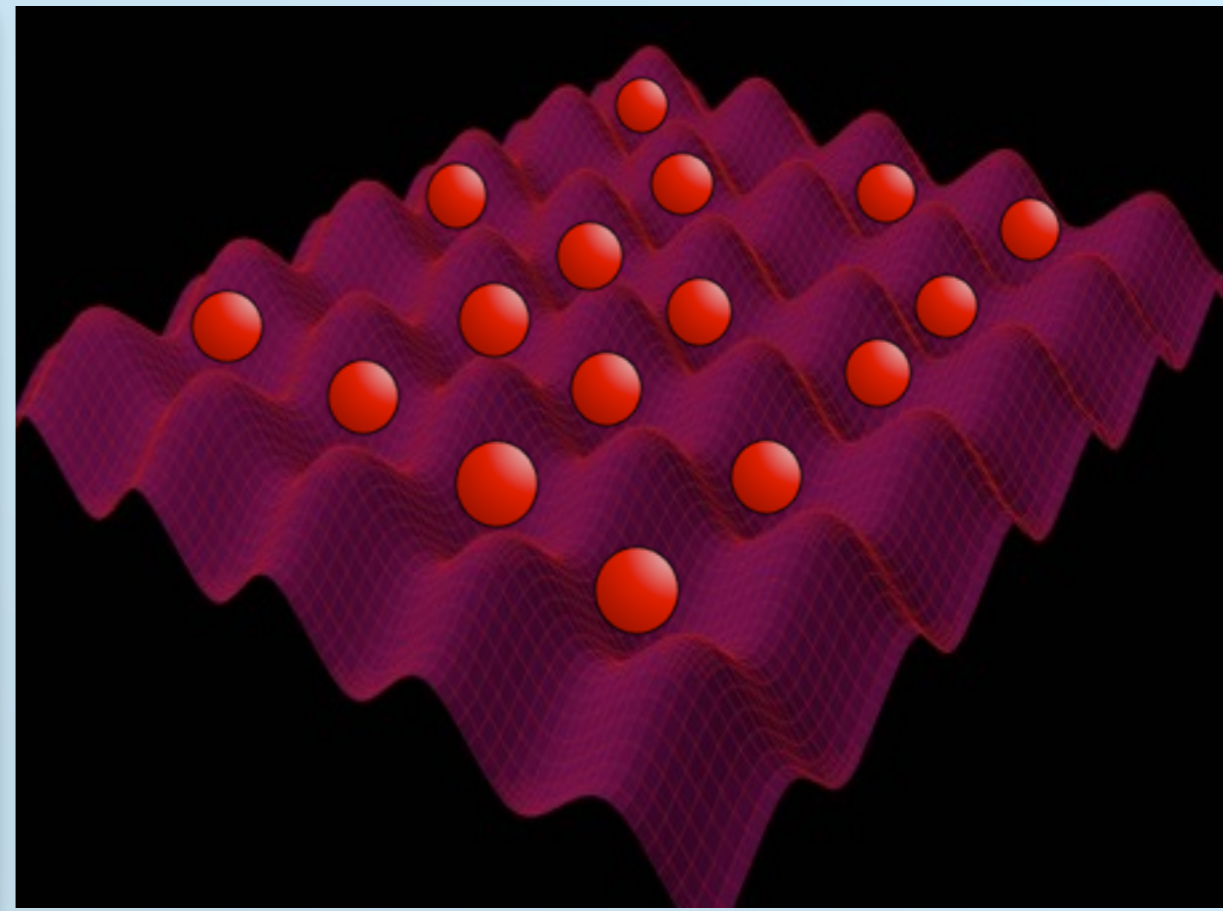
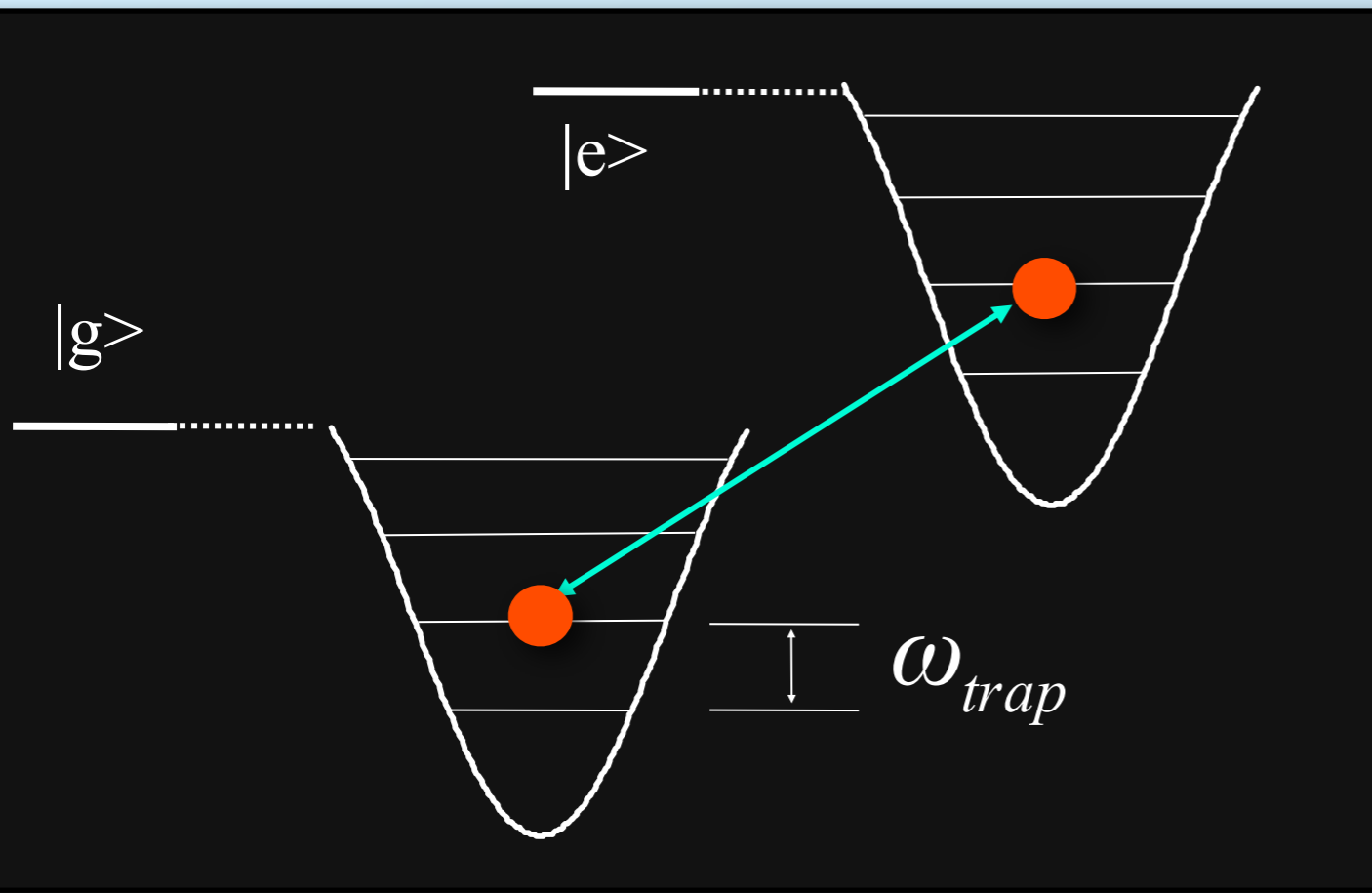
PTB, D



NIST, USA



The best clock: atoms in optical lattices

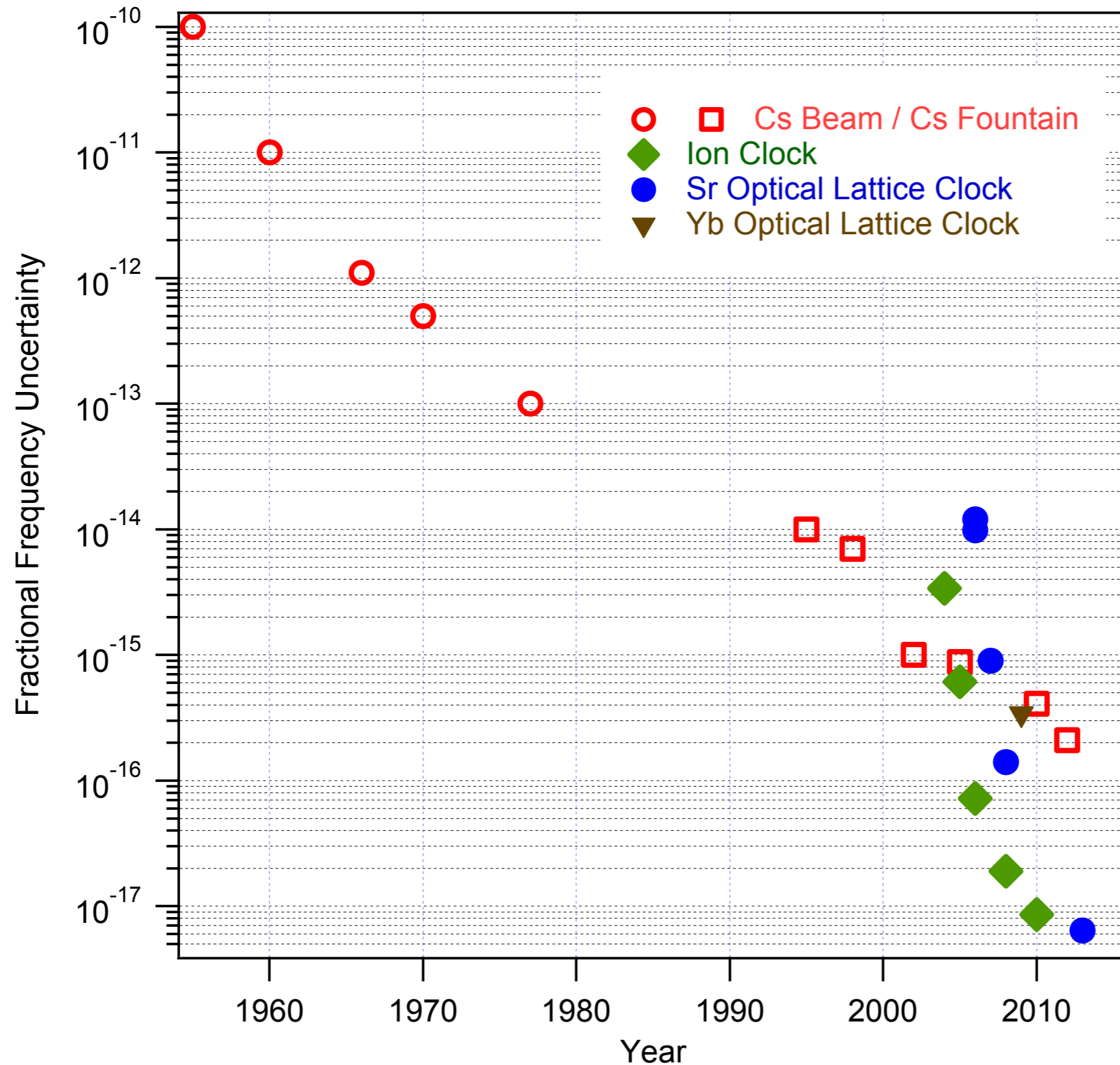


Quality factor $> 10^{17}$

Optical dipole moment
 $\sim 10^{-4} - 10^{-5}$ Debye

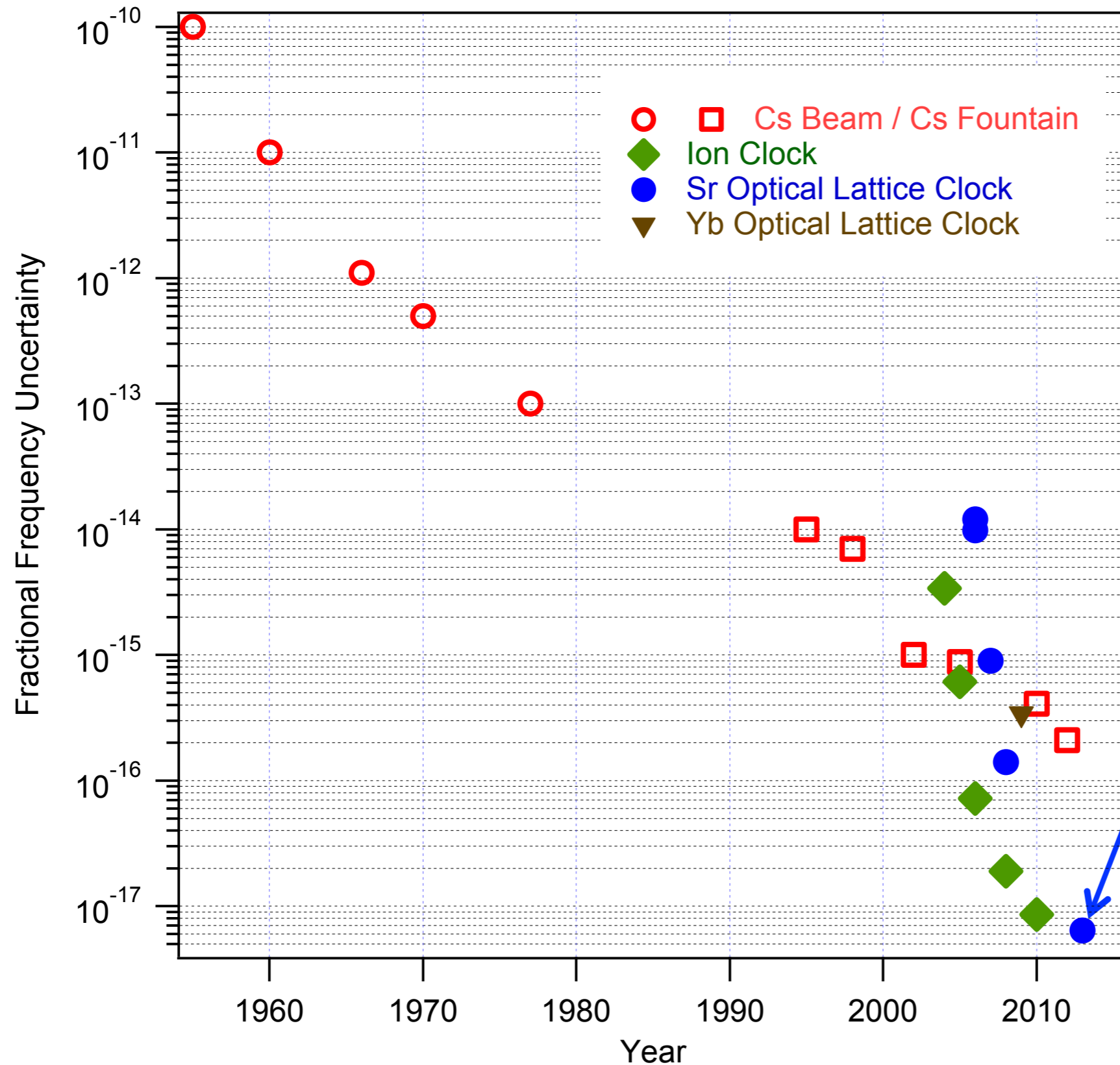
Boyd et al., *Science* **314**, 1430 (2006).

Sr clock - a new frontier for stability & accuracy



Sr clock - a new frontier for stability & accuracy

Bloom *et al.*,
arXiv:1309.1137



Sr: lowest
uncertainty in all
atomic clocks:
 6.4×10^{-18}

Achieving this
x 100 faster
than ion clocks



The inaccuracy of such a clock corresponds to 1s over the entire lifetime of the universe!

Outlook

- Search for New Phases of Matter
- Extremely Strong Magnetic Field Physics
- Novel Quantum Magnets
- Controlled Quasiparticle Manipulations
- Non-Equilibrium Dynamics (Universality?)
- Thermalization in Isolated Quantum Systems
- Entanglement Measures in Dynamics
- Supersolids
- Cosmology - Black Hole Models?
- High Energy Physics/String Theory
- New clocks/Navigation

**Quantitative testbeds
for theory!**

•
•
•

